

Thermal modification of open heavy-flavour mesons from an effective hadronic theory

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[GM, Angels Ramos, Laura Tolos, Juan Torres-Rincon, Phys.Lett.B 806 (2020)]

[GM, Angels Ramos, Laura Tolos, Juan Torres-Rincon, Phys.Rev.D 102 (2020)]

[GM, Olaf Kaczmarek, Laura Tolos, Angels Ramos, Eur.Phys.J.A 56 (2020)]

[Juan Torres-Rincon, GM, Angels Ramos, Laura Tolos, arXiv:2106.01156]

A Virtual Tribute to Quark Confinement and the Hadron Spectrum 2021

2-6 August 2021



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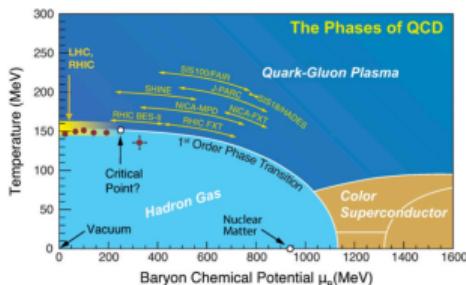
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EXCELENCIA
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DE MAEZTU



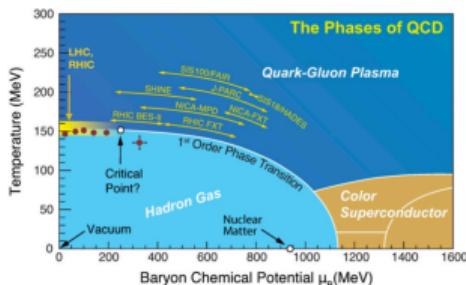
Introduction

INTRODUCTION



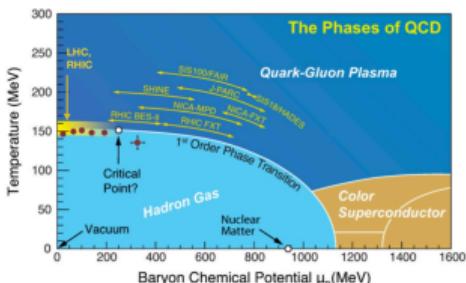
- Matter at **very high temperatures and vanishing baryon densities** (QGP?) is produced in HICs at RHIC and LHC
→ **hot mesonic (pionic) matter after confinement transition**

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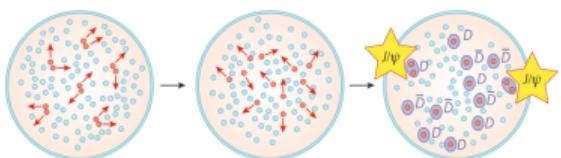
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- ▶ Heavy quarks are formed at the initial stage of the collision and have a large relaxation time

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- ▶ Matter at **very high temperatures** and **vanishing baryon densities** (QGP?) is produced in HICs at RHIC and LHC
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- ▶ Heavy quarks are formed at the initial stage of the collision and have a large relaxation time
- ▶ **Heavy mesons** are a powerful probe of the QGP
 - Open heavy-flavour mesons created at the confinement transition
 - They interact with the light mesons in the medium
 - Quarkonia suppression: color screening + comover scattering

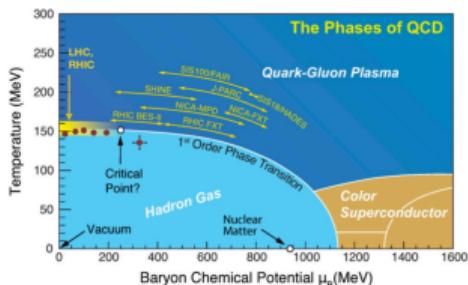
Color screening



Comover scattering

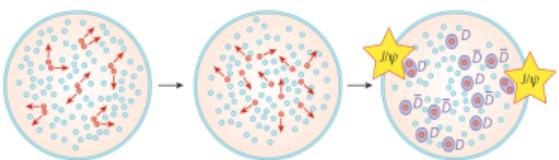


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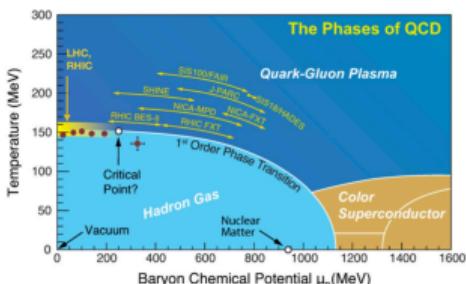
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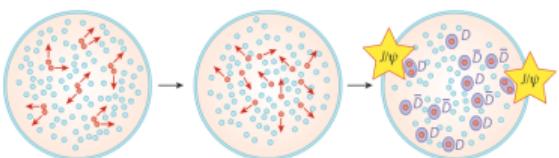


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- ▶ Properties of hadrons and their thermal modification are contained in their spectral functions
- ▶ **Spectral functions** can be calculated with effective hadronic theories within a unitarized approach

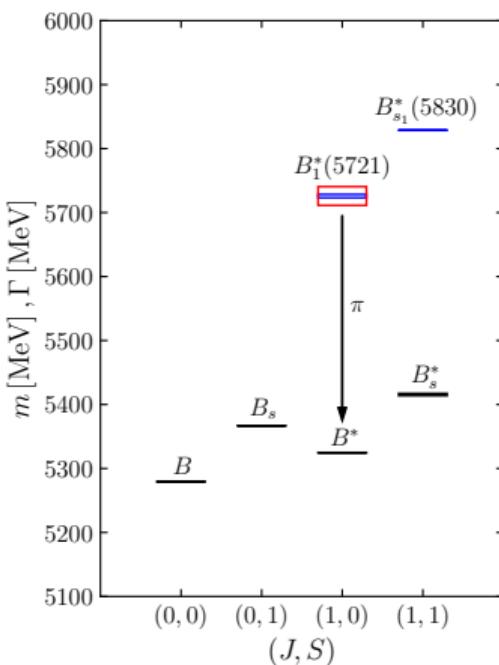
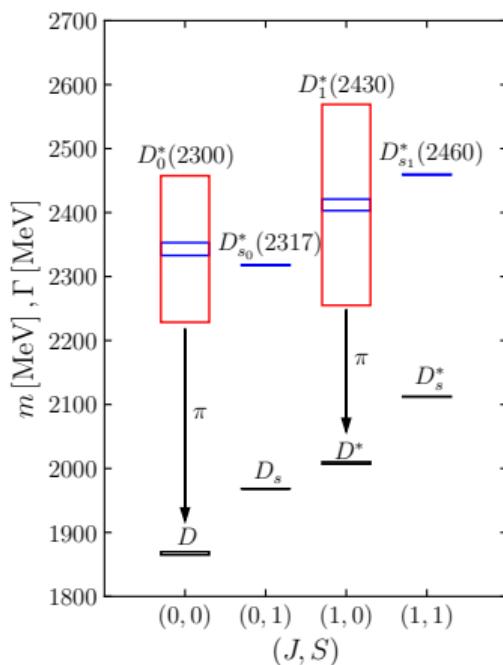
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Comover scattering



OPEN HEAVY-FLAVOUR SPECTRUM



- ▶ Broad resonances with $S = 0$
- ▶ Narrow states with $S = 1$

[P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. 2020, 083C01 (2020)]

How do these states change with temperature?

Scattering of open heavy-flavour mesons off light mesons in free space

EFFECTIVE THEORY

Effective Lagrangian based on approximate **chiral** and **heavy-quark spin symmetries**

- ▶ Chiral expansion up to NLO: broken by light meson masses ($\Phi = \pi, K, \bar{K}, \eta$)
- ▶ Heavy-quark expansion up to LO: broken by physical heavy meson masses (D, D_s, D^*, D_s^*)

$$\mathcal{L}(D^{(*)}, \Phi) = \mathcal{L}_{\text{LO}}(D^{(*)}, \Phi) + \mathcal{L}_{\text{NLO}}(D^{(*)}, \Phi)$$

$$\begin{aligned} \mathcal{L}_{\text{LO}} = & \langle \nabla^\mu D \nabla_\mu D^\dagger \rangle - m_D^2 \langle DD^\dagger \rangle - \langle \nabla^\mu D^{*\nu} \nabla_\mu D_\nu^{*\dagger} \rangle + m_D^2 \langle D^{*\nu} D_\nu^{*\dagger} \rangle \\ & + i g \langle D^{*\mu} u_\mu D^\dagger - D u^\mu D_\mu^{*\dagger} \rangle + \frac{g}{2m_D} \langle D_\mu^* u_\alpha \nabla_\beta D_\nu^{*\dagger} - \nabla_\beta D_\mu^* u_\alpha D_\nu^{*\dagger} \rangle \epsilon^{\mu\nu\alpha\beta} \\ u = & \exp \left(\frac{i\Phi}{\sqrt{2}f} \right), \quad \nabla^\mu = \partial^\mu - \frac{1}{2} (u^\dagger \partial^\mu u + u \partial^\mu u^\dagger), \quad u^\mu = i(u^\dagger \partial^\mu u - u \partial^\mu u^\dagger) \end{aligned}$$

