

[arXiv:2004.09440]

# Direct CP violation and the ∆I=1/2 rule in K→ππ decay from the Standard Model

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### Motivation

- Likely explanation for matter/antimatter asymmetry in Universe, baryogenesis, requires violation of CP.
- Amount of CPV in Standard Model appears too low to describe measured M/AM asymmetry: tantalizing hint of new physics.
- Direct CPV first observed in late 90s at CERN (NA31/NA48) and Fermilab (KTeV) in  $K^0 \rightarrow \pi\pi$ :

$$\eta_{00} = \frac{A(K_{\rm L} \to \pi^0 \pi^0)}{A(K_{\rm S} \to \pi^0 \pi^0)}, \qquad \eta_{+-} = \frac{A(K_{\rm L} \to \pi^+ \pi^-)}{A(K_{\rm S} \to \pi^+ \pi^-)}.$$

$$\operatorname{Re}(\epsilon'/\epsilon) \approx \frac{1}{6} \left( 1 - \left| \frac{\eta_{00}}{\eta_{\pm}} \right|^2 \right) = 16.6(2.3) \times 10^{-4} \quad \text{(experiment)}$$

measure of direct CPV

measure of indirect CPV

- Small size of ε' makes it particularly sensitive to new direct-CPV introduced by many BSM models.
- Looking for deviations from experiment may help shed light on origin of M/AM asymmetry.

• A Standard Model prediction of  $\epsilon$ ' also provides a new horizontal band constraint on CKM matrix in  $\rho$ - $\eta$  plane:



new constraint from this work!

- While underlying weak process occurs at high energies  $\sim M_w$ =80 GeV, K  $\rightarrow \pi\pi$  decays receive large corrections from low-energy hadronic physics O( $\Lambda_{_{QCD}}$ )~250 MeV.
- Lattice QCD is the only known *ab initio*, **systematically improvable** technique for studying non-perturbative QCD.



Hadronic energy scale << M<sub>w</sub> – use weak effective theory (3 flavors)



## Anatomy of a lattice calculation

- Lattice QCD uses Monte Carlo techniques to sample the discretized (Euclidean) Feynman path integral directly, generating an ensemble of N "gauge configurations".
- Expectation value of some Green's function computed over the ensemble converges to path integral value in large N limit.
- Green's function composed of *operators* created from quark fields that create/destroy states of interest.
- Operators create all states with same quantum numbers, eg  $\bar{u}\gamma^5 d$  creates pions and all excited pion-like states.
- Contributions of each state i decay exponentially in time as exp(-E<sub>i</sub>t) due to Euclidean time.
- Extract contributions of lightest states by fitting large time dependence.
- <u>Challenges:</u>
  - Computationally expensive, requiring months to years of running on the world's fastest supercomputers.
  - Much like experiment, have both statistical and systematic errors.
  - Systematic errors (e.g. from discretization or from fitting) require careful analysis and treatment.

### Lattice QCD for $K \rightarrow \pi \pi$



- Extract matrix elements by fitting time dependence in limit of large ( $t_{snk}$ -t), ( $t_{src}$ -t) at which lower-energy states dominate.
- Series is necessarily truncated for fit: Systematic errors arise if excited state effects not properly taken into account.

## I=2 calculation

- A<sub>2</sub> can be measured very precisely using "standard" lattice techniques.
- Most recent result (2015):
  - Computed with large, ~  $(5.5 \text{ fm})^3$  volumes
  - Physical quark masses
  - Two lattice spacings (2.36 GeV and 1.73 GeV) → Continuum limit taken.
- <1% statistical error!
- 10% and 12% total errors on  $Re(A_2)$  and  $Im(A_2)$  resp.
- Dominant sys. errors due to truncation of PT series in computation of renormalization and Wilson coefficients.

### Δ*I*=1/2 rule

• In experiment kaons ~450x (!) more likely to decay into I=0 pi-pi states than I=2.

$$\frac{\text{Re}A_0}{\text{Re}A_2} = 22.45(6)$$
 (the  $\Delta$ I=1/2 rule)

- Perturbative running to charm scale accounts for about a factor of 2. Where does the remaining 10x come from? New Physics?
- The answer is low-energy QCD!

[arXiv:1212.1474, arXiv:1502.00263]

Strong cancellation between the two dominant contractions not predicted by naive factorization:



## I=0 Calculation

- $A_0$  is more difficult than  $A_2$ , primarily because I=0  $\pi\pi$  state has vacuum quantum numbers.
- "Disconnected diagrams" dominate statistical noise



"type4"

#### 2015 calculation

Single  $\pi\pi$  operator:

[Phys.Rev.Lett. 115 (2015) 21, 212001]

- Physical quark masses on single, coarse lattice (a<sup>-1</sup>= 1.38 GeV) but with large (4.6 fm)<sup>3</sup> physical volume to control FV errors.
- G-parity boundary conditions remove dominant unphysical contribution from stationary  $\pi\pi$  state.



