

A brief review on collectivity in small collision systems

Prithwish Tribedy
(Brookhaven National Laboratory)

A Virtual Tribute to Quark Confinement
and the Hadron Spectrum 2021
August 2-6, 2021

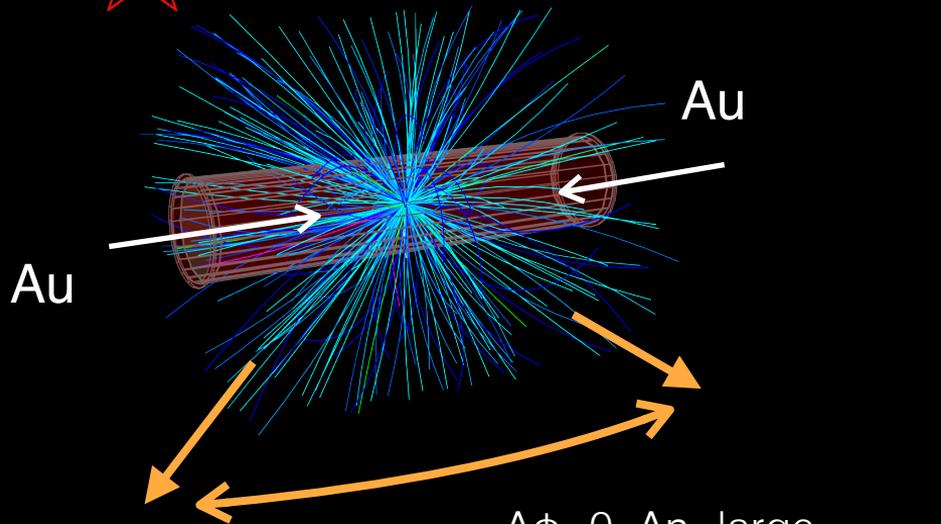
Outline

- Introduction
 - My definition of collectivity & why it is interesting
- What drives collectivity in small collision systems ?
 - Key players in the game
- Pinning down the origin of collectivity with RHIC small system scan
 - Predictions from initial state (CGC) and final state (Hydrodynamics)
- The hybrid framework to study collectivity in small systems
 - Framework combining CGC + Hydro. and predictions
- Strong acceptance dependence and puzzle with triangular flow
 - Where do we see shape engineering works?
- Further attempts to distinguish initial & final state effects
 - Correlation between transverse momentum and anisotropy harmonics
- Most recent venture: Collectivity in Photon included collisions
 - Collectivity search & building a bridge between RHIC/LHC and EIC

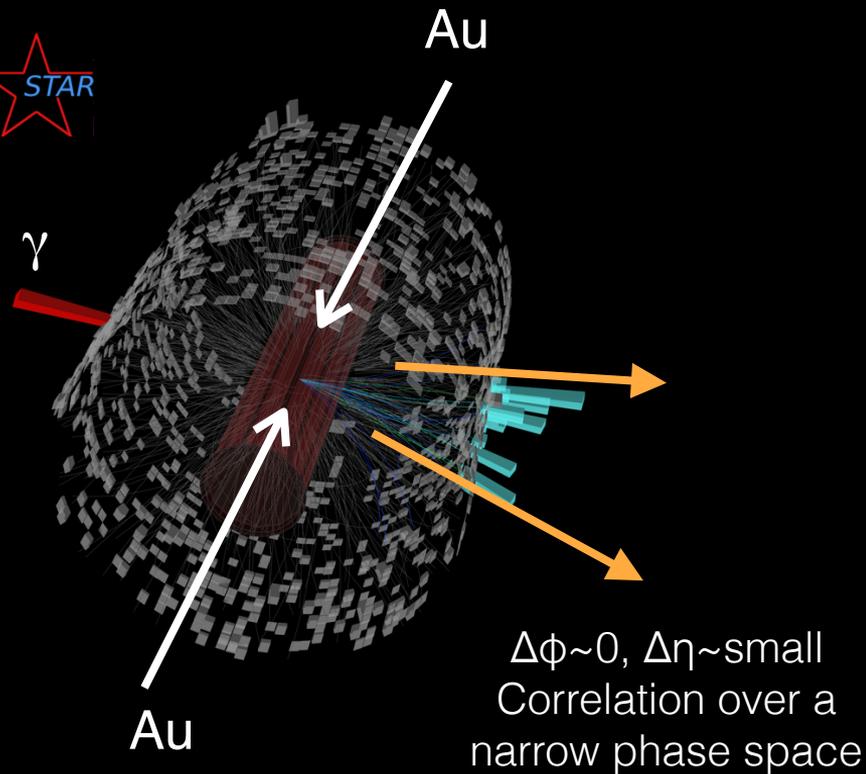
Pattern of particle emission



Au+Au 200 GeV Run# 17172038



$\Delta\phi \sim 0, \Delta\eta \sim \text{large}$
(Correlation pattern repeated over wide phase space)

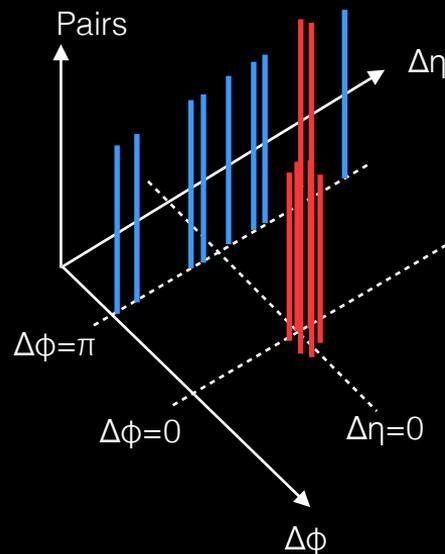
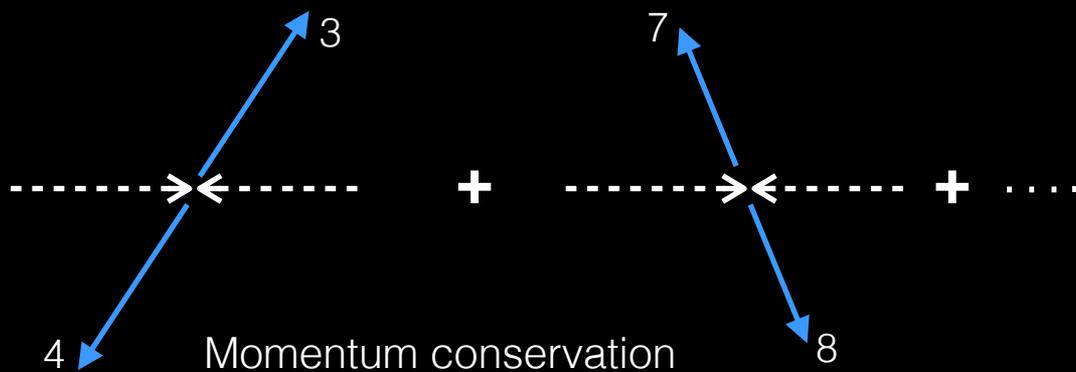
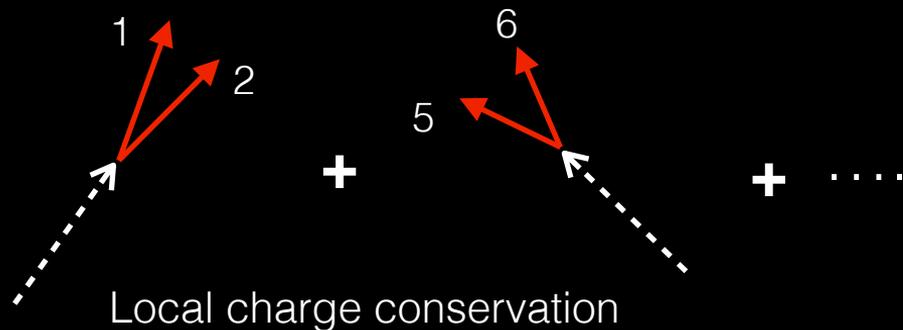


$\Delta\phi \sim 0, \Delta\eta \sim \text{small}$
Correlation over a narrow phase space

In collisions very often a pattern of particle emission is observed that span over a wide phase space

What is collectivity ?

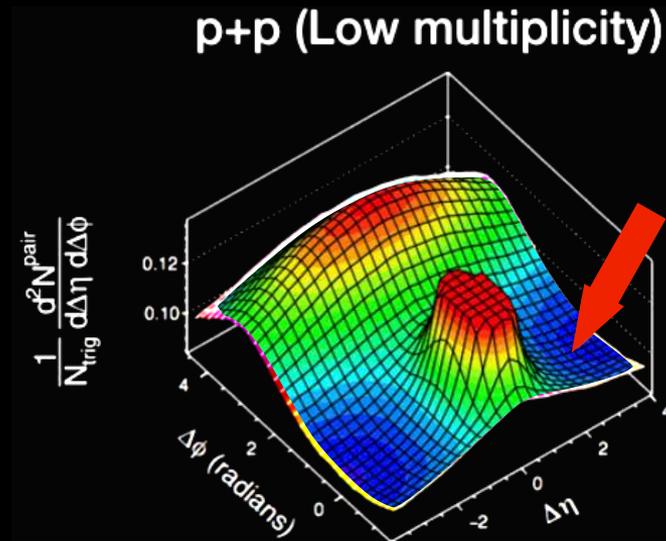
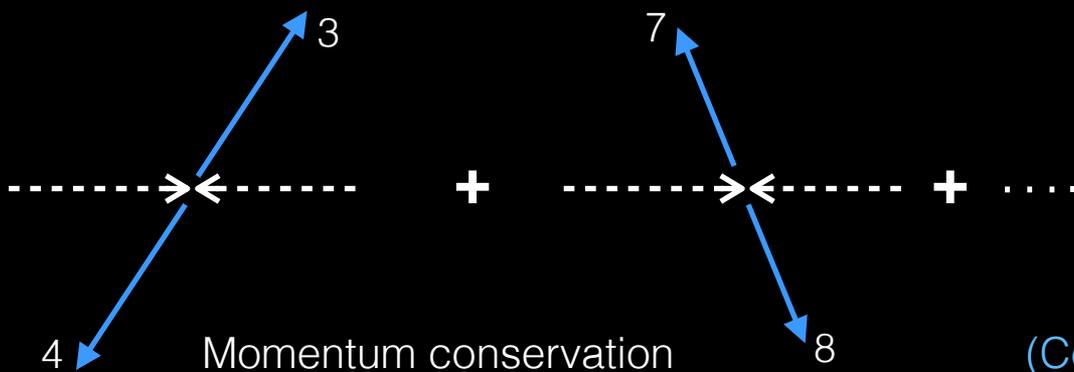
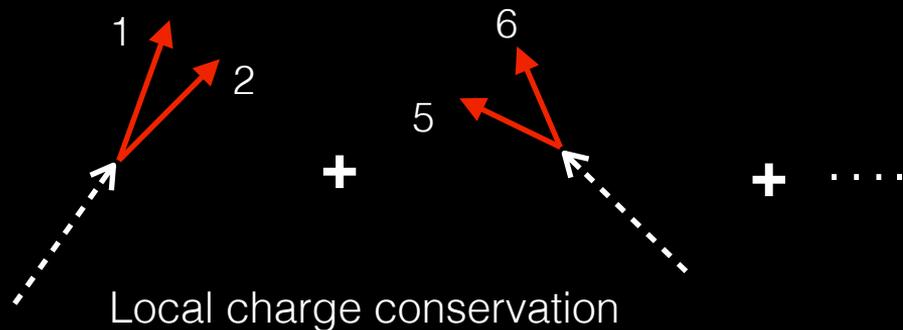
At fundamental levels conservation laws determine correlation among few particles



These correlations will not fill the full-phase space

What is collectivity ?

At fundamental levels conservation laws determine correlation among few particles

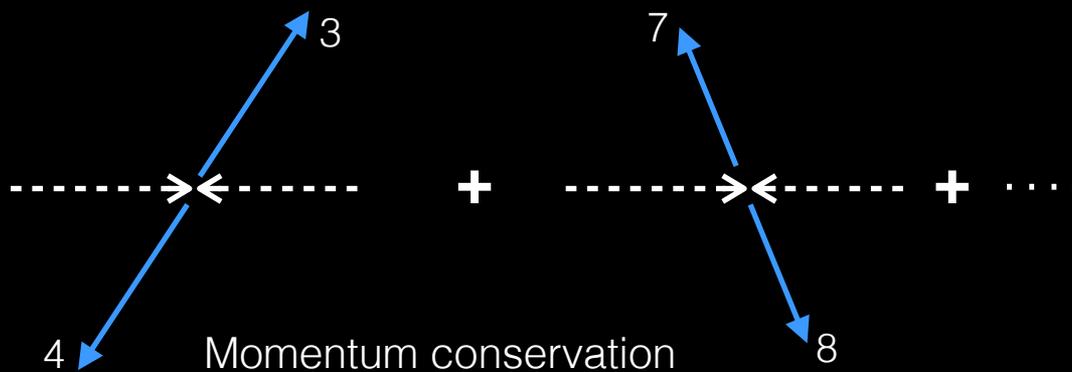
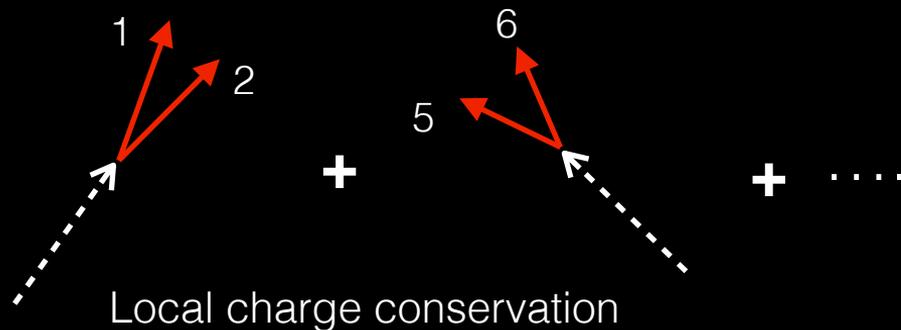


These correlations will not fill the full-phase space (Seen in experiment)

(Conservation \Rightarrow perfect configurations)

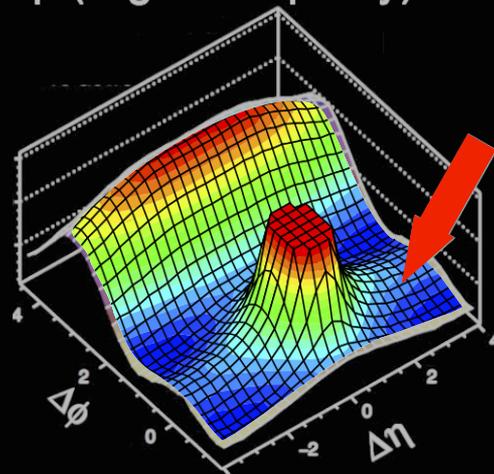
What is collectivity ?

At fundamental levels conservation laws determine correlation among few particles



p+p (High-Multiplicity)

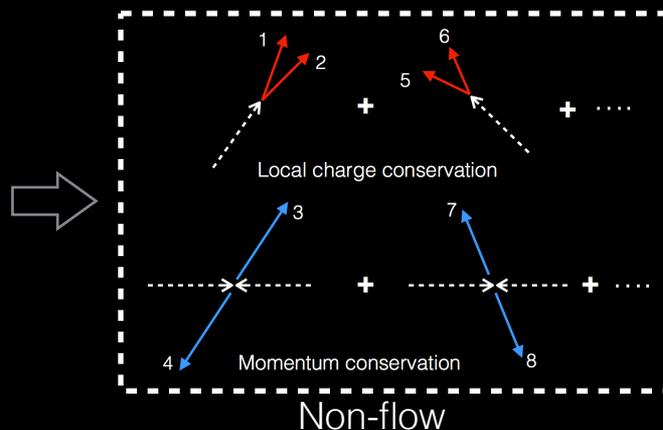
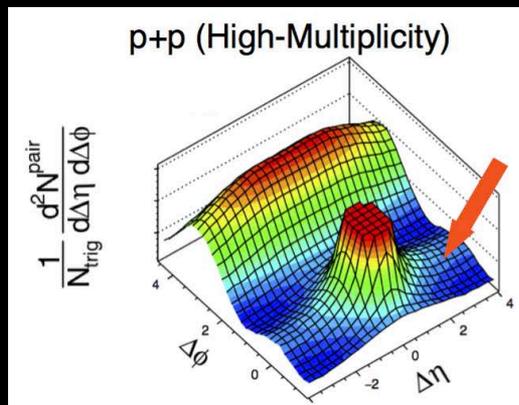
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$



Violation from such scenario is striking

What is collectivity ?

Deviations from these perfect configurations or correlation among few particles \Rightarrow Important physics at play (often non-perturbative)



+ New physics

Collectivity \Rightarrow observation of a specific pattern or behavior that is followed by most of its constituents in a system

Observing correlations among many must be accompanied by a large scale deviation \Rightarrow interesting to study with decreasing system size

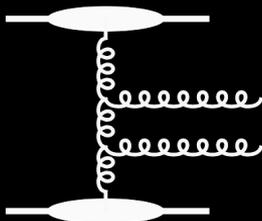
$Au+Au \rightarrow p+A \rightarrow p+p \rightarrow e(\gamma)+A \rightarrow e(\gamma)+p \rightarrow e+e$

What drives collectivity in small collision systems ?

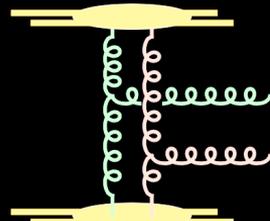
Origin of collectivity: initial state correlations from CGC

Quantum correlations due to
Bose enhancement / Glasma graphs

Di-Jet Graph

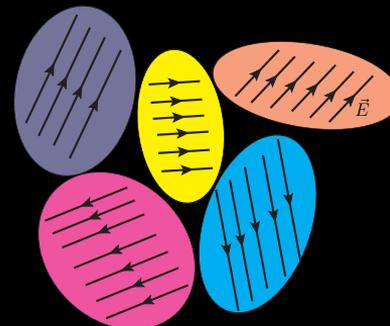


Glasma Graph



Enhanced probability to find two gluons with the same transverse momentum.

Classical correlations due to
local anisotropy $1/Q_s$

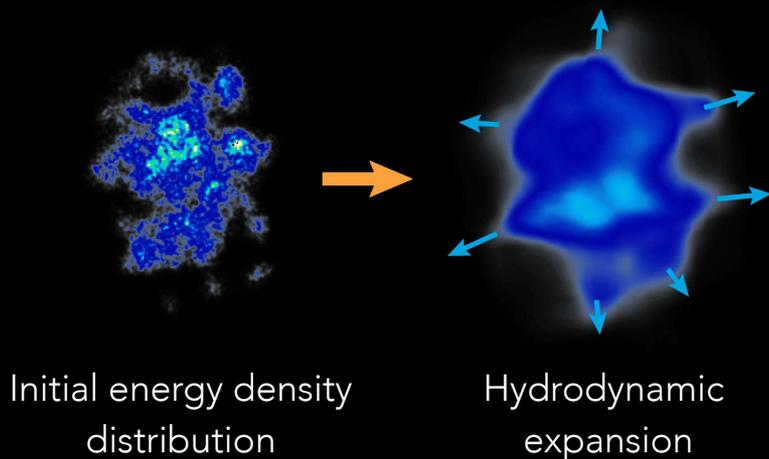


Gluons hitting the same domain in target get scatter in the same direction

Gelis, Lappi Venugopalan PRD 78 054020 (2008), PRD 79 094017 (2009); Dumitru, Gelis, McLerran, Venugopalan NPA810, 91 (2008); Dumitru, Jalilian-Marian PRD 81 094015 (2010); Dusling, Venugopalan PRD 87 (2013); A. Dumitru, A.V. Giannini, Nucl.Phys.A933 (2014) 212; V. Skokov, Phys.Rev.D91 (2015) 054014; T. Lappi, B. Schenke, S. Schlichting, R. Venugopalan, JHEP 1601 (2016) 061; Kovner, Skokov, Phys.Rev. D98 (2018) no.1, 014004

Origin of collectivity: final state correlations from hydro

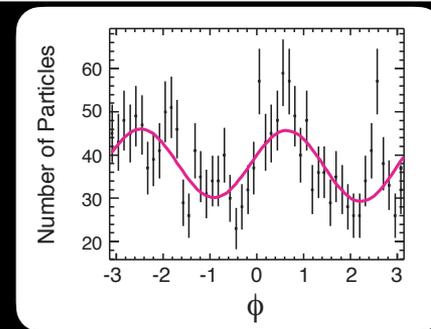
Azimuthal momentum anisotropy generated by medium response to the initial transverse geometry: Pressure gradients drive expansion