[Kolomeitsev and Lutz (2004)]

[Lutz and Soyeur (2008)]

[Guo, Hanhart and Meißner (2009)]

[Geng, Kaiser, Martin-Camalich and Weise (2010)]

...

$$D = (D^0 \quad D^+ \quad D_s^+) ,$$

$$D_\mu^* = (D^{*0} \quad D^{*+} \quad D_s^{*+})_\mu$$

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$$\begin{aligned} \mathcal{L}_{\text{NLO}} = & - h_0 \langle DD^\dagger \rangle \langle \chi_+ \rangle + h_1 \langle D \chi_+ D^\dagger \rangle + h_2 \langle DD^\dagger \rangle \langle u^\mu u_\mu \rangle + h_3 \langle Du^\mu u_\mu D^\dagger \rangle \\ & + h_4 \langle \nabla_\mu D \nabla_\nu D^\dagger \rangle \langle u^\mu u^\nu \rangle + h_5 \langle \nabla_\mu D \{u^\mu, u^\nu\} \nabla_\nu D^\dagger \rangle + \{D \rightarrow D_\mu^*\} \end{aligned}$$

LECs : $h_{0,\dots,5}, \tilde{h}_{0,\dots,5}$

[Liu, Orginos, Guo, Hanhart and Meiñner (2013)]

[Tolos and Torres-Rincon (2013)]

[Albaladejo, Fernandez-Soler, Guo and Nieves (2017)]

[Guo, Liu, Meiñner, Oller and Rusetsky (2019)]

SCATTERING IN COUPLED CHANNELS

s-wave scattering amplitude of $D^{(*)}$, $D_s^{(*)}$ mesons with π , K , \bar{K} , η :

$$\begin{aligned} \mathcal{L} \rightarrow V^{ij}(s, t, u) = & \frac{1}{f_\pi^2} \left[\frac{1}{4} C_{\text{LO}}^{ij} (s - u) - 4 C_0^{ij} h_0 + 2 C_1^{ij} h_1 \right. \\ & - 2 C_{24}^{ij} \left(2h_2(p_2 \cdot p_4) + h_4((p_1 \cdot p_2)(p_3 \cdot p_4) + (p_1 \cdot p_4)(p_2 \cdot p_3)) \right) \\ & \left. + 2 C_{35}^{ij} \left(h_3(p_2 \cdot p_4) + h_5((p_1 \cdot p_2)(p_3 \cdot p_4) + (p_1 \cdot p_4)(p_2 \cdot p_3)) \right) \right], \end{aligned}$$

$D_i(p_1)$ $D_j(p_3)$



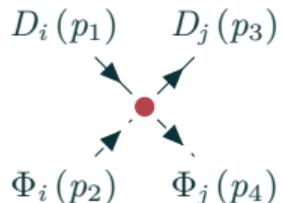
$\Phi_i(p_2)$ $\Phi_j(p_4)$

C_n^{ij} : isospin coefficients

SCATTERING IN COUPLED CHANNELS

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Unitarization: Bethe-Salpeter equation

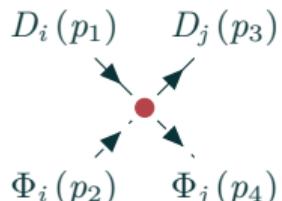
$$D_i \quad D_j = D_i \quad D_j + D_i \quad D_k \quad D_j + D_i \quad D_k \quad D_l \quad D_j + \dots$$

$$T_{ij} = V_{ij} + V_{ik} G_k V_{kj} + V_{ik} G_k V_{kl} G_l V_{lj} + \dots$$

SCATTERING IN COUPLED CHANNELS

s-wave scattering amplitude of $D^{(*)}$, $D_s^{(*)}$ mesons with π , K , \bar{K} , η :

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Unitarization: Bethe-Salpeter equation

$$D_i \quad D_j = D_i \quad D_j + D_i \quad D_k \quad D_j \quad \longrightarrow$$

$\Phi_i \quad \Phi_j$ $\Phi_i \quad \Phi_j$ $\Phi_i \quad \Phi_k \quad \Phi_j$

The diagram shows the Bethe-Salpeter equation. On the left, two mesons D_i and D_j (green circles with arrows) interact. This is equated to the sum of a bare interaction term (mesons D_i and D_j plus a red dot) and a loop correction term (mesons D_i , D_j , and D_k with a circular loop between D_i and D_k , and D_k and D_j). An arrow points to the right, indicating the result of the unitarization process.

$$T_{ij} = V_{ij} + V_{ik} G_k T_{kj}$$

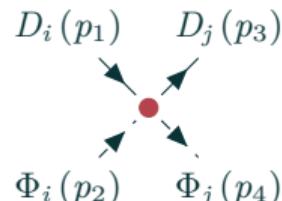
On-shell factorization of the T -matrix:

$$T = (1 - VG)^{-1} V$$

SCATTERING IN COUPLED CHANNELS

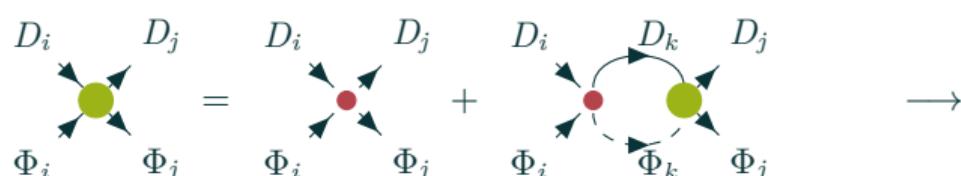
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C_n^{ij} : isospin coefficients

Unitarization: Bethe-Salpeter equation



- The two-meson propagator is regularized with a **cutoff**

$$T_{ij} = V_{ij} + V_{ik} G_k T_{kj}$$

On-shell factorization of the T -matrix:

$$T = (1 - VG)^{-1} V$$

$$G_k = i \int^\Lambda \frac{d^4 q}{(2\pi)^4} \frac{1}{q^2 - m_{D,k}^2 + i\varepsilon} \frac{1}{(P - q)^2 - m_{\Phi,k}^2 + i\varepsilon}$$

- Poles in different Riemann sheets: **bound states**, **resonances** and **virtual states**, $m_R = \text{Re } z_R$, $\Gamma_R = 2\text{Im } z_R$
- Identification of the dynamically generated states with the experimental ones

RESULTS: DYNAMICALLY GENERATED OPEN-CHARM STATES

	$D_0^*(2300)$	$D_{s0}^*(2317)$	$D_1^*(2430)$	$D_{s1}^*(2460)$
M_R (MeV)	2343 ± 10	2317.8 ± 0.5	2412 ± 9	2459.5 ± 0.6
Γ_R (MeV)	229 ± 16	< 3.8	314 ± 29	< 3.5

J^P	(S, I)	Coupled channels	RS	Poles (MeV)	Couplings (GeV)
0^+	$(0, \frac{1}{2})$	$D\pi$ $D\eta$ $D_s\bar{K}$	$(-, +, +)$	$2081.9 - i86.0$	$ g_{D\pi} = 8.9, g_{D\eta} = 0.4, g_{D_s\bar{K}} = 5.4$
		$(2005.28) \quad (2415.10) \quad (2463.98)$	$(-, -, +)$	$2529.3 - i145.4$	$ g_{D\pi} = 6.7, g_{D\eta} = 9.9, g_{D_s\bar{K}} = 19.4$
	$(1, 0)$	DK $D_s\eta$	$(+, +)$	$2252.5 - i0.0$	$ g_{DK} = 13.3, g_{D_s\eta} = 9.2$
		$(2364.88) \quad (2516.20)$			
1^+	$(0, \frac{1}{2})$	$D^*\pi$ $D^*\eta$ $D_s^*\bar{K}$	$(-, +, +)$	$2222.3 - i84.7$	$ g_{D^*\pi} = 9.5, g_{D^*\eta} = 0.4, g_{D_s^*\bar{K}} = 5.7$
		$(2146.59) \quad (2556.42) \quad (2607.84)$	$(-, -, +)$	$2654.6 - i117.3$	$ g_{D^*\pi} = 6.5, g_{D^*\eta} = 10.0, g_{D_s^*\bar{K}} = 18.5$
	$(1, 0)$	D^*K $D_s^*\eta$	$(+, +)$	$2393.3 - i0.0$	$ g_{D^*K} = 14.2, g_{D_s^*\eta} = 9.7$
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		$(2005.28) \quad (2415.10) \quad (2463.98)$	$(-, -, +)$	$2529.3 - i145.4$	$ g_{D\pi} = 6.7, g_{D\eta} = 9.9, g_{D_s\bar{K}} = 19.4$
	$(1, 0)$	DK $D_s\eta$	$(+, +)$	$2252.5 - i0.0$	$ g_{DK} = 13.3, g_{D_s\eta} = 9.2$
		$(2364.88) \quad (2516.20)$			
1^+	$(0, \frac{1}{2})$	$D^*\pi$ $D^*\eta$ $D_s^*\bar{K}$	$(-, +, +)$	$2222.3 - i84.7$	$ g_{D^*\pi} = 9.5, g_{D^*\eta} = 0.4, g_{D_s^*\bar{K}} = 5.7$
		$(2146.59) \quad (2556.42) \quad (2607.84)$	$(-, -, +)$	$2654.6 - i117.3$	$ g_{D^*\pi} = 6.5, g_{D^*\eta} = 10.0, g_{D_s^*\bar{K}} = 18.5$
	$(1, 0)$	D^*K $D_s^*\eta$	$(+, +)$	$2393.3 - i0.0$	$ g_{D^*K} = 14.2, g_{D_s^*\eta} = 9.7$
		$(2504.20) \quad (2660.06)$			

RESULTS: DYNAMICALLY GENERATED OPEN-BEAUTY STATES

	$B_1^*(5721)$	$B_{s1}^*(5830)$
M_R (MeV)	$5725.9^{+2.5}_{-2.7}$	5828.7 ± 0.2
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	$(1, 0)$	$\bar{B}K$ $\bar{B}_s\eta$	$(+, +)$	$5639.3 - i0.0$ (5775.12) (5914.75)	$ g_{\bar{B}K} = 35.6$, $ g_{\bar{B}_s\eta} = 23.8$
1^+	$(0, \frac{1}{2})$	$\bar{B}^*\pi$ $\bar{B}^*\eta$ $\bar{B}_s^*\bar{K}$	$(-, +, +)$	$5528.6 - i72.3$ (5462.69) (5872.51) (5911.04)	$ g_{\bar{B}^*\pi} = 22.6$, $ g_{\bar{B}^*\eta} = 0.8$, $ g_{\bar{B}_s^*\bar{K}} = 14.4$ $ g_{\bar{B}^*\pi} = 10.7$, $ g_{\bar{B}^*\eta} = 18.0$, $ g_{\bar{B}_s^*\bar{K}} = 32.1$
	$(1, 0)$	\bar{B}^*K $\bar{B}_s^*\eta$	$(+, +)$	$5686.0 - i0.0$ (5820.29) (5963.26)	$ g_{\bar{B}^*K} = 14.2$, $ g_{\bar{B}_s^*\eta} = 9.7$

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				$5848.0 - i65.9$ ($-$, $-$, $+$)	
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				$5893.3 - i65.0$ ($-$, $-$, $+$)	$ g_{\bar{B}^*\pi} = 10.7$, $ g_{\bar{B}^*\eta} = 18.0$, $ g_{\bar{B}_s^*\bar{K}} = 32.1$
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Thermal Effective Field Theory

THERMAL MODIFICATION OF HEAVY MESONS IN A MESONIC BATH

► Imaginary-time formalism

- Sum over Matsubara frequencies → Bose-Einstein distribution functions

$$q^0 \rightarrow i\omega_n = \frac{i}{\beta} 2\pi n, \quad \int \frac{d^4 q}{(2\pi)^4} \rightarrow \frac{i}{\beta} \sum_n \int \frac{d^3 q}{(2\pi)^3} \quad (\text{bosons})$$

THERMAL MODIFICATION OF HEAVY MESONS IN A MESONIC BATH

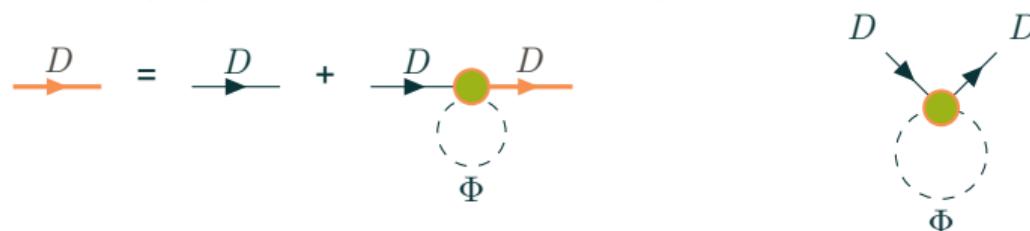
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► Dressing the mesons in the loop function

- Self-energy corrections
- Pion mass varies slightly below T_c → only the heavy meson is dressed



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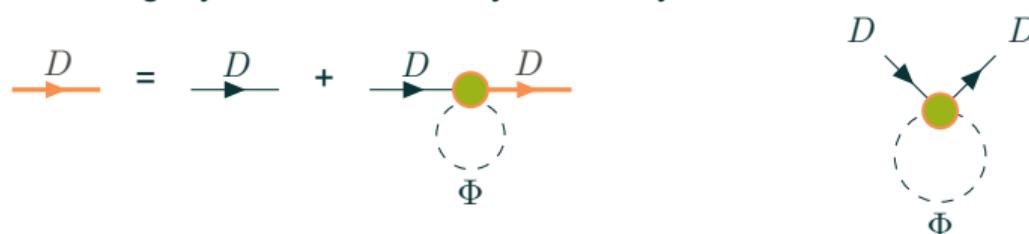
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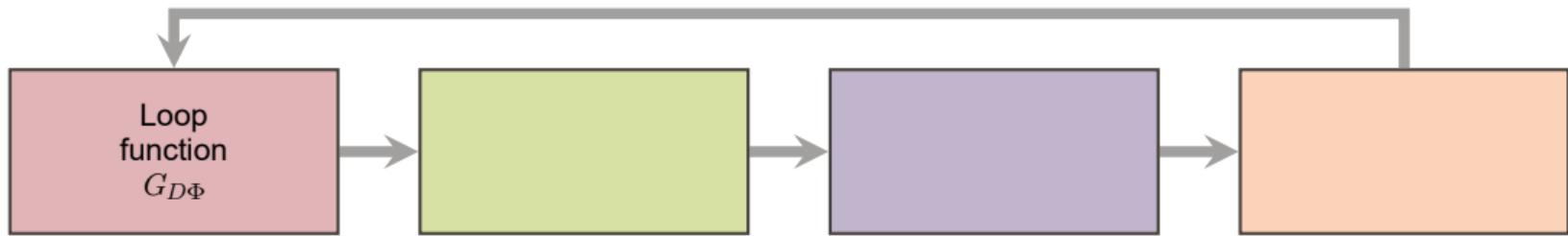
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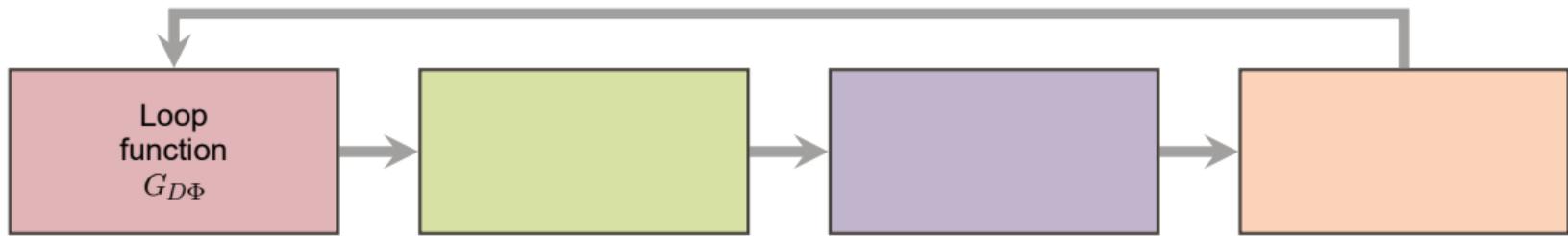
In the bath, processes that are forbidden in free space become possible: both **production** and **absorption of heavy-light pairs**.

