Holographic QCD in the NICER era





A Virtual Tribute to Quark Confinement and the Hadron Spectrum 2021 August 5, 2021

Equilibrium

• equation of state of dense nuclear and quark matter

- Applications to neutron stars
- Out-of-equilibrium
 - transport properties of cool quark matter

1. Equilibrium

A holographic model for QCD in the Veneziano limit (large N_f , N_c with $x = N_f/N_c$ fixed): V-QCD

[Järvinen-Kiritsis 1112.1261]

[...many extensions...]

- Bottom-up, try follow string theory as closely as possible
- Many parameters: effective description of QCD
- Comparison with QCD data essential
- Works surprisingly well!

Constraining the model at $\mu \approx 0$

- Many parameters already fixed by requiring qualitative agreement with QCD
- Good description of lattice data nontrivial result!

Interaction measure,

2+1 flavors

Lattice data: Borsanyi et al. arXiv:1309.5258

Baryon number susceptibility

Lattice data: Borsanyi et al. arXiv:1112.4416



Phase diagram at zero quark mass

- Extrapolate to finite μ
- Intermediate- μ , low-T instanton solution appears: baryons



Hybrid Equations of State

- V-QCD nuclear matter description not reliable at low densities
- \Rightarrow use traditional models (effective field theory) instead
 - Match nuclear models (low densities) with V-QCD (high densities)
 - Variations in model parameters give rise to the band
 - Same (holographic) model for nuclear and quark matter phases!



Speed of sound and comparison to FRG

Speed of sound (squared) as a function of density



- Relatively mild dependence on model parameters
- Similar predictions as with FRG method!



2. Applications to neutron stars

Predictions for neutron stars

Plug EoSs in the TOV equations \Rightarrow Mass-Radius relations

- without holography
- with holography (hybrid EoSs)

[[]NJ-Järvinen-Nijs-Remes 2006.01141]



- Strong 1st order nuclear to quark matter phase transitions: quark cores unstable
- Large radii of neutron stars preferred

NICER predictions for neutron stars



[NJ-Järvinen-Remes to appear]

- Red curves V-QCD(APR); submitted in CompOSE
- w/ NICER results compatible with no quark matter cores
- $R(2M_{\odot}) > 12.2$ km results in very constrained bands

 \Rightarrow predictions for QCD

NICER predictions for neutron stars



[NJ-Järvinen-Remes to appear]

- Predictions for GW peak etc. frequencies
- Generated using "universal" relations [Takami-Rezzolla-Baiotti 1403.5672,1412.3240; Breschi et al. 1908.11418]
- Red curves V-QCD(APR)

3. Out-of-equilibrium

Transport of cool quark matter

Beyond the EoS: transport properties

- (Bulk) viscosity relevant for neutron star merger dynamics?
- Viscosities \leftrightarrow instabilities (*r*-modes) in spinning NSs
- Conductivities relevant for NS cooling and equilibration after NS merger

[Review: Schmitt-Shternin 1711.06520]

However transport is challenging to analyze...

- While the EoS of dense and cold QCD matter has large uncertainties, even less is known about transport
- Only available first-principles result for quark matter: leading order pQCD analysis in the unpaired phase

[Heiselberg-Pethick PRD 48(1993)2916]

- We carried out the strong coupling analysis (also at $\omega
 eq 0$)
 - to-be-submitted in CompOSE

 $[{\sf Hoyos-NJ-J\"arvinen-Subils-Tarrio-Vuorinen\ 2005.14205+to\ appear}]$

Transport of cool quark matter



- Predictions for viscosities for unpaired quark matter (dashed $\mu = 450$ MeV, solid $\mu = 600$ MeV)
- Large deviation from perturbative results
- Notice that our (small) results assume "idealized" case: only QCD contributions, no weak interactions or electrons
- \bullet Also computed electrical σ and heat κ conductivities

Conclusions and outlook

- Gauge/gravity duality (combined with other approaches) is useful to study dense QCD
- Using V-QCD with simple approximations, many details work really well:
 - $\checkmark\,$ Precise fit of lattice thermodynamics at $\mu\approx$ 0
 - ✓ Extrapolated EoS for cold quark matter reasonable
 - \checkmark Simultaneous model for nuclear and quark matter
 - ✓ Stiff EoS for nuclear matter
- Predictions for
 - equation of state of cold matter
 - transport in quark matter phase
 - properties of neutron stars
 - gravitational wave spectrum in neutron star mergers

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Backup slides

No quark matter cores?!

A recent model independent study claims that most massive neutron stars have quark matter cores

> [Annala-Gorda-Kurkela-Nättilä-Vuorinen 1903.09121(Nature Phys.)]



- They find that purely hadronic stars require very high speeds of sound in nuclear matter, $c_s^2\gtrsim 0.7$
- Seems to contradict our results, what's going on?

(Simplified) answer: our model predicts lower adiabatic index $\gamma = d \log p/d \log \epsilon$ for nuclear matter than what they expect



Transport from gauge/gravity duality

Transport: deviation from equilibrium \leftrightarrow fluctuations of the 5D metric

Leading order deviation characterized in terms of transport coefficients:

- Shear viscosity η "standard" viscosity
- Bulk viscosity ζ viscosity in compression/expansion
- Electric conductivity σ defined by $\vec{J} = \sigma \vec{E}$
- Thermal conductivity κ defined by $\vec{Q} = -\kappa \nabla T$

Coefficients can be computed from correlators via using Kubo formulae + standard dictionary

• E.g.

$$\eta = -\frac{1}{\omega} \operatorname{Im} \left\langle T_{xy}(\omega, \vec{k_1}) T_{xy}(\omega, \vec{k_2}) \right\rangle \Big|_{\substack{\omega \to 0, k_i \to 0}}$$
• Famous result: $\eta = \frac{s}{4\pi}$ ("universal", holds also in our models)