Fourier components of initial geometry



e.g.
 $\epsilon_2 \sim v_2$



Cartoon: B. Schenke

Collectivity across systems

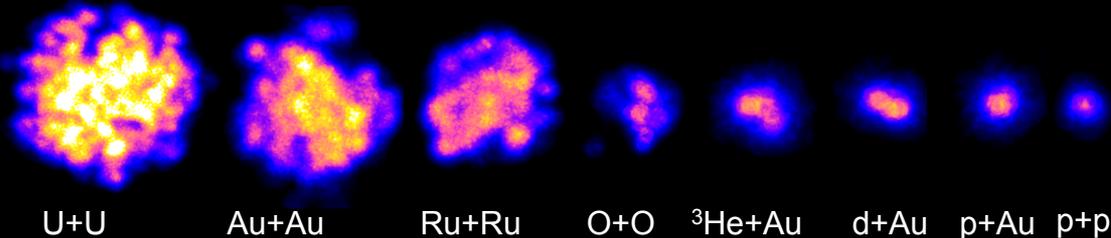
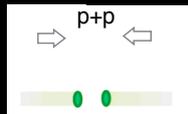
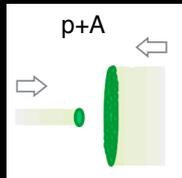
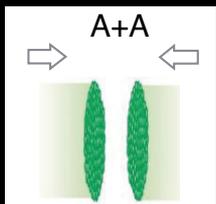
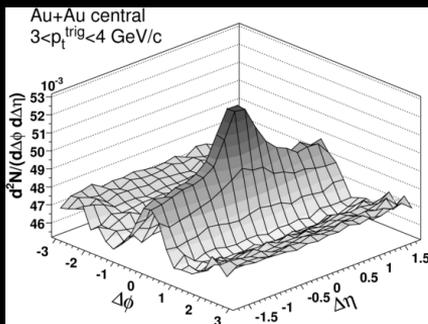
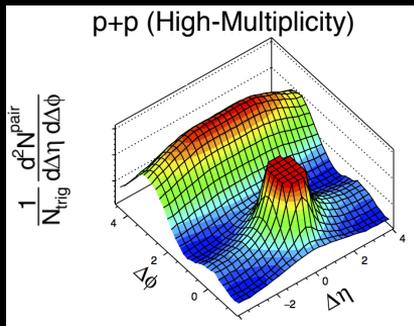


fig: Chun Shen QM19



STAR collaboration, Phys. Rev. Lett. 95, 152301
Phys. Rev. C 80 (2009) 64912



CMS collab., JHEP 1009:091,2010

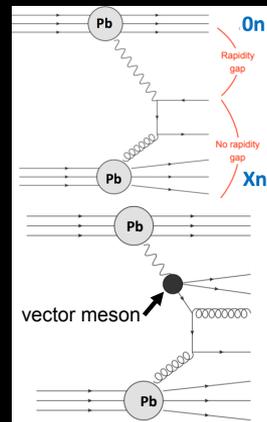
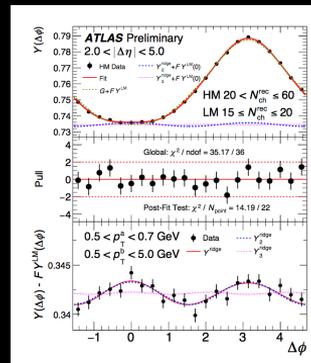
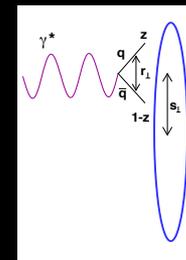


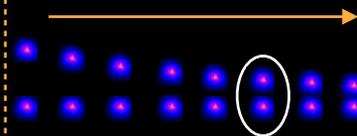
Photo-nuclear



ATLAS collab.,
Phys. Rev. C 104, 014903 (2021)



larger Q^2



dipole+A (EIC)

Will γ^*+A be the next small system?

What drives collectivity in small systems ?

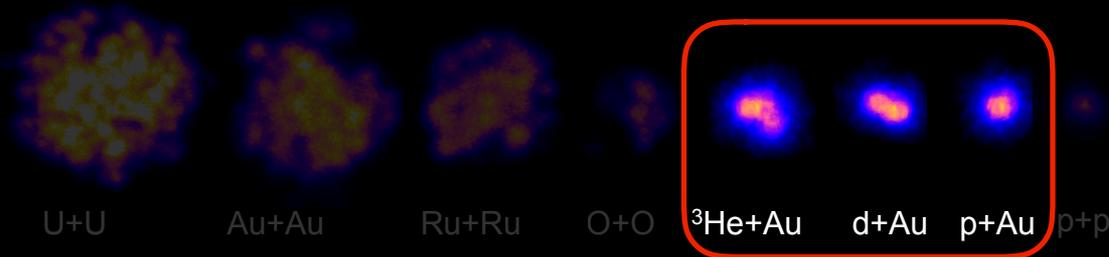
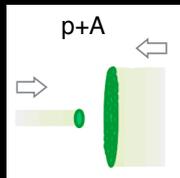
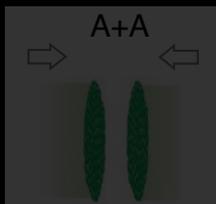
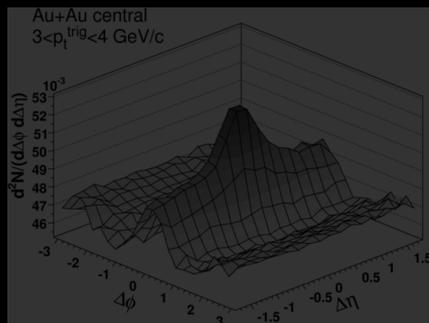
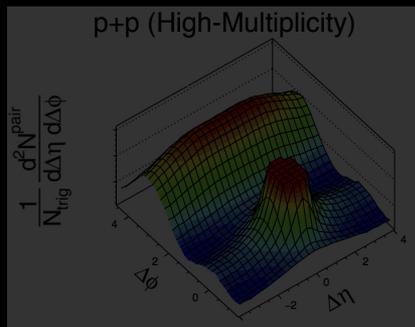


fig: Chun Shen QM19



STAR collaboration, Phys. Rev. Lett. 95, 152301
Phys. Rev. C 80 (2009) 64912



CMS collab.,

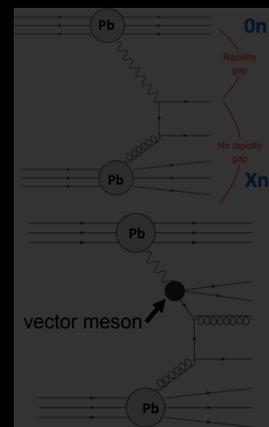
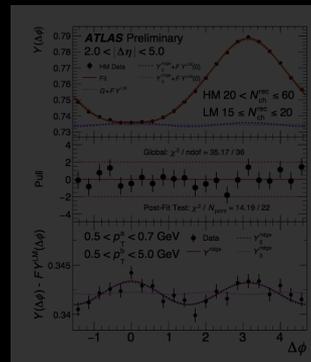
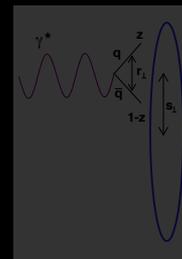


Photo-nuclear



ATLAS collab.,
Phys. Rev. C 104, 014903 (2021)



larger Q



dipole+A (EIC)

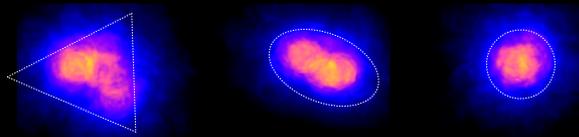
Will γ^*+A be the next small system ?

Pinning down the origin of collectivity with RHIC small system scan

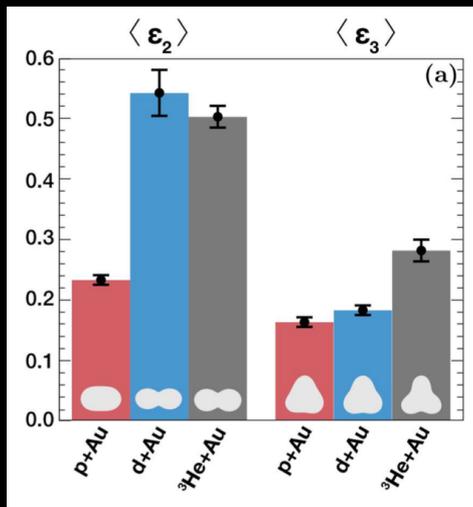
Event Engineering using different light ions

Shape engineering:

${}^3\text{He}+\text{Au} \rightarrow$ Triangular
 $d+\text{Au} \rightarrow$ Elliptical
 $p+\text{Au} \rightarrow$ Circular



PHENIX collab, Nature Physics 15, 214–220 (2019)



PHENIX collab., arXiv: 2107.06634v1
 Nagle et. al., Phys. Rev. Lett. 113, 112301

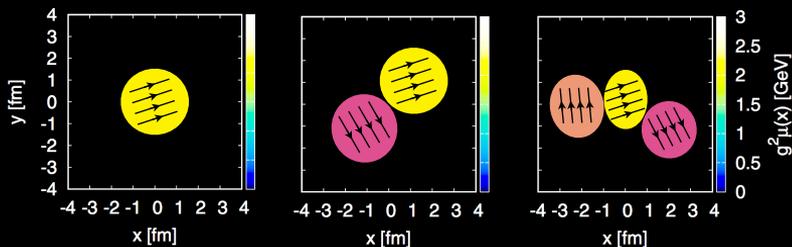
$\langle \epsilon_{2,3} \rangle$	Collision system	Nucl. w/o NBD Fluc.	Nucl. w/ NBD Fluc.	Quarks w/ NBD Fluc.	IP-G w/ Nucl.	IP-G w/ Quarks
$\langle \epsilon_2 \rangle$	$p+\text{Au}$	0.23	0.32	0.38	0.10	0.50
	$d+\text{Au}$	0.54	0.48	0.51	0.58	0.73
	${}^3\text{He}+\text{Au}$	0.50	0.50	0.52	0.55	0.64
$\langle \epsilon_3 \rangle$	$p+\text{Au}$	0.16	0.24	0.30	0.09	0.32
	$d+\text{Au}$	0.18	0.28	0.31	0.28	0.40
	${}^3\text{He}+\text{Au}$	0.28	0.32	0.35	0.34	0.46

A primary motivation of the RHIC small system scan

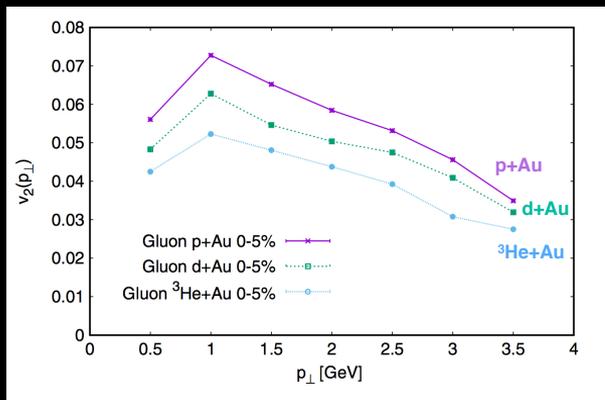
The ordering of v_3 is more decisive (v_2 ordering \rightarrow stronger final state effect)

What drives collectivity in small systems ?