SELF-CONSISTENT ITERATIVE PROCEDURE



$$G_{D\Phi}(E, \vec{p}; T) = \int \frac{d^3 q}{(2\pi)^3} \int d\omega \int d\omega' \frac{S_D(\omega, \vec{q}; T) S_\Phi(\omega', \vec{p} - \vec{q}; T)}{E - \omega - \omega' + i\varepsilon} [1 + f(\omega, T) + f(\omega', T)]$$

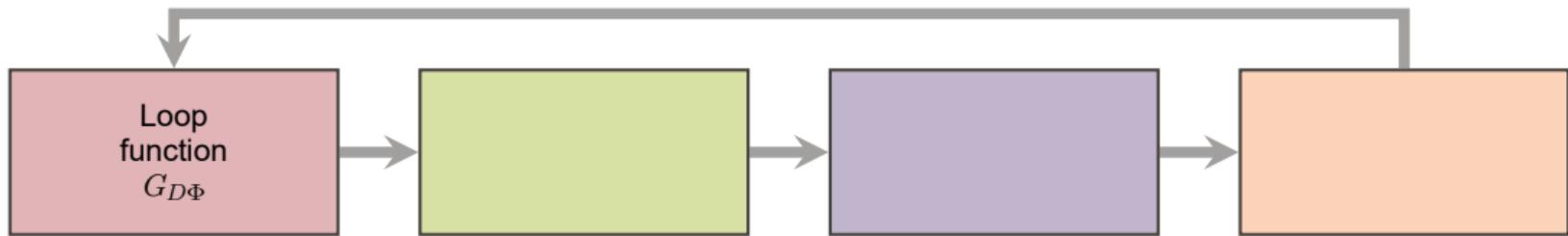
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Spectral functions

SELF-CONSISTENT ITERATIVE PROCEDURE

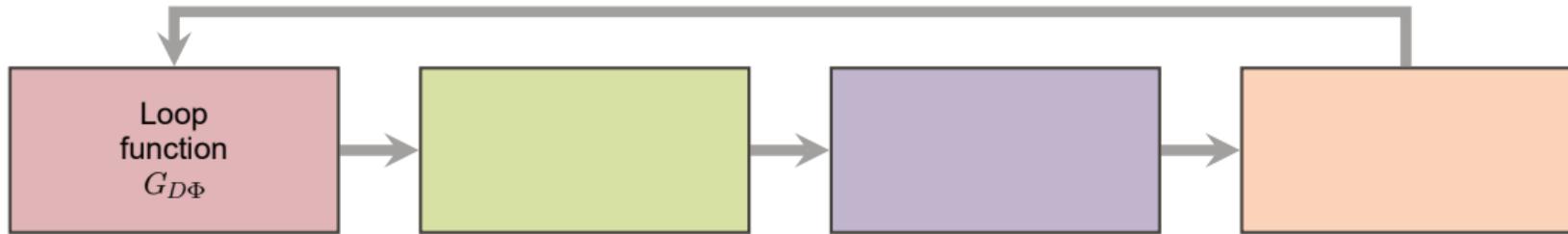


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Spectral functions

Bose distribution function at T: $f(\omega, T) = \frac{1}{e^{\omega/T} - 1}$ (At zero temperature $f(\omega, T = 0) = 0$.)

SELF-CONSISTENT ITERATIVE PROCEDURE



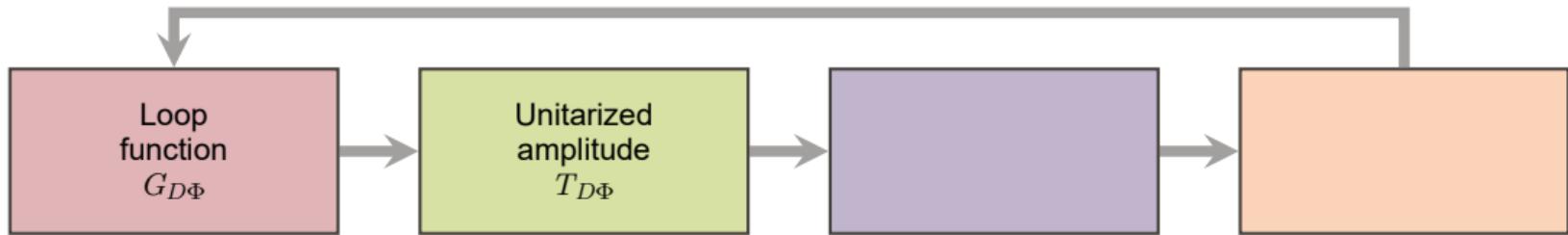
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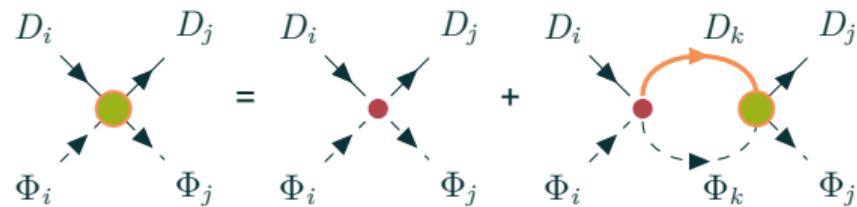
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Regularized with a cutoff Λ

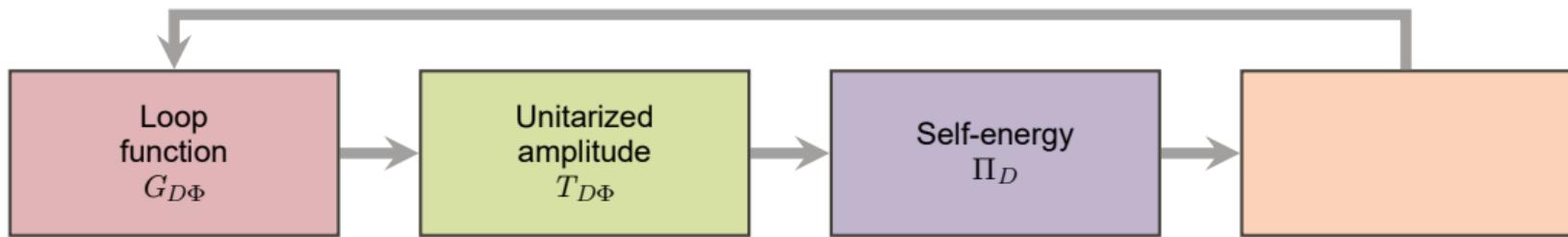
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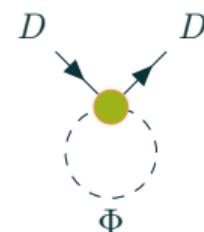
$$T_{ij} = V_{ij} + V_{ik} G_k T_{kj}$$



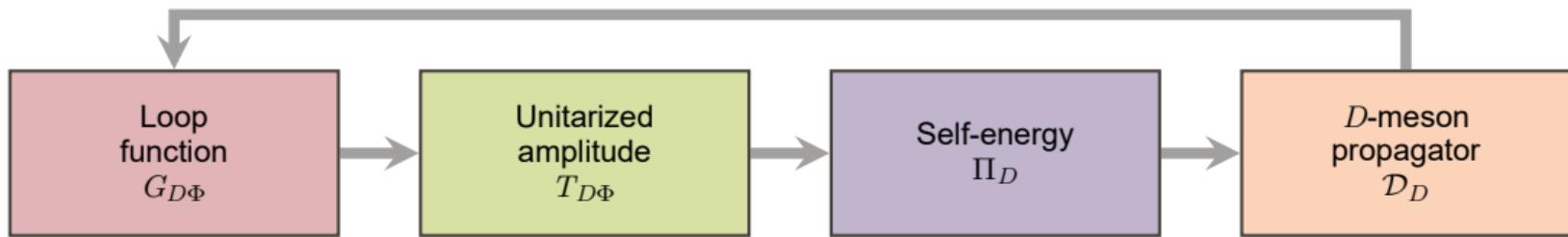
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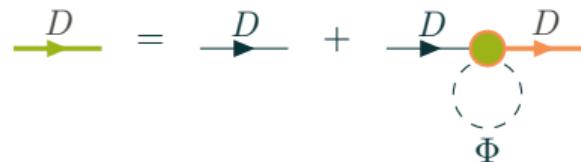
$$\Pi_D(E, \vec{p}; T) = \frac{1}{\pi} \int \frac{d^3 q}{(2\pi)^3} \int d\Omega \frac{E}{\omega_\Phi} \frac{f(\Omega, T) - f(\omega_\Phi, T)}{E^2 - (\omega_\Phi - \Omega)^2 + i\varepsilon} \text{Im } T_{D\Phi}(\Omega, \vec{p} + \vec{q}; T)$$



SELF-CONSISTENT ITERATIVE PROCEDURE



$$S_D(\omega, \vec{q}; T) = -\frac{1}{\pi} \text{Im } \mathcal{D}_D(\omega, \vec{q}; T) = -\frac{1}{\pi} \text{Im} \left(\frac{1}{\omega^2 - \vec{q}^2 - m_D^2 - \Pi_D(\omega, \vec{q}; T)} \right)$$



Results: Thermal modification of open-charm mesons

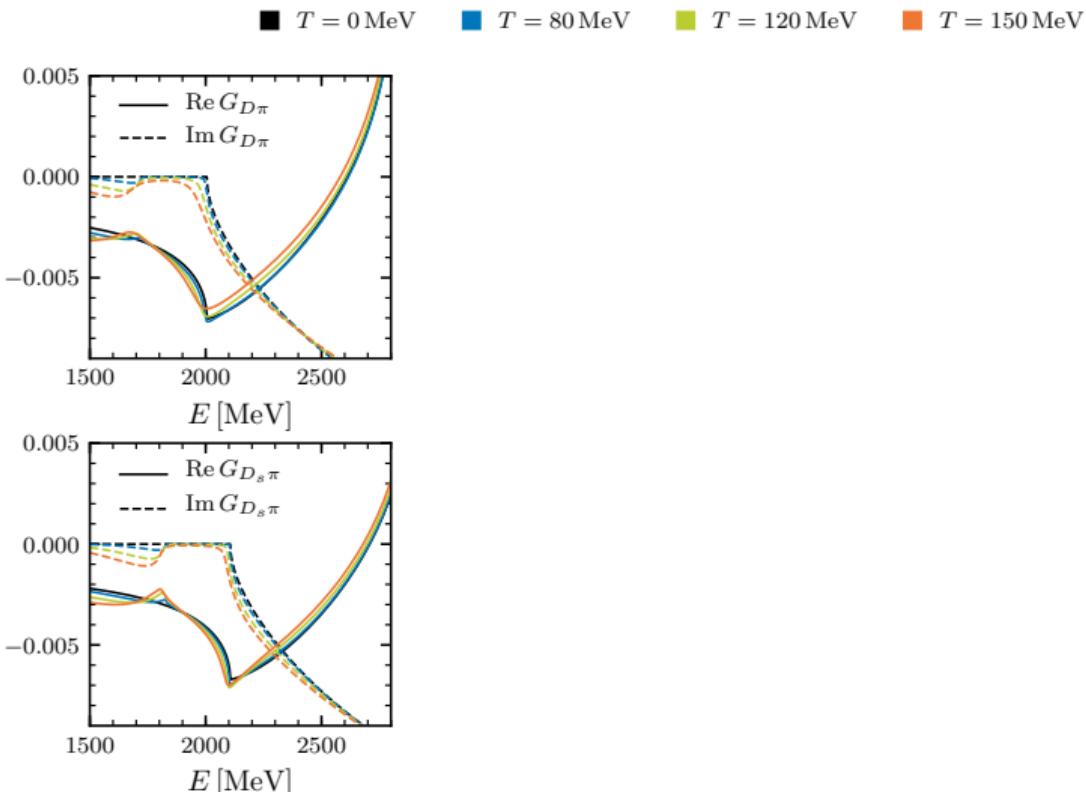
LOOP FUNCTIONS

Pionic bath

D and D_s with light mesons

Unitary cut:
 $E \geq (m_D + m_\Phi)$

Landau cut:
 $E \leq (m_D - m_\Phi)$



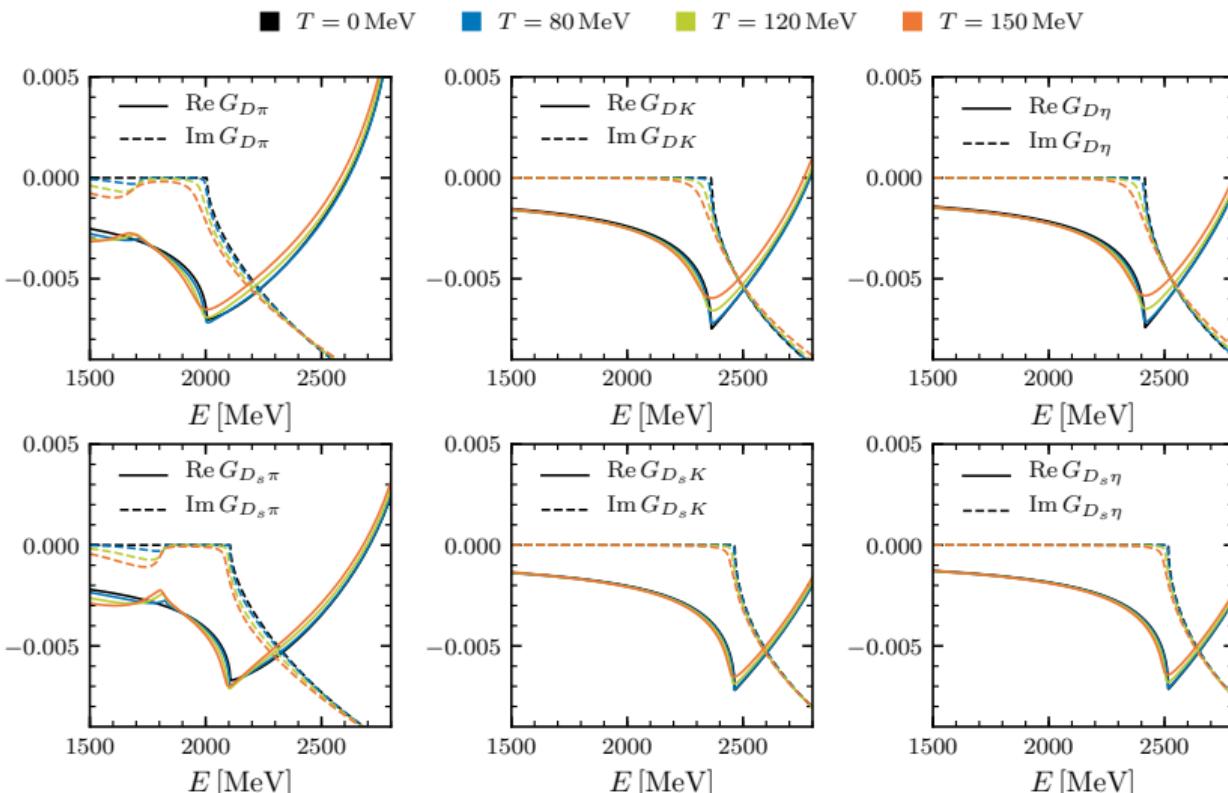
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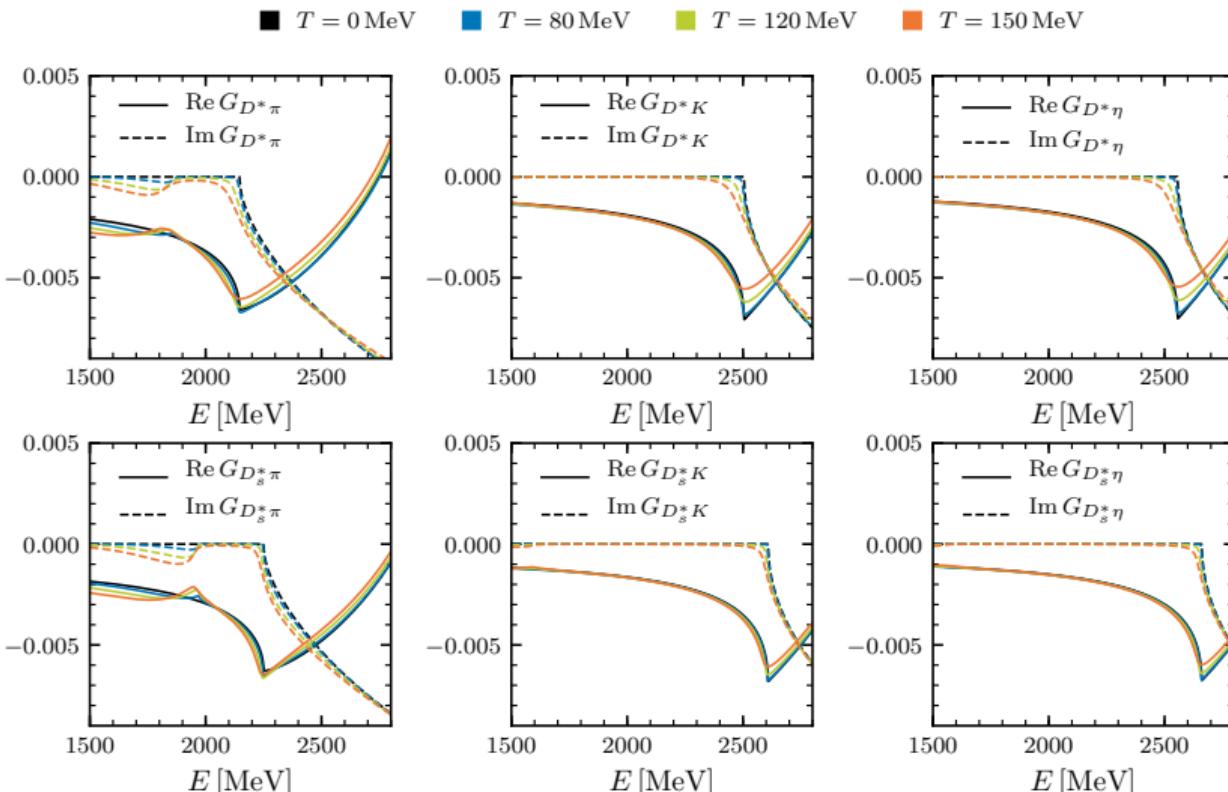
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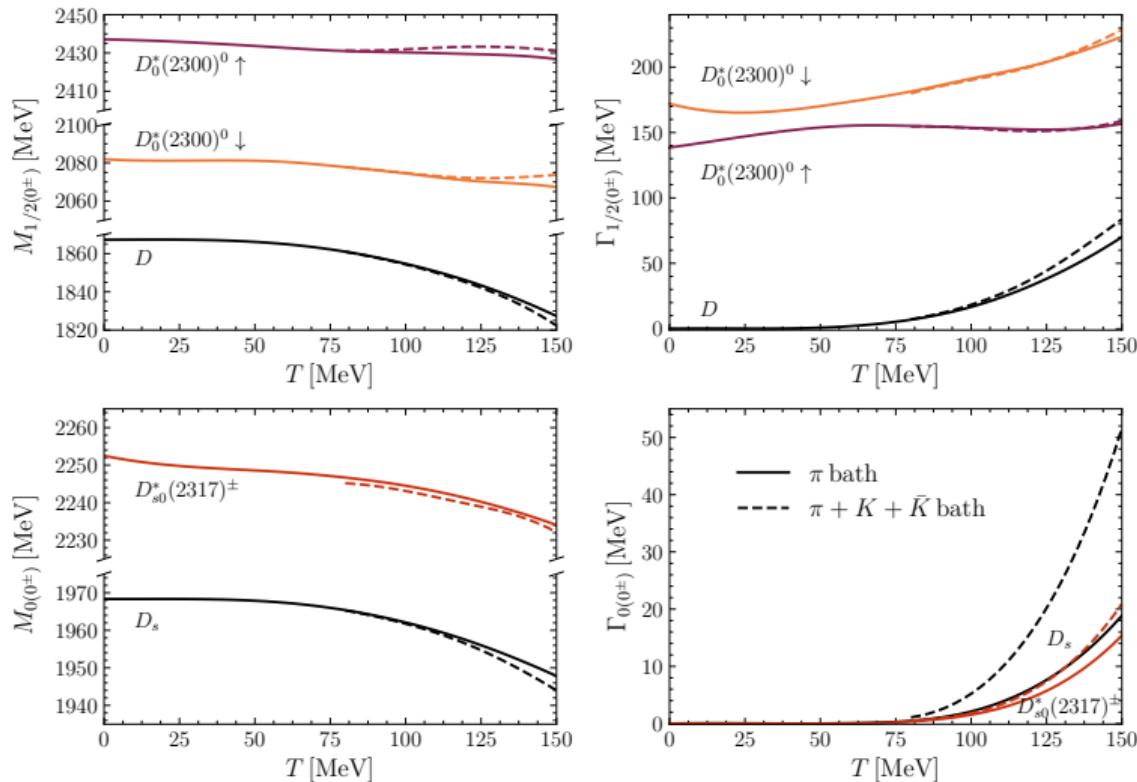


CHIRAL PARTNERS

Evolution of masses and widths

- ▶ Pionic bath (solid lines)
- ▶ Bath of π, K, \bar{K} (dashed lines)

$$I(J^P) = \frac{1}{2}(0^\pm), 0(0^\pm)$$



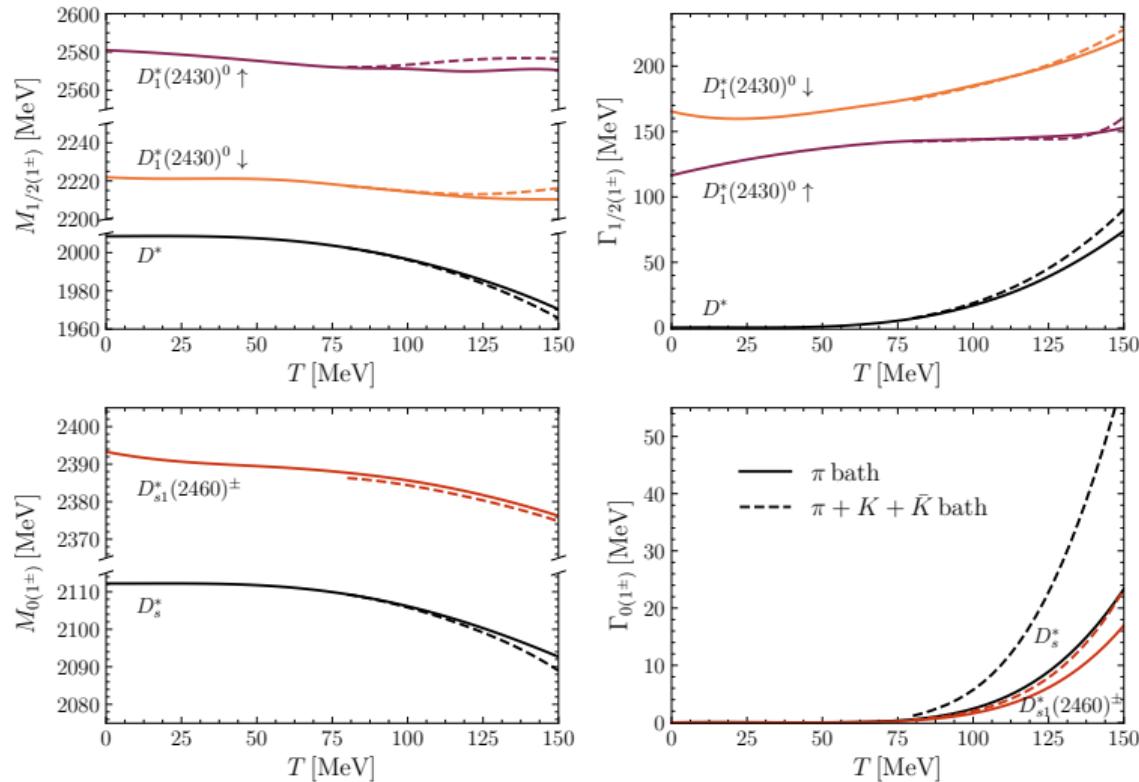
[GM, A. Ramos, L. Tolos, J. Torres-Rincon,
Phys.Rev.D 102 (2020)]

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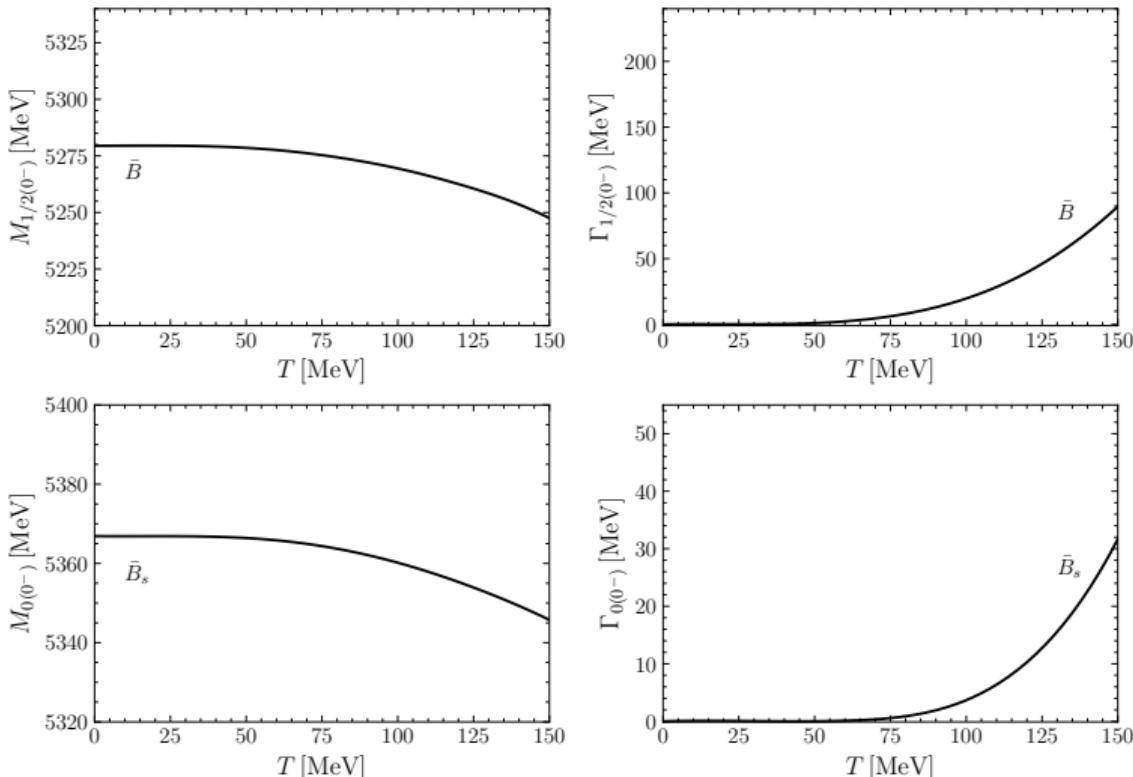
B MESONS