- 21% and 65% stat errors on  $Re(A_0)$  and  $Im(A_0)$  due to disconn. diagrams and, for  $Im(A_0)$  a strong cancellation between  $Q_4$  and  $Q_6$ .
- Dominant, 15% systematic error due again to PT truncation errors.

### **2015 calculation:** ε'

- $\operatorname{Re}(A_0)$  and  $\operatorname{Re}(A_2)$  from expt.
- Lattice values for  $Im(A_0)$ ,  $Im(A_2)$  and the phase shifts,

$$\operatorname{Re}\left(\frac{\varepsilon'}{\varepsilon}\right) = \operatorname{Re}\left\{\frac{i\omega e^{i(\delta_{2}-\delta_{0})}}{\sqrt{2}\varepsilon} \begin{bmatrix} \operatorname{Im}A_{2} \\ \operatorname{Re}A_{2} \end{bmatrix} \right\}$$
$$= 1.38(5.15)(4.43) \times 10^{-4}, \quad \text{(our result)}$$
$$16.6(2.3) \times 10^{-4} \quad \text{(experiment)}$$

- Result is  $2.1\sigma$  below experimental value.
- Total error on  $\text{Re}(\epsilon'/\epsilon)$  is ~3x the experimental error
- "This is now a quantity accessible to lattice QCD"!
- Focus since has been to improve statistics and reduce / improve understanding of systematic errors.

#### The " $\pi\pi$ puzzle"

- Essential to understand  $\pi\pi$  system:
  - Energy needed to extract ground-state matrix element
  - Energy also needed to compute phase-shift (Luscher)
  - Derivative of phase-shift w.r.t. energy is required for Lellouch-Luscher finitevolume correction (F)
- 2015 calculation phase shift  $\delta_0(E_{\pi\pi} \approx m_K) = 23.8(5.0)^\circ$ substantially smaller than prediction obtained by combining dispersion theory with experimental input,  $36^\circ$ .
- Result was very stable under varying fit range and also with 2state fits.
- Increasing statistics by almost 7x did not resolve (  $\delta_0 = 19.1(2.5)^\circ$  )
- Nevertheless, most likely explanation is excited-state contamination hidden by rapid reduction in signal/noise.



#### **Resolving the** $\pi\pi$ puzzle [arXiv:2103.15131]

• To better resolve the ground-state we have introduced 2 more  $\pi\pi$  operators:



• Obtain parameters by simultaneous fitting to matrix of correlation functions, eg for pipi 2pt Green's function:

$$C_{ij}(t) = \langle 0 | O_i^{\dagger}(t) O_j(0) | 0 \rangle = C + \sum_{\alpha} A_{i,\alpha} A_{j,\alpha} e^{-E_{\alpha}t}$$
  
round-the-world single pion propagation small compared to errors - drop

- A far more powerful technique than just increasing statistics alone.
- 741 configurations measured with 3 operators.

#### Effect of multiple operators on $\pi\pi$



Result compatible with dispersive value:  $\delta_0(479.5 \text{ MeV}) = 32.3(1.0)(1.4)^\circ$ 

[For more details, cf talk by Tianle Wang, Lattice 2021]

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### **Effect of multiple operators on K** $\rightarrow \pi\pi$

 Convenient to visualize data by taking "optimal" linear combination of the two most important operators that best projects onto ground-state.

$$\mathcal{O}_{\text{opt}} = r_1 \mathcal{O}_{\pi\pi(111)} + r_2 \mathcal{O}_{\sigma}$$

$$r_1 = 5.24(18) \times 10^{-7} \text{ using } \pi\pi$$

$$r_2 = -2.86(17) \times 10^{-4} \text{ fits}$$

strong, clear plateau + improved precision

2

4

6

t'