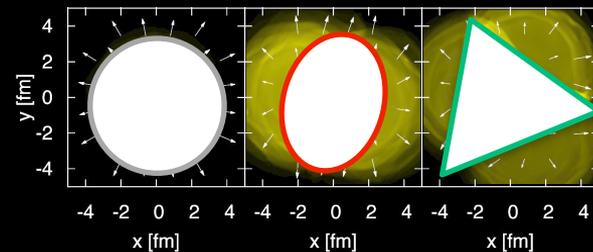
Color Glass Condensate (oversimplified)



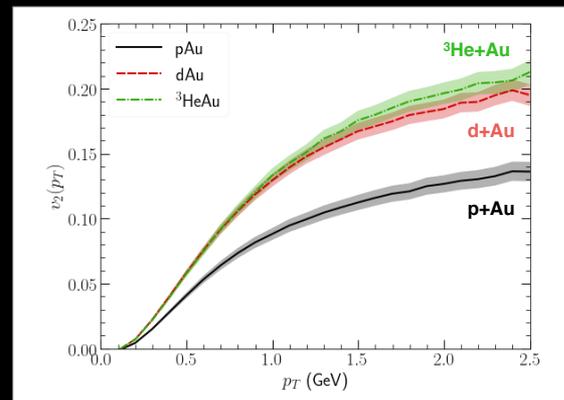
$$v_2(\text{p+Au}) > v_2(\text{d+Au}) > v_2(^3\text{He+Au})$$



Relativistic Hydrodynamics (oversimplified)



$$v_2(\text{p+Au}) < v_2(\text{d+Au}) \sim v_2(^3\text{He+Au})$$



Mace, Skokov, PT, Venugopalan, Phys. Rev. Lett. Erratum 123, 039901(E) (2019)

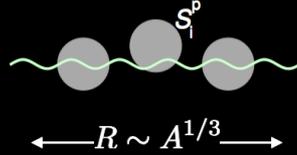
Schenke, Shen, PT, Phys. Rev. C 102, 044905 (2020)

Two possible mechanisms, qualitatively different predictions

The hybrid framework to study collectivity in small systems

Initial state model based on CGC: IP-Glasma

Kowalski, Teaney hep-ph/0304189v3

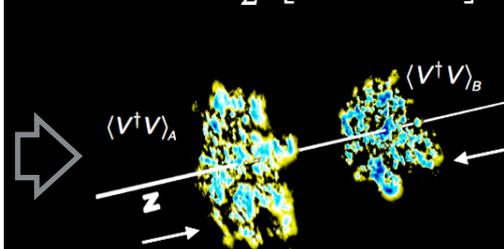
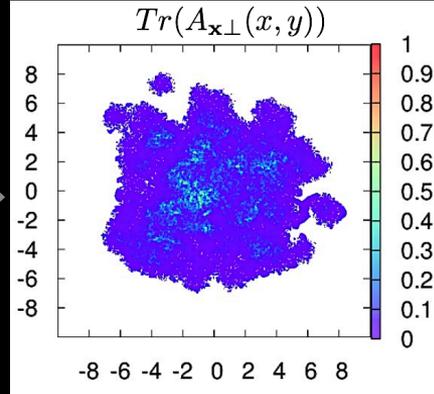
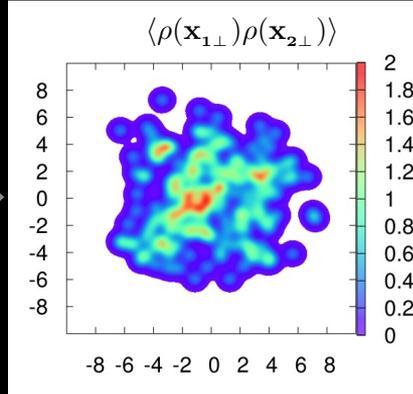
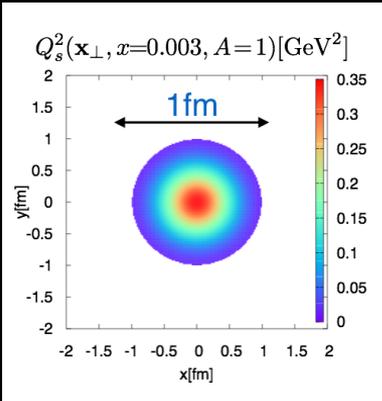


Schenke, PT, Venugopalan Phys. Rev. Lett. 108 (2012) 252301, Phys. Rev. C 86, 034908 (2012)

$$[D_\mu, F^{\mu\nu}] = J^\nu$$

$$A^i = A_{(A)}^i + A_{(B)}^i$$

$$A^\eta = \frac{ig}{2} [A_{(A)}^i, A_{(B)}^i]$$



A saturation model of proton

Build a saturation model of nucleus

Estimate the color fields inside nucleus

Compute & evolve the color fields after collisions

$$\text{Stress-Energy tensor: } T^{\mu\nu} = -g^{\mu\alpha} g^{\nu\beta} g^{\gamma\delta} F_{\alpha\gamma} F_{\beta\delta} + \frac{1}{4} g^{\mu\nu} g^{\alpha\gamma} g^{\beta\delta} F_{\alpha\beta} F_{\gamma\delta}$$

Hybrid framework combining CGC + Hydro

Schenke, Shen, PT, Phys. Rev. C 102, 044905 (2020)

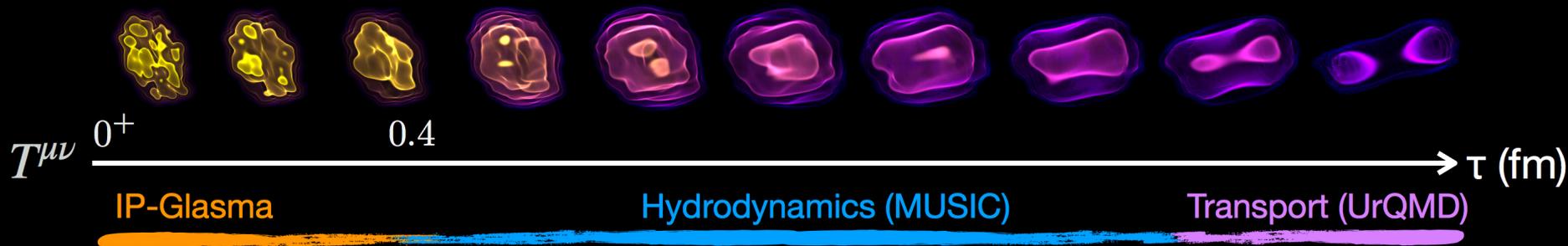


Fig: Chun Shen (different calculation)

$$T_{\text{CYM}}^{\mu\nu} = T_{\text{hydro}}^{\mu\nu} \longrightarrow u_{\mu} T_{\text{hydro}}^{\mu\nu} = e u^{\nu}$$

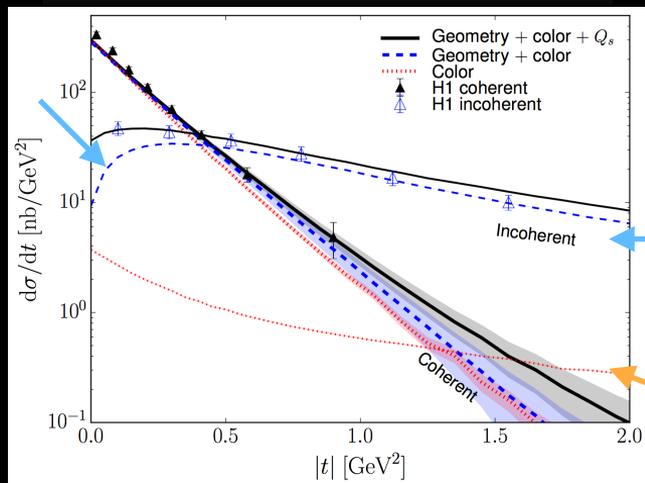
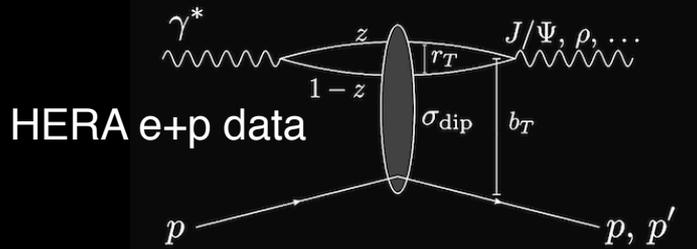
$$\pi^{\mu\nu} = T_{\text{CYM}}^{\mu\nu} - \frac{4}{3} e u^{\mu} u^{\nu} + \frac{e}{3} g^{\mu\nu}$$

$$\Pi = \frac{e}{3} - P(e)$$

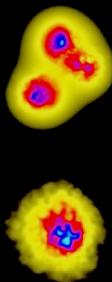
Smooth matching between CGC and Hydro
+ Landau Matching with lattice EoS

Cooper-Frye particlization

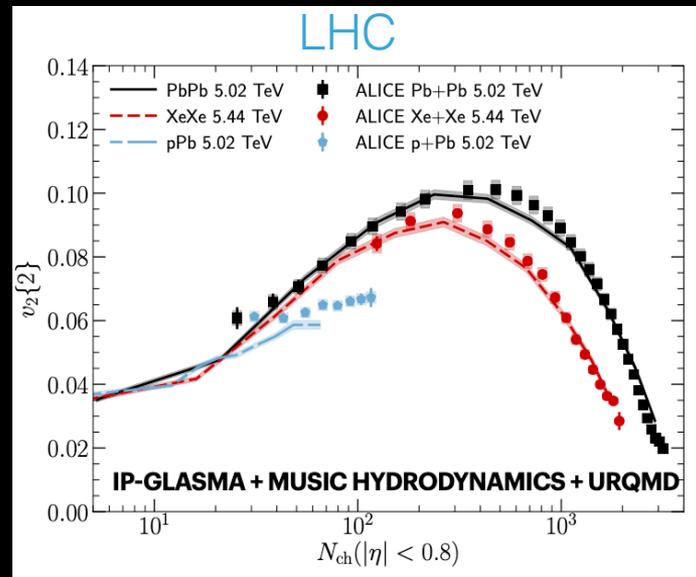
Independent constrains from Global data



Mantysaari, Schenke,
 Phys. Rev. Lett. 117,
 052301 (2016), Phys.Rev.
 D94 (2016) 034042

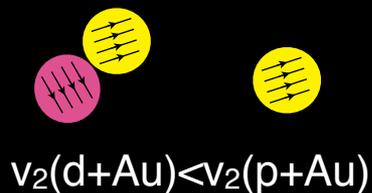


Before simulating hadronic collisions IP-Glasma is constrained by photon-induced collision data

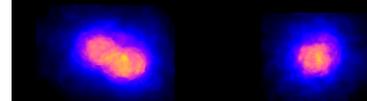
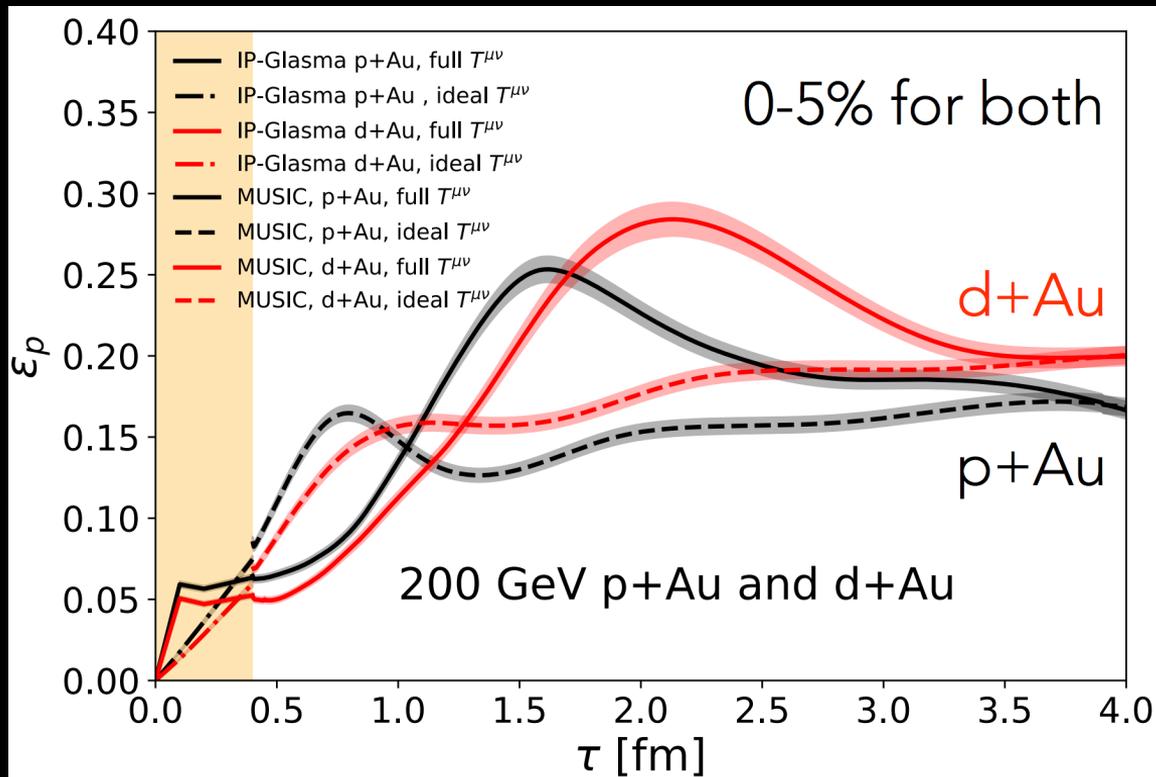


Using single set of parameters we fit bulk observables in different collision system

What drives collectivity in small systems ?



Early Time
(pre-equilibrium
CGC-dynamics
dominate)

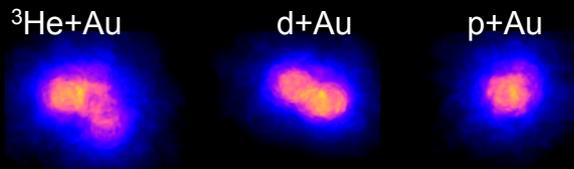


$v_2(d+Au) > v_2(p+Au)$

Late Time
(Final state/hydro
dominates)

Schenke, Shen, PT, Phys. Lett. B, 135322

What drives collectivity in small systems ?



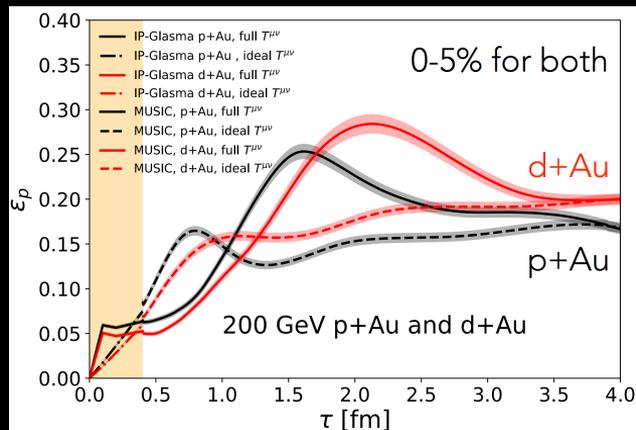
nature physics

Creation of quark-gluon plasma droplets with three distinct geometries

PHENIX Collaboration

Nature Physics 15, 214–220(2019) | Cite this article

12k Accesses | 76 Citations | 227 Altmetric | Metrics



$v_2(d+Au) < v_2(p+Au)$

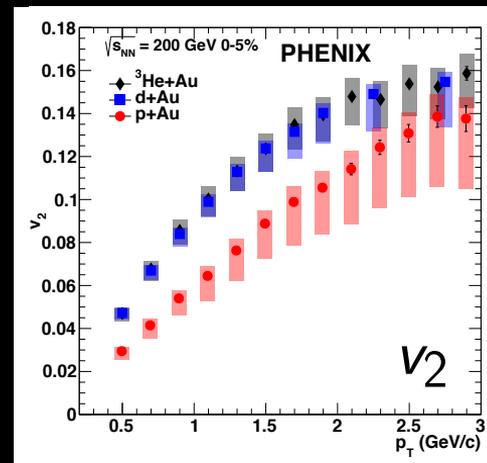
Early Time
(pre-equilibrium
CGC-dynamics dominate)

Schenke, Shen, PT, Phys. Lett. B, 135322

$v_2(d+Au) > v_2(p+Au)$

Late Time
(Hydrodynamics dominate)

$v_2(^3\text{He}+Au) \sim v_2(d+Au) > v_2(p+Au)$



PHENIX collab, Nature Physics 15, 214–220 (2019)

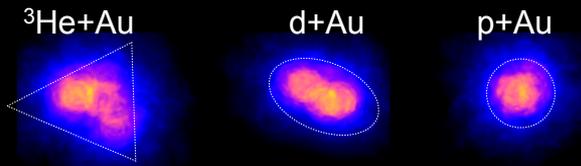
PHENIX results decisively establishes role of final state driving collectivity
our framework provides deeper insight on how it happens

Strong acceptance dependence and puzzle with triangular flow

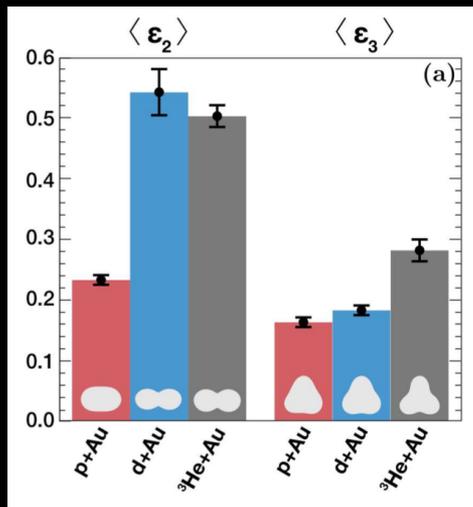
Puzzle with triangular flow in small systems

Shape engineering:

$^3\text{He}+\text{Au} \rightarrow$ Triangular
 $d+\text{Au} \rightarrow$ Elliptical
 $p+\text{Au} \rightarrow$ Circular



PHENIX collab, Nature Physics 15, 214–220 (2019)



PHENIX collab., arXiv: 2107.06634v1
 Nagle et. al., Phys. Rev. Lett. 113, 112301

$\langle \epsilon_{2,3} \rangle$	Collision system	Nucl.	Nucl.	Quarks	IP-G	IP-G
		w/o NBD Fluc.	w/ NBD Fluc.	w/ NBD Fluc.	w/ Nucl.	w/ Quarks
$\langle \epsilon_2 \rangle$	$p+\text{Au}$	0.23	0.32	0.38	0.10	0.50
	$d+\text{Au}$	0.54	0.48	0.51	0.58	0.73
	$^3\text{He}+\text{Au}$	0.50	0.50	0.52	0.55	0.64
$\langle \epsilon_3 \rangle$	$p+\text{Au}$	0.16	0.24	0.30	0.09	0.32
	$d+\text{Au}$	0.18	0.28	0.31	0.28	0.40
	$^3\text{He}+\text{Au}$	0.28	0.32	0.35	0.34	0.46

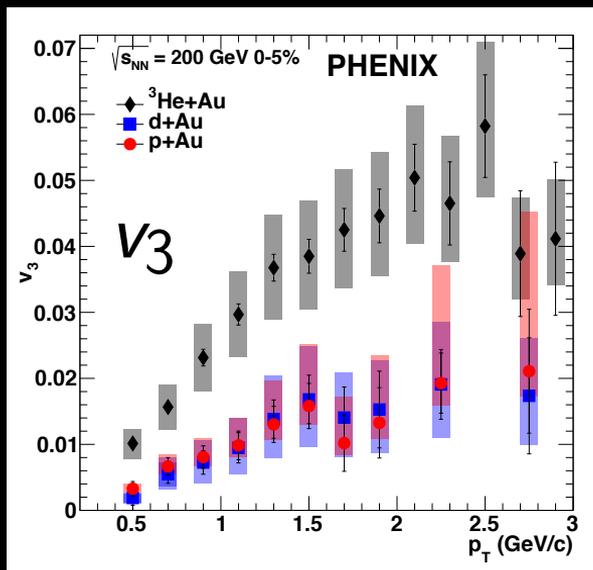
A primary motivation of the RHIC small system scan, confirmed by PHENIX data

The ordering of v_3 is more decisive (v_2 ordering \rightarrow stronger final state effect)

Puzzle with triangular flow in small systems

PHENIX collab, Nature Physics 15, 214–220 (2019)

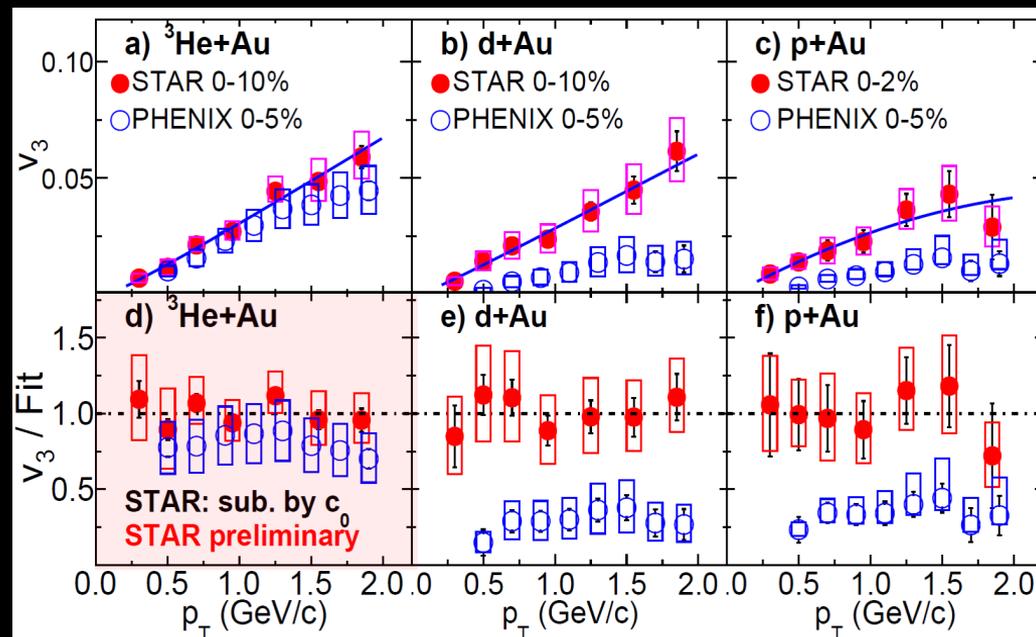
$$v_3(^3\text{He+Au}) > v_3(\text{d+Au}) \sim v_3(\text{p+Au})$$



PHENIX results are compatible with shape engineering

$$v_3(^3\text{He+Au}) \sim v_3(\text{d+Au}) \sim v_3(\text{p+Au})$$

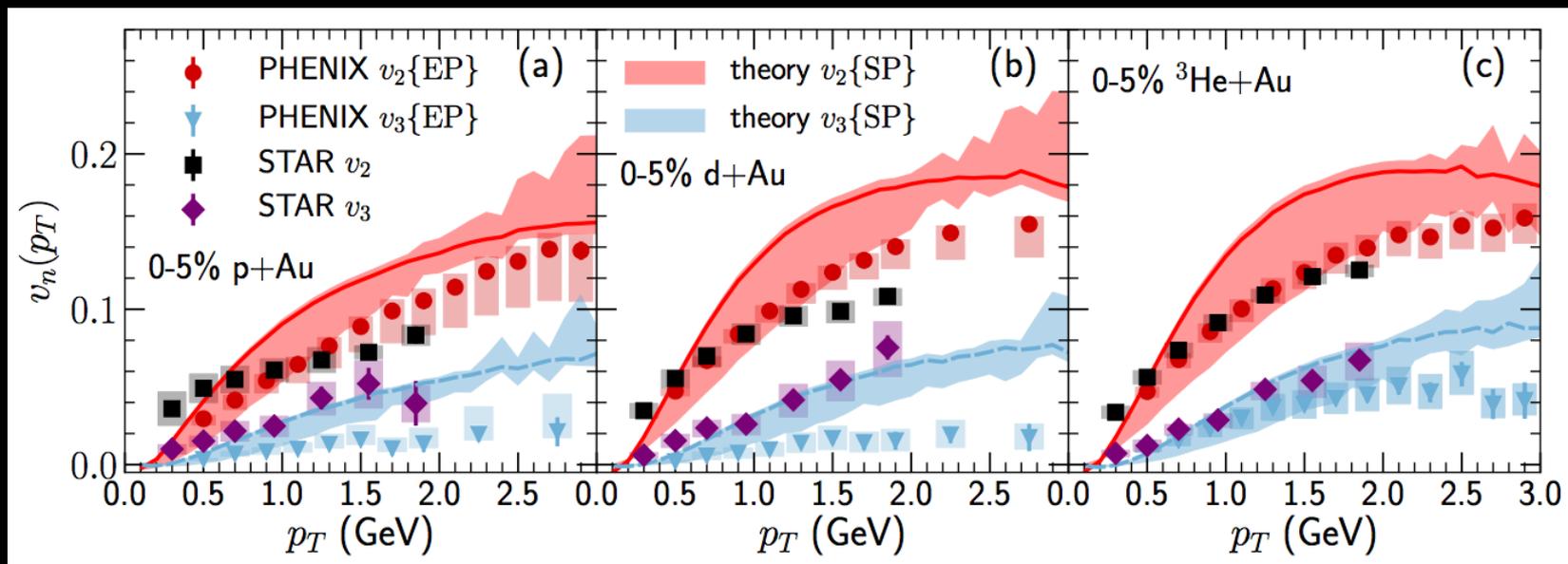
Shengli Huang, IS 2021



STAR mid-rapidity results seem to be not compatible with shape engineering expectations

Puzzle with triangular flow in small systems

B. Schenke, C. Shen, P. Tribedy, Phys.Lett.B 803 (2020) 135322; Data: C. Aidala et al. (PHENIX), Nature Phys. 15, 214 (2019), STAR Preliminary data: Roy Lacey (QM2019)



Hydrodynamic simulations: describes small system v_2 well but also do not show strong evidence of shape engineering in terms of v_3
(Our framework is boost invariant, data have strong acceptance dependence)

Strong acceptance dependence of (raw) harmonic coefficients

PHENIX (3x2PC,EP)
 $v_2(^3\text{He+Au}) \sim v_2(\text{d+Au}) > v_2(\text{p+Au})$ 😊
 $v_3(^3\text{He+Au}) > v_3(\text{d+Au}) \sim v_3(\text{p+Au})$ 😊

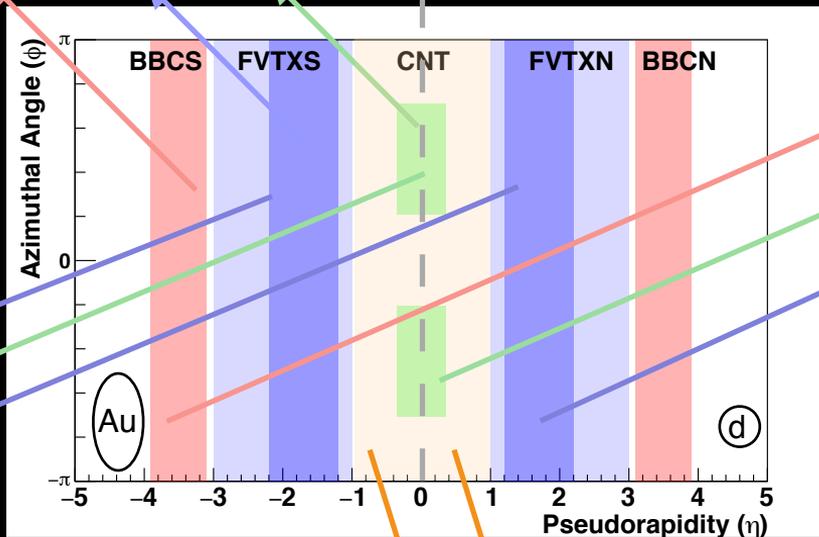
CGC+Hydro (Boost invariant)
 $v_2(^3\text{He+Au}) \sim v_2(\text{d+Au}) > v_2(\text{p+Au})$ 😊
 $v_3(^3\text{He+Au}) \sim v_3(\text{d+Au}) \sim v_3(\text{p+Au})$ 😞

Schenke, Shen, PT,
 Phys.Lett.B 803 (2020)
 135322

PHENIX collab, Nature Phys. 15, 214–220 (2019)

PHENIX (3x2PC)
 $v_2(\text{p+Au}) \geq v_2(\text{d+Au})$
 $\geq v_2(^3\text{He+Au})$ 😞
 $v_3(^3\text{He+Au}) > 0$
 $v_3(\text{d+Au}) = ?$
 $v_3(\text{p+Au}) = ?$ 😞

PHENIX collab., arXiv: 2107.06634v1,
 Nagle et. al, arXiv:2107.07287



PHENIX (3x2PC)
 $v_2(\text{p+Au}) \geq v_2(\text{d+Au})$
 $\geq v_2(^3\text{He+Au})$ 😞
 $v_3(^3\text{He+Au}) > 0$
 $v_3(\text{d+Au}) = ?$
 $v_3(\text{p+Au}) = ?$ 😞

PHENIX collab., arXiv: 2107.06634v1
 Nagle et. al, arXiv:2107.07287

STAR TPC (2PC)
 $v_2(^3\text{He+Au}) \sim v_2(\text{d+Au}) > v_2(\text{p+Au})$ 😊
 $v_3(^3\text{He+Au}) \sim v_3(\text{d+Au}) \sim v_3(\text{p+Au})$ 😞

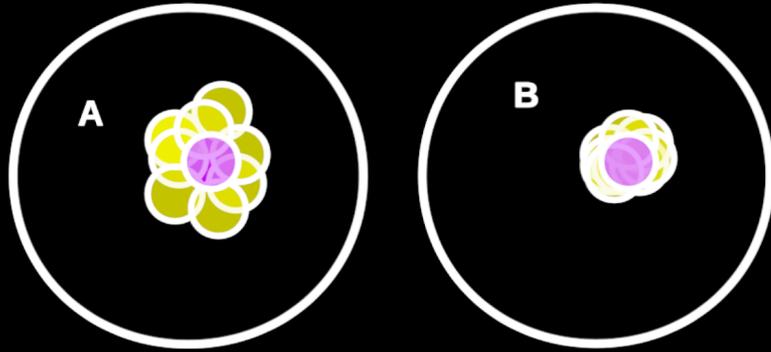
😊 Shape engineering works

😞 Doesn't work (or can't be checked)

Further attempts to distinguish initial & final state effects

If final state effects (hydro) dominates

G. Giacalone, B. Schenke and C. Shen, Phys. Rev. Lett. 125, 192301 (2020)



Event-by-event correlation between v_2 and $\langle p_T \rangle$

$$\hat{\rho}_2(v_2^2, \langle p_T \rangle) = \frac{\langle \hat{\delta}v_2^2 \hat{\delta}\langle p_T \rangle \rangle}{\sqrt{\langle (\hat{\delta}v_2^2)^2 \rangle \langle (\hat{\delta}\langle p_T \rangle)^2 \rangle}}$$

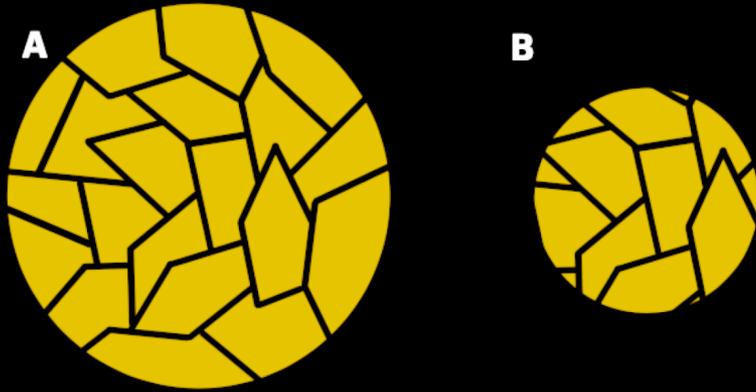
$R(A) > R(B) \rightarrow \langle p_T \rangle(A) < \langle p_T \rangle(B)$

$\varepsilon_2(A) > \varepsilon_2(B) \rightarrow v_2(A) > v_2(B)$

$\rightarrow v_2$ and $\langle p_T \rangle$ are anti-correlated

If initial state effects (hydro) dominates

G. Giacalone, B. Schenke and C. Shen, Phys. Rev. Lett. 125, 192301 (2020)



Event-by-event correlation between v_2 and $\langle p_T \rangle$

$$\hat{\rho}_2(v_2^2, \langle p_T \rangle) = \frac{\langle \hat{\delta}v_2^2 \hat{\delta}\langle p_T \rangle \rangle}{\sqrt{\langle (\hat{\delta}v_2^2)^2 \rangle \langle (\hat{\delta}\langle p_T \rangle)^2 \rangle}}$$

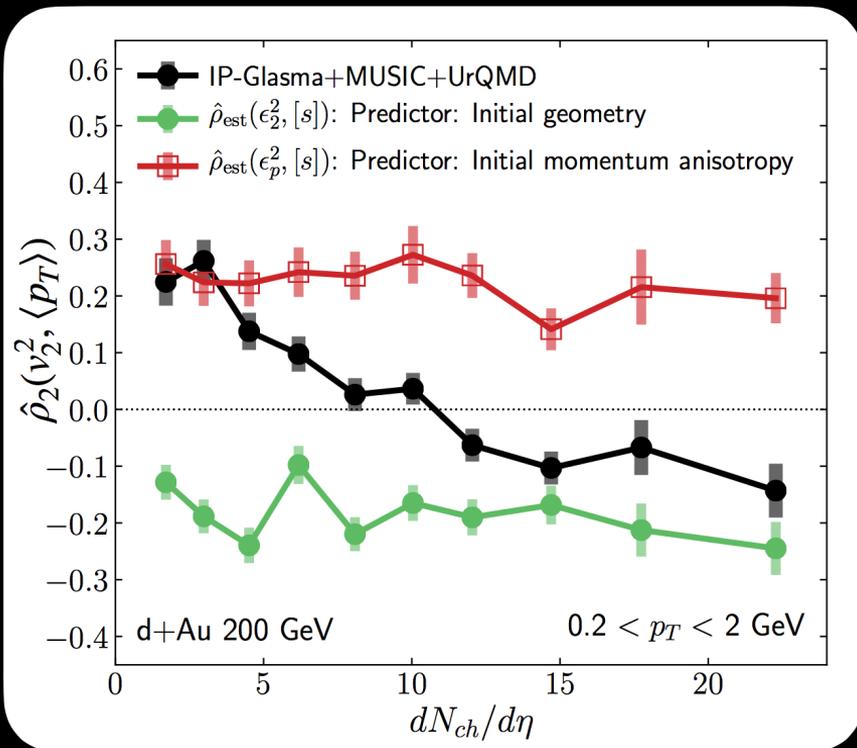
$R(A) > R(B)$ \rightarrow $\langle p_T \rangle(A) < \langle p_T \rangle(B)$

$\varepsilon_p(A) < \varepsilon_p(B)$ \rightarrow $v_2(A) < v_2(B)$

\rightarrow v_2 and $\langle p_T \rangle$ are **correlated**

Correlation between initial and final anisotropy

G. Giacalone, B. Schenke and C. Shen, Phys. Rev. Lett. 125, 192301 (2020)



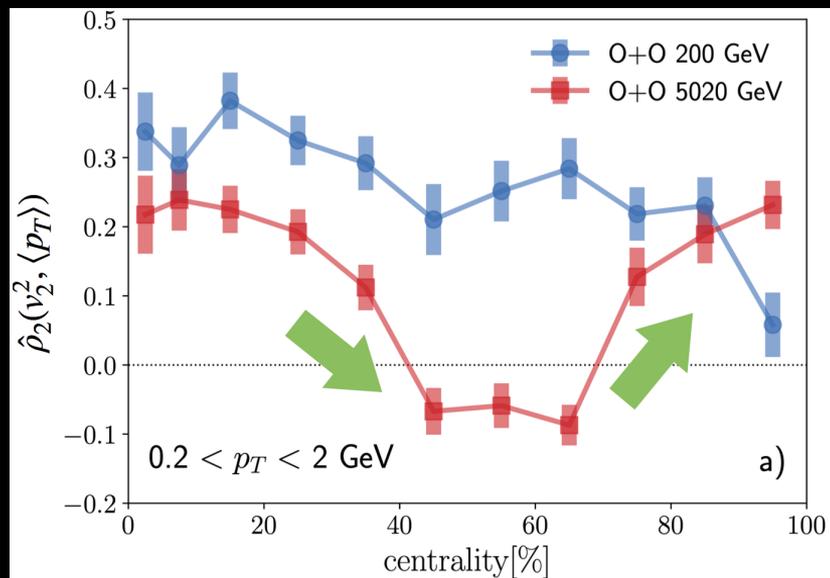
Event-by-event correlation between v_2 and $\langle p_T \rangle$

$$\hat{\rho}_2(v_2^2, \langle p_T \rangle) = \frac{\langle \hat{\delta}v_2^2 \hat{\delta}\langle p_T \rangle \rangle}{\sqrt{\langle (\hat{\delta}v_2^2)^2 \rangle \langle (\hat{\delta}\langle p_T \rangle)^2 \rangle}}$$

For $dN_{ch}/d\eta \approx 10$, switches from initial state correlation to final state correlation

Correlation between initial and final anisotropy

G. Giacalone, B. Schenke and C. Shen, Phys. Rev. Lett. 125, 192301 (2020), Lim, Nagle, Phys. Rev. C 103, 064906 (2021), Zhang et. al., arXiv:2103.01348



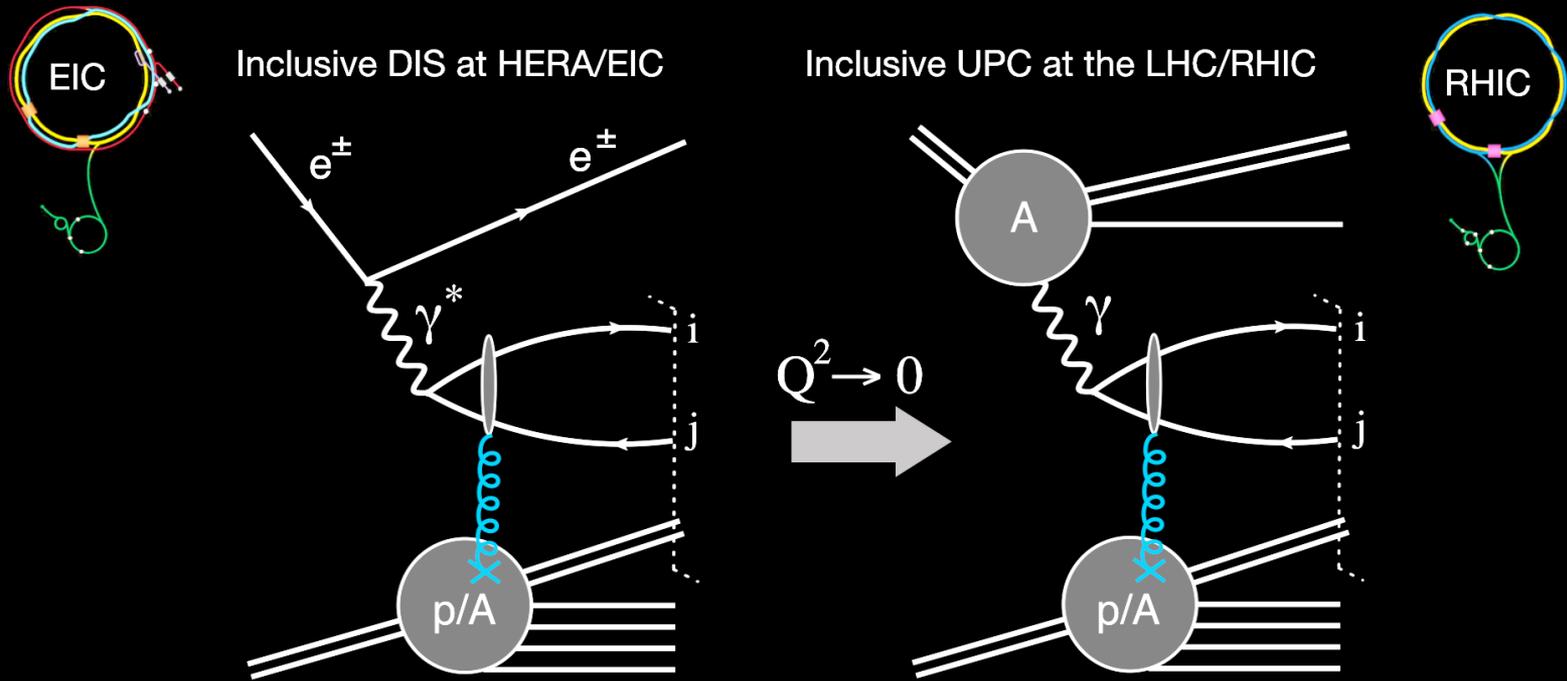
Double sign change @ LHC energy, No sign change @ RHIC energy

Opportunity: RHIC just took O+O data with wide acceptance STAR detector

Caution: This observable will be plagued by non-flow (conservation) effects

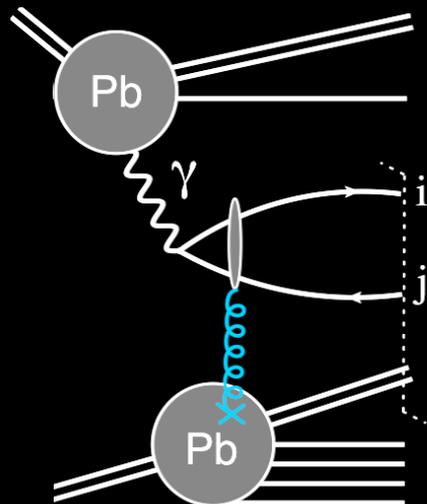
Most recent venture: Collectivity in Photon included collisions

Search for collectivity in photon induced collisions



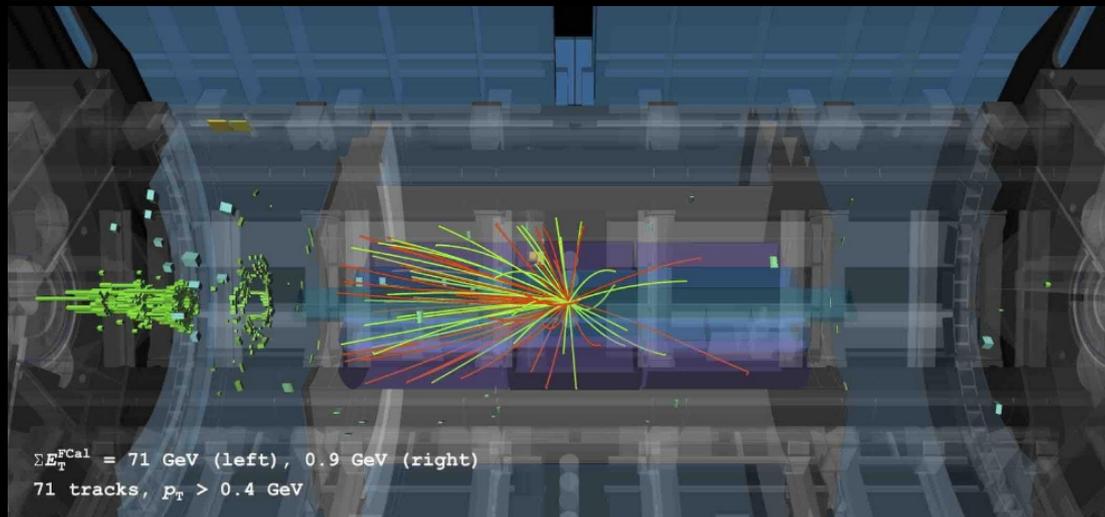
$e+p/A$ DIS ($Q^2 > 1 \text{ GeV}^2$), most events have $Q^2 \rightarrow 0$, called photoproduction processes
Until the EIC is built ultra-peripheral $p/A+A$ collisions \rightarrow opportunity to study photoproduction

Search for collectivity UPC collisions at the LHC



Pb+Pb, 5.02 TeV
 Run: 365681
 Event: 1064766274
 2018-11-11 22:00:07 CEST

ATLAS collect γ +Pb collisions by triggering on ultra-peripheral Pb+Pb



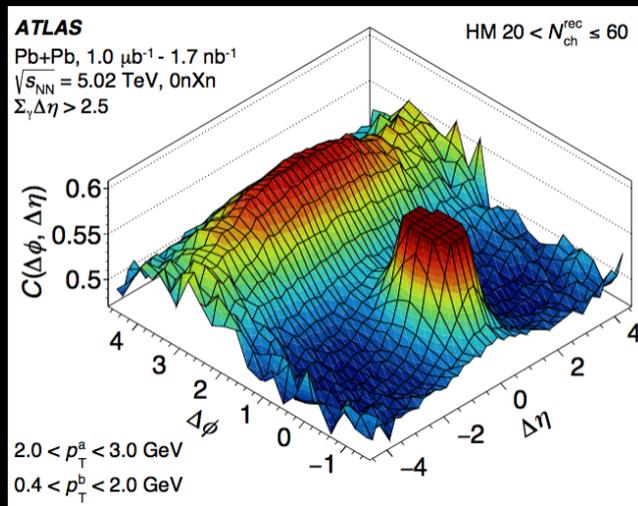
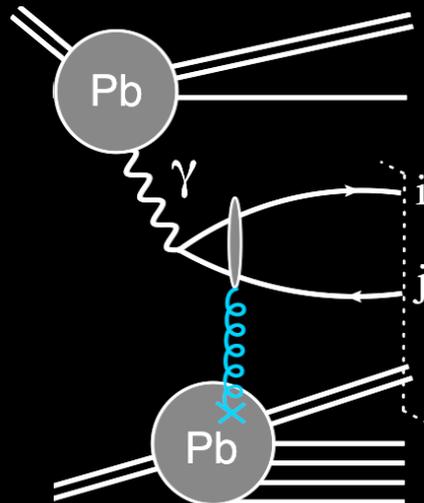
$$Q^2 \sim (\hbar c/R_A)^2 \rightarrow 0, \gamma^L(p, \text{LHC})=6.51e3,$$

$$E_\gamma(\text{LHC}) \sim \gamma^L (\hbar c/R_A) \sim 71 \text{ GeV}$$

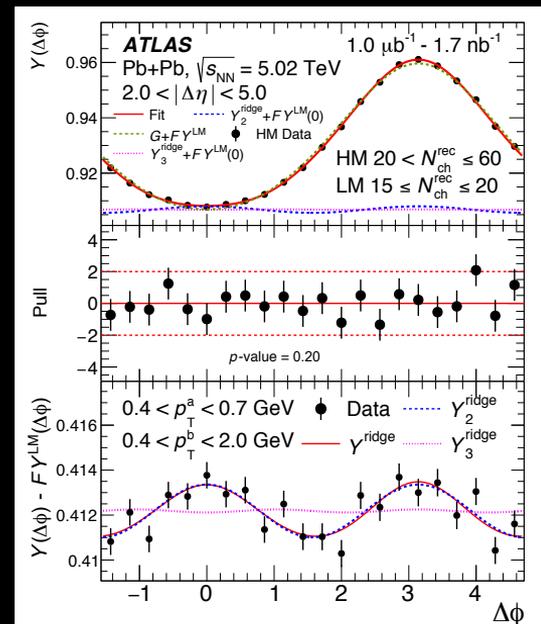
$$W_{\gamma\text{Pb}}(\text{LHC}) \sim 844 \text{ GeV, } dN_{\text{trk}}/d\eta(\text{HM}) > 10$$

ATLAS collaboration performed this pioneering measurements of collectivity in γ +Pb collisions

Search for collectivity UPC collisions at the LHC



ATLAS collab., Phys. Rev. C 104, 014903 (2021)



$$Y(\Delta\phi, 2 < |\Delta\eta| < 5) = \frac{1}{N_{\text{trig}}} \frac{d^2 N_{\text{pair}}}{d\Delta\phi} = \frac{N_{\text{asco}}}{2\pi} \left(1 + \sum_n 2a_n \cos(n\Delta\phi) \right)$$

$$Y(\Delta\phi)^{\text{template}}(HM) = F Y(\Delta\phi)(LM) + Y(\Delta\phi)^{\text{ridge}}(HM)$$

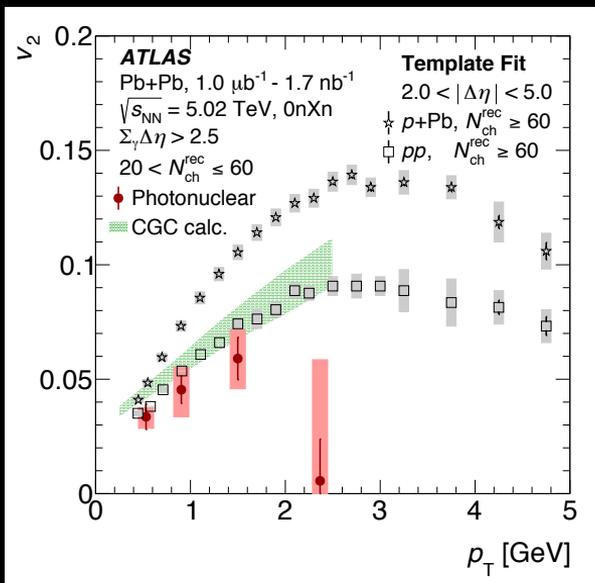
$$Y(\Delta\phi)^{\text{ridge}}(HM) = G \{ 1 + 2a_2 \cos(2\Delta\phi) + 2a_3 \cos(3\Delta\phi) + 2a_4 \cos(4\Delta\phi) \}$$

Template fitting of di-hadron correlations

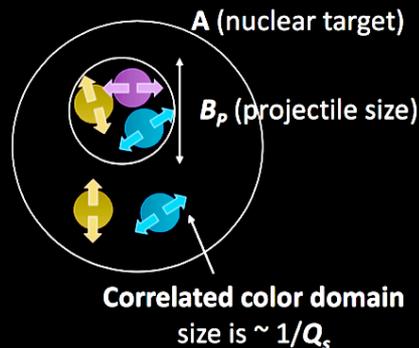
High activity γ +Pb events can accommodate a long-range ridge component (related to collectivity)

Search for collectivity UPC collisions at the LHC

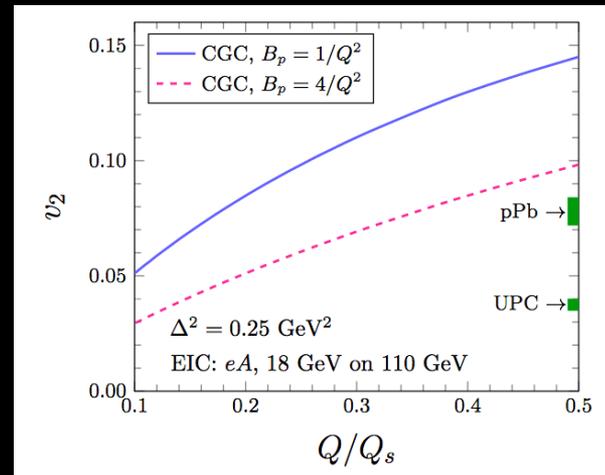
ATLAS collab., Phys. Rev. C 104, 014903 (2021)



Cartoon: Blair Seidlitz, IS2021



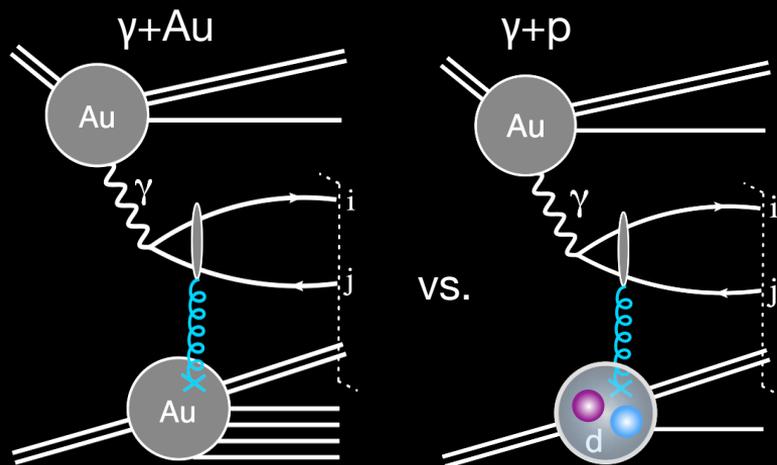
Shi et. al., Phys. Rev. D 103, 054017 (2021)



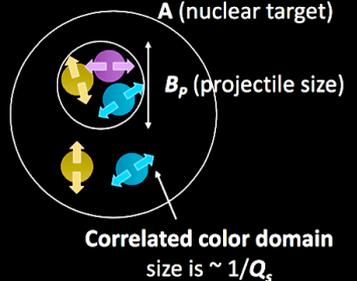
Elliptic anisotropy is lower in $\gamma+\text{Pb}$ than in $p+\text{Pb}$

CGC calculations provide an explanation based on color domain picture.

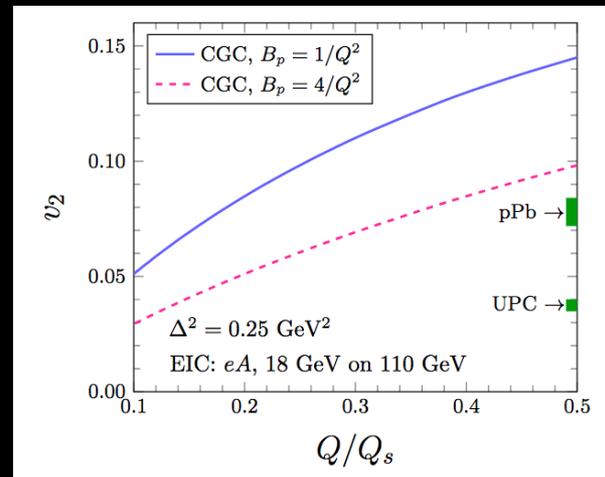
What can we do at RHIC Au+Au(γ) vs d+Au(γ)



Cartoon: Blair Seidlitz, IS2021



Shi et. al., Phys. Rev. D 103, 054017 (2021)



$$Q_{S,A}^2 = Q_{S,p}^2 \times A^{1/3}$$

$$v_2^{\gamma+Au} \propto \frac{Q}{Q_{S,A}} = \frac{Q}{Q_{S,p} \times A^{1/6}} \approx \frac{v_2^{\gamma+p}}{A^{1/6}}$$

$$\left. \frac{v_2^{\gamma+p}}{v_2^{\gamma+Au}} \right|_{Q^2=\text{fixed}} \propto A^{1/6} > 1$$

If the domain picture holds we should be able to see this ordering by triggering photonuclear processes in ultra-peripheral Au+Au and p/d+Au at RHIC 200 GeV collisions

At EIC we can test this with much better control

Summary

Collectivity in small systems:

RHIC small system collision has been very successful

Hybrid framework combining CGC + Hydro can provide many insights

Challenges to understand acceptance dependence and non-flow

New observables are under investigation and scrutiny

UPC can be a doorway to study collectivity at the future EIC

Many exciting new possibilities

1. RHIC took data this year on O+O, possible O+O run at the LHC
2. RHIC just took d+Au data with the STAR detector (wide acceptance measurements)
3. Anticipated Au+Au 200 GeV run of RHIC (2023, 2025) sPHENIX & STAR with forward upgrade

Thanks