Evolution of masses and widths
of the ground states

► Pionic bath

$$I(J^P) = \frac{1}{2}(0^-), 0(0^-)$$

Similiar thermal effects for D
and B mesons



Euclidean correlators: comparison with lattice QCD

FROM SPECTRAL FUNCTIONS TO EUCLIDEAN CORRELATORS

Spectral function $\rho(\omega, \vec{p}; T) \longrightarrow$ Euclidean correlator $G_E(\tau, \vec{p}; T)$

$$G_E(\tau, \vec{p}; T) = \int_0^\infty d\omega K(\tau, \omega; T) \rho(\omega, \vec{p}; T)$$

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Euclidean correlator \longrightarrow Spectral function (ill-posed)

- Bayesian methods (e.g. MEM)
- Fitting Ansätze

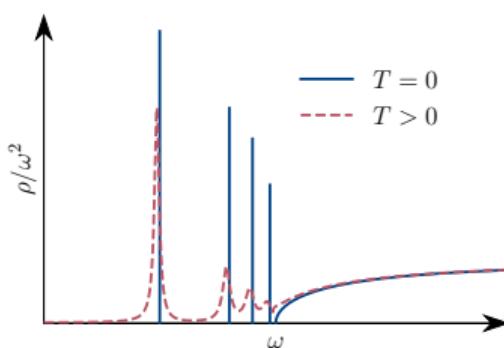
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$$S_D(\omega, \vec{q}; T) = -\frac{1}{\pi} \text{Im} \left(\frac{1}{\omega^2 - \vec{q}^2 - M_D^2 - \Pi_D(\omega, \vec{q}; T)} \right)$$

at unphysical meson masses (used in the lattice)

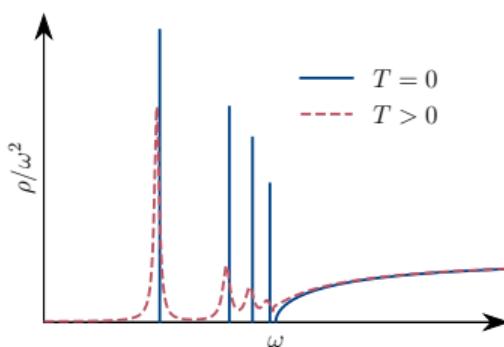
FROM SPECTRAL FUNCTIONS TO EUCLIDEAN CORRELATORS

Spectral function $\rho(\omega, \vec{p}; T) \longrightarrow$ **Euclidean correlator** $G_E(\tau, \vec{p}; T)$

$$G_E(\tau, \vec{p}; T) = \int_0^\infty d\omega K(\tau, \omega; T) \rho(\omega, \vec{p}; T) \quad \rightarrow \quad K(\tau, \omega; T) = \frac{\cosh[\omega(\tau - \frac{1}{2T})]}{\sinh(\frac{\omega}{2T})}$$

Euclidean correlator \longrightarrow **Spectral function** (ill-posed)

- Bayesian methods (e.g. MEM)
- Fitting Ansätze



$$S_D(\omega, \vec{q}; T) = -\frac{1}{\pi} \text{Im} \left(\frac{1}{\omega^2 - \vec{q}^2 - M_D^2 - \Pi_D(\omega, \vec{q}; T)} \right)$$

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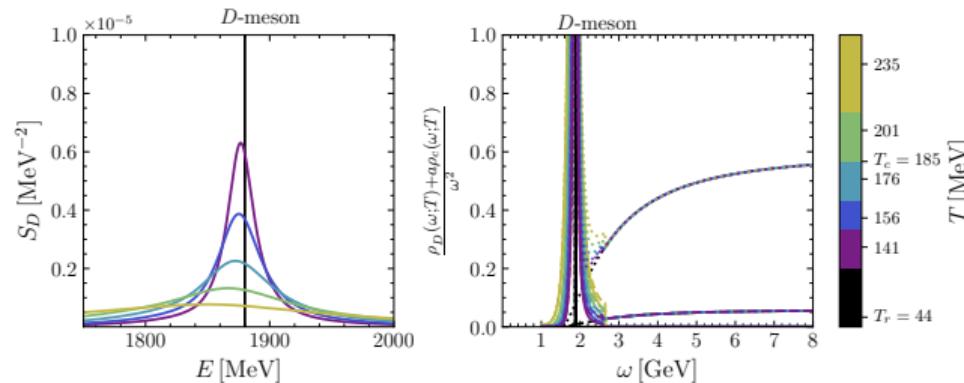
► Full: $\rho(\omega; T) = \rho_{\text{gs}}(\omega; T) + a\rho_{\text{cont}}(\omega; T)$

EUCLIDEAN CORRELATORS WITH EFT

$$\begin{aligned} m_\pi &= 384 \text{ MeV} \\ m_K &= 546 \text{ MeV} \\ m_\eta &= 589 \text{ MeV} \\ m_D &= 1880 \text{ MeV} \\ m_{D_s} &= 1943 \text{ MeV} \end{aligned}$$

[Kelly, Rothkopf, Skullerud (2018)]

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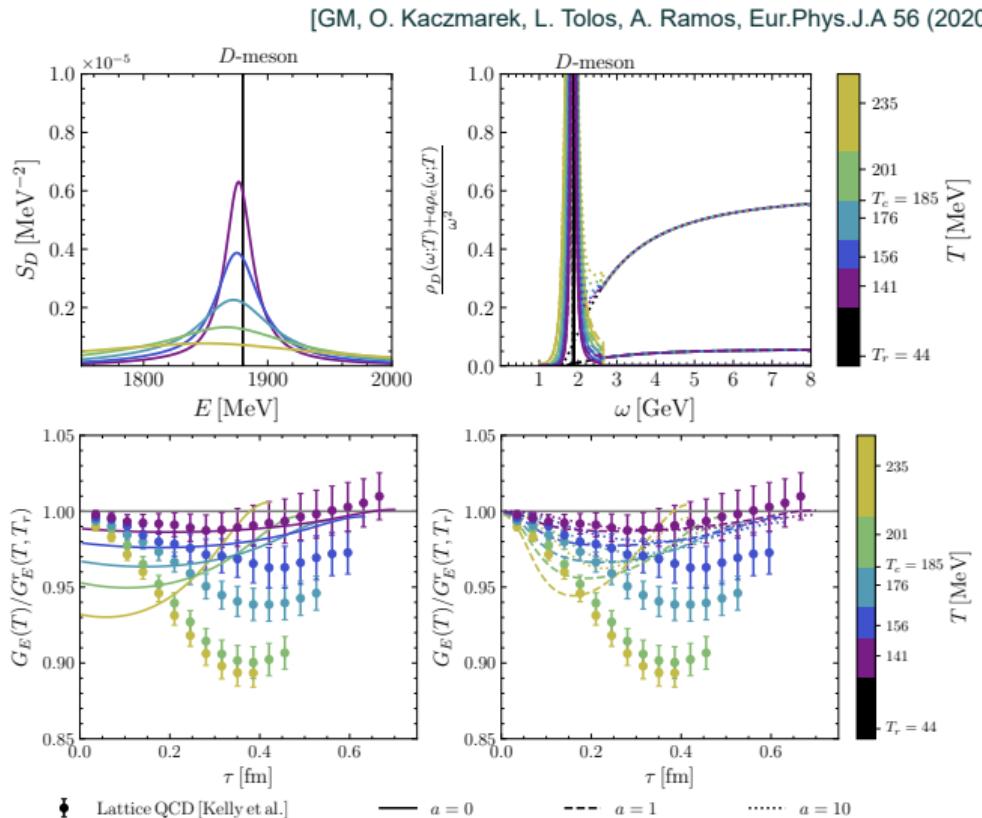


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- ▶ The inclusion of the continuum improves the comparison at small τ
- ▶ Good agreement at the lowest temperature. At larger temperatures: excited states?
- ▶ Close and above T_c the EFT breaks down
- ▶ Similar results for the D_s



Transport coefficients of an off-shell D meson

TRANSPORT COEFFICIENTS OF AN OFF-SHELL D -MESON

Fokker-Planck equation for the Green's function

$$\frac{\partial}{\partial t} G_D^<(t, k) = \frac{\partial}{\partial k^i} \left\{ \hat{A}(k; T) k^i G_D^<(t, k) + \frac{\partial}{\partial k^j} \left[\hat{B}_0(k; T) \Delta^{ij} + \hat{B}_1(k; T) \frac{k^i k^j}{\mathbf{k}^2} \right] G_D^<(t, k) \right\}$$

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Off-shell transport coefficients