8

10

8

0

2

4

6

ť

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12

10

#### [arXiv:2004.09440]

### K→ππ fit results

Examine many fit ranges, #states and #operators



Adopt uniform fit t'<sub>min</sub>=5 which is stable for all Q<sub>i</sub>

"bump" appears to be statistical

 Evidence that excited state error was significantly underestimated in 2015 work

## Systematic error budget

- Primary systematic errors of 2015 work:
  - Finite lattice spacing: 12%
  - Wilson coefficients: 12%
  - Renormalization (mostly PT matching): 15%
  - Excited-state:  $\leq$  5% but now known to be significantly underestimated
  - Lellouch-Luscher factor (derivative of  $\pi\pi$  phase shift wrt. energy): 11%
- In our new work we have used step-scaling to raise the renormalization scale from  $1.53 \rightarrow 4.00 \text{ GeV}$ :  $15\% \rightarrow 5\%$
- 3 operators have dramatically improved understanding of  $\pi\pi$  system: Lellouch-Luscher factor  $11\% \rightarrow 1.5\%$
- Detailed analysis shows no evidence of remaining excited-state contamination: Excited state error now negligible!
- Still single lattice spacing: Discretization error unchanged.
- Evidence that Wilson coefficient systematics are driven by using PT for 3-4f matching, not improved by higher μ: Wilson coeff error unchanged.

## Isospin breaking + EM effects

- Our simulation does not include effects of isospin breaking or EM effects.
- While these effects are typically small O(1%), heavy suppression of A<sub>2</sub> (ΔI=1/2 rule) means relative effect on A<sub>2</sub> and ε' could be O(20%).
- Current best determination of effect uses NLO  $\chi$ PT and  $1/N_c$  expansion predicts 23% correction to our result:

Include as separate systematic error.

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### **Final result for** ε'

Combining our new result for Im(A<sub>0</sub>) and our 2015 result for Im(A<sub>2</sub>), and again using expt. for the real parts, we find

$$\operatorname{Re}\left(\frac{\varepsilon'}{\varepsilon}\right) = \operatorname{Re}\left\{\frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\varepsilon} \left[\frac{\operatorname{Im}A_2}{\operatorname{Re}A_2} - \frac{\operatorname{Im}A_0}{\operatorname{Re}A_0}\right]\right\}$$
$$= 0.00217(26)(62)(50)$$
$$\overset{\bullet}{\underset{\text{stat}}} \overset{\bullet}{\underset{\text{sys}}} \overset{\bullet}{\underset{\text{IB} + \text{EM}}}$$

Consistent with experimental result:

$$\operatorname{Re}(\epsilon'/\epsilon)_{\mathrm{expt}} = 0.00166(23)$$

### The road ahead

- Primary pure-lattice systematic is discretization error (12%). Currently estimated using scaling of I=2 operators but there may be significant "error on the error".
- Near-term availability of next-gen supercomputers (Perlmutter, Aurora) opens up opportunity to perform a full continuum extrapolation.
- Current plan is two additional ensembles with following properties:
  - Physical pion and kaon masses.
  - Same gauge action allowing continuum extrapolation with 3 points.
  - Same physical volume such that  $\pi\pi$  energy remains the same and the interaction remains physical.
- 40<sup>3</sup>x64, a<sup>-1</sup>=1.7 GeV and 48<sup>3</sup>x64, a<sup>-1</sup>=2.1 GeV are computationally feasible while providing a good lever arm (a<sup>2</sup> scaling).
- Already started generating 16<sup>3</sup> test ensembles for tuning.
- Measurement code has been ported to NVidia and Intel GPUs, utilizing Grid's portable GPU kernel API.

### The road ahead pt.2

- Independent calculation of  $\epsilon$ ' using multiple operators to extract on-shell matrix elements as excited-state contributions in a periodic lattice is well under way. [cf. talk by M.Tomii, Lattice 2021]
  - > Avoid complications of using G-parity BCs
  - > Uses existing MDWF+I ensembles with physical pion masses
  - > 2 lattice spacings allowing continuum limit
- We are developing techniques to perform 3-4f matching in the Wilson coefficients non-perturbatively in order to avoid relying on PT at the charm scale.
   [Pos LATTICE2018 (2019) 216]
- Also working on laying the groundwork for the lattice calculation of EM contributions.
   [cf. talk by J.Karpie, Lattice 2021]

### Conclusions

- Completed update on our 2015 lattice determination of  $A_0$  and  $\epsilon$ '
  - 3.2x increase in statistics.
  - Improved systematic errors, notably use of multi-operator techniques essentially removes excited-state systematic.
- Reproduce experimental value for  $\Delta I = 1/2$  rule, demonstrating that QCD sufficient to solve this decades-old puzzle.
- Result for  $\varepsilon$ ' consistent with experimental value.
- Total error is  $\sim$ 3.6x that of experiment.
- ε' remains a promising avenue to search for new physics, but greater precision is required.
- The work goes on....

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#### **Excited state contamination**

- Primary concern is residual excited-state contamination
- See excellent consistency and strong plateaus among fits for 2+ operators with  $t'_{\mbox{\scriptsize min}}{\geq}4$
- Also examine 2 and 3-state fits with 3 ops:

