

MODIFIED TMD FACTORIZATION AND SUB-LEADING POWER CORRECTIONS

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OUTLINE

1 INTRODUCTION

2 POWER CORRECTIONS

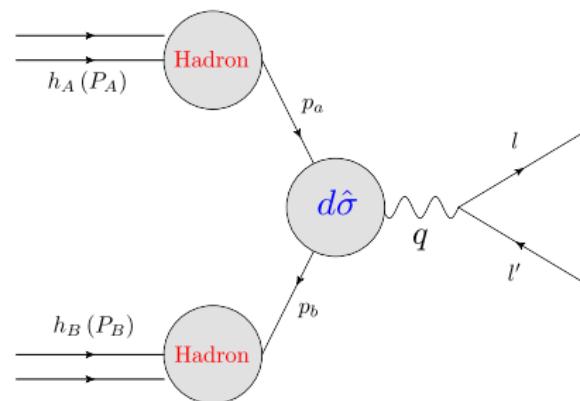
3 SUMMARY & OUTLOOK

FACTORIZATION THEOREM

Partonic cross section in Drell-Yan process

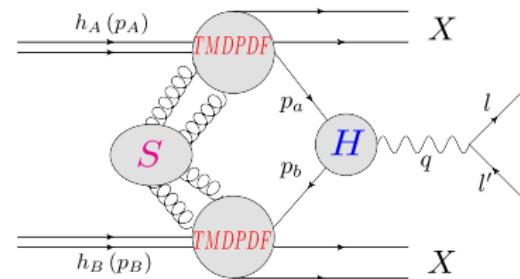
$$\frac{d\hat{\sigma}}{dQ^2 dy d\mathbf{q}_T^2} = \sigma^{\text{Born}} + \frac{1}{\mathbf{q}_T^2} \sum_{n=1} \alpha_s^n \frac{d\hat{\sigma}^{[n, -1]}}{dQ^2 dy d\mathbf{q}_T^2} + \delta^{(2)}(\mathbf{q}_T) \sum_{n=1} \alpha_s^n \frac{d\hat{\sigma}^{[n, 0]}}{dQ^2 dy d\mathbf{q}_T^2} + \frac{1}{Q^2} \sum_{m, n=1} \left(\frac{\mathbf{q}_T^2}{Q^2} \right)^m \alpha_s^n \frac{d\hat{\sigma}^{[n, m]}}{dQ^2 dy d\mathbf{q}_T^2}$$

- $\frac{d\sigma^{[n, -1]}}{dQ^2 dy d\mathbf{q}_T^2}$ and $\frac{d\sigma^{[n, 0]}}{dQ^2 dy d\mathbf{q}_T^2}$ are leading power contributions. Well studied in TMD and Collinear factorization Scimemi et al. JHEP 07 (2012), 002; Becher and Neubert, EPJC 71 (2011), 1665; Catani, Grazzini et al. Nucl. Phys. B. (2001); Grazzini et al. Phys. Rev. Lett. (2000)
- $\frac{d\hat{\sigma}^{[n, m]}}{dQ^2 dy d\mathbf{q}_T^2}$ are the power suppressed corrections: kinematics, Operator Product Expansion, SCET lagrangian.



TMD FACTORIZATION IN SCET

- The emerging partons are not **parallel** to the incoming hadron and are **off-shell**.
- The partons from the TMDPDFs have a non-negligible **transverse momentum** $\mathbf{p}_{T a(b)}$.
- All ingredients can be written as matrix elements of QFT operators, which can be further matched onto collinear PDF. **Vladimirov et al. EPJC 78 (2018) no.10, 802**
- The **transverse momentum** has to be **smaller** than the **collinear component** of the emerging parton: $p_{a(b)T}^2/Q^2 \sim q_T^2/Q^2 \ll 1$ up to power corrections.



$$\frac{d\sigma_{h_A h_B \rightarrow ll' X}^{\text{SCET}}}{dQ^2 dy dq_T^2} = \sum_c \sigma^{\text{Born}} H(\alpha_s, Q^2) \int \frac{d^2 \mathbf{b}_T}{(2\pi)^2} e^{i \mathbf{b}_T \cdot \mathbf{q}_T} F_{c \leftarrow h_A}(\alpha_s, x_A, b_T^2) F_{c \leftarrow h_B}(\alpha_s, b_T^2, x_B) + Y$$

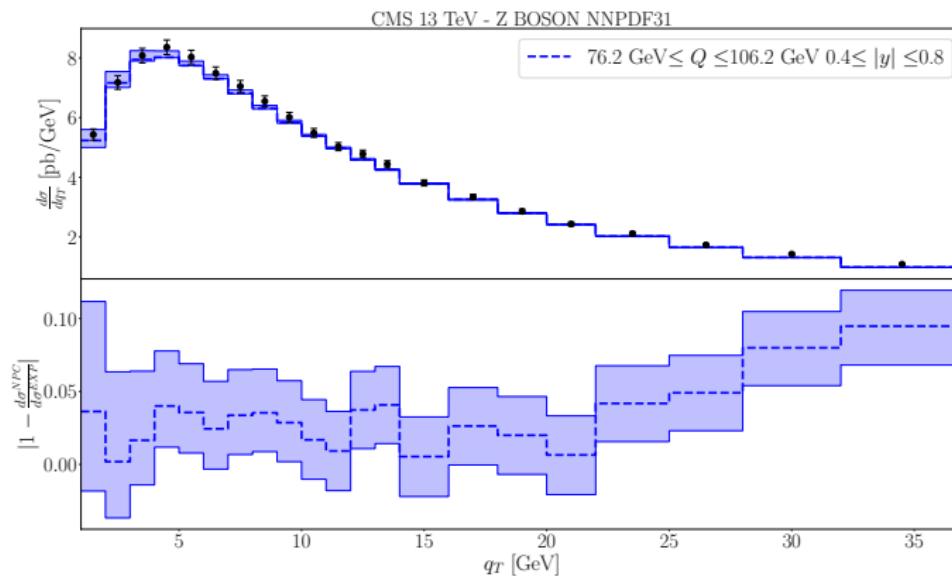
$$\mu^2 \frac{dF_{a \leftarrow h_A}(\alpha_s(\mu^2), b_T^2, x_A, \mu^2, \zeta)}{d\mu^2} = \frac{1}{2} \gamma_q(\alpha_s(\mu^2), \mu^2, \zeta) F_{a \leftarrow h_A}(\alpha_s(\mu^2), b_T^2, x_A, \mu^2, \zeta)$$

$$\zeta \frac{dF_{a \leftarrow h_A}(\alpha_s(\mu^2), b_T^2, x_A, \mu^2, \zeta)}{d\zeta} = -\