- Drag force

$$\hat{A}(k^0, \mathbf{k}; T) \equiv \frac{1}{2k^0} \int \frac{dk_1^0}{2\pi} \frac{d^3 q}{(2\pi)^3} W(k^0, \mathbf{k}, k_1^0, \mathbf{q}) \frac{\mathbf{q} \cdot \mathbf{k}}{\mathbf{k}^2}$$

- Diffusion coefficients

$$\hat{B}_0(k^0, \mathbf{k}; T) \equiv \frac{1}{4} \frac{1}{2k^0} \int \frac{dk_1^0}{2\pi} \frac{d^3 q}{(2\pi)^3} W(k^0, \mathbf{k}, k_1^0, \mathbf{q}) \left[\mathbf{q}^2 - \frac{(\mathbf{q} \cdot \mathbf{k})^2}{\mathbf{k}^2} \right]$$

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$$\begin{aligned} \frac{1}{2k^0} \int \frac{dk_1^0}{2\pi} \frac{d^3 q}{(2\pi)^3} W(k^0, \mathbf{k}, k_1^0, \mathbf{q}) &= \frac{1}{2k^0} \sum_{\lambda, \lambda'=\pm} \lambda \lambda' \int_{-\infty}^{\infty} dk_1^0 \int \prod_{i=1}^3 \frac{d^3 k_i}{(2\pi)^3} \frac{1}{2E_2 2E_3} S_D(k_1^0, \mathbf{k}_1) \\ &\times (2\pi)^4 \delta^{(3)}(\mathbf{k} + \mathbf{k}_3 - \mathbf{k}_1 - \mathbf{k}_2) \delta(k^0 + \lambda' E_3 - \lambda E_2 - k_1^0) \\ &\times |T(k^0 + \lambda' E_3, \mathbf{k} + \mathbf{k}_3)|^2 f^{(0)}(\lambda' E_3) \tilde{f}^{(0)}(\lambda E_2) \tilde{f}^{(0)}(k_1^0) \end{aligned}$$

- Thermal effects in $|T|^2$ and E_k
- Landau cut
- Off-shell effects

RESULTS: D MESON TRANSPORT COEFFICIENTS

In the static limit $\mathbf{k} \rightarrow 0$

For $k^0 = E_k$ solution of

$$E_k^2 - \mathbf{k}^2 - m_D^2 - \text{Re } \Pi(E_k, \vec{k}; T) = 0$$

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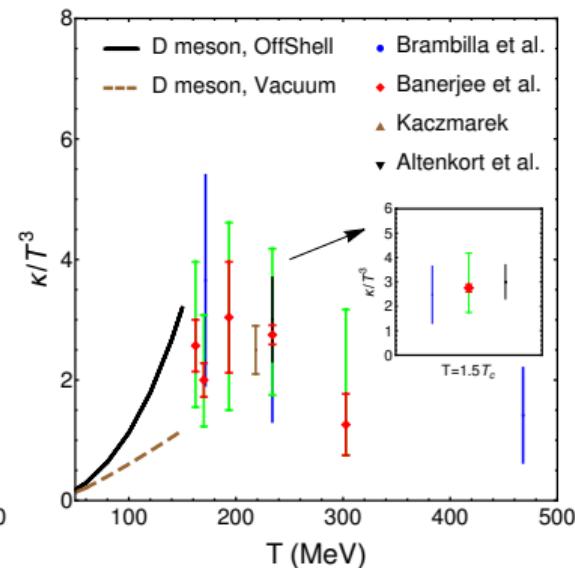
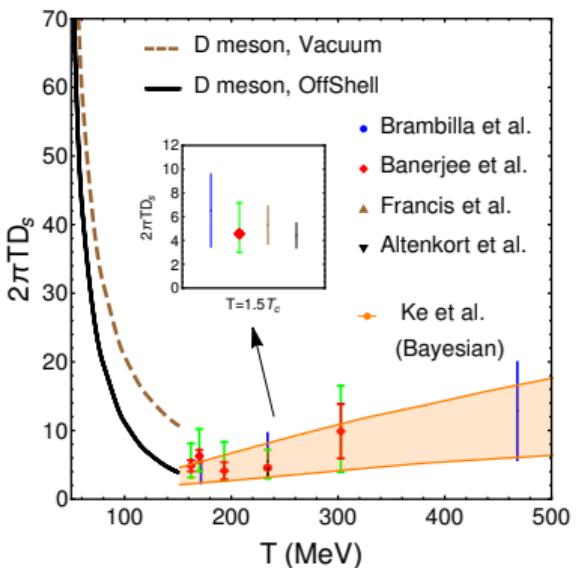
Spatial diffusion coefficient

$$2\pi TD_s(T) = \lim_{\mathbf{k} \rightarrow 0} \frac{2\pi T^3}{\hat{B}_0(E_k, \mathbf{k}; T)}$$

Momentum diffusion coefficient

$$\kappa(T) = 2\hat{B}_0(E_k, \mathbf{k} \rightarrow 0; T)$$

[J. Torres-Rincon, GM, A. Ramos, L. Tolos, arXiv:2106.01156]



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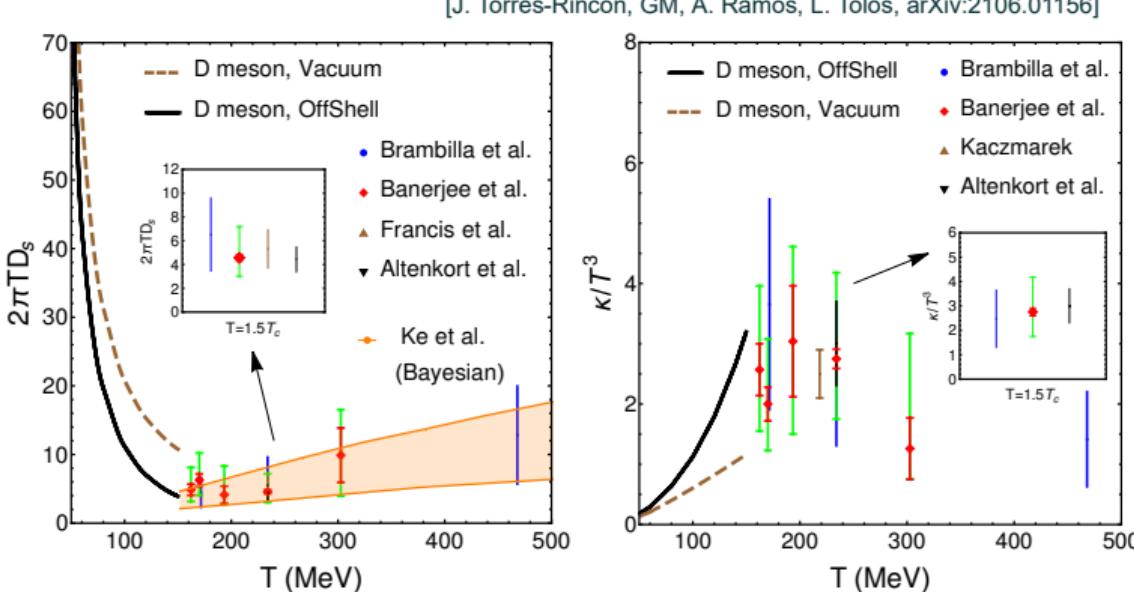
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Good matching around T_c of our results with the lattice QCD data and a Bayesian analysis, specially when thermal and off-shell effects are included.

Conclusions

CONCLUSIONS

- ▶ We have described the scattering of open heavy-flavour mesons off light mesons including **temperature corrections** in a self-consistent manner.
- ▶ We have obtained **spectral functions** at various temperatures below T_c .
- ▶ The **mass** of the open heavy-flavour ground-state mesons **decreases** with temperature while they **acquire a substantial width**.
- ▶ Modification also of the **dynamically generated resonances**, but still far from chiral degeneracy at the temperatures explored.
- ▶ The largest effect comes from the **pions in the bath**. Heavier light mesons are less abundant.
- ▶ We have obtained **Euclidean correlators** from spectral functions at unphysical masses, which are in **good agreement** with LQCD results **well below** T_c . The discrepancy close to T_c indicates the missing contribution of higher-excited states.
- ▶ We have introduced **thermal and off-shell effects** in the computation of **D-meson transport coefficients**. The **Landau Cut** contributes sizeably at moderate temperatures.

Thermal modification of open heavy-flavour mesons from an effective hadronic theory

Glòria Montaña

University of Barcelona
Institute of Cosmos Sciences

[GM, Angels Ramos, Laura Tolos, Juan Torres-Rincon, Phys.Lett.B 806 (2020)]

[GM, Angels Ramos, Laura Tolos, Juan Torres-Rincon, Phys.Rev.D 102 (2020)]

[GM, Olaf Kaczmarek, Laura Tolos, Angels Ramos, Eur.Phys.J.A 56 (2020)]

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A Virtual Tribute to Quark Confinement and the Hadron Spectrum 2021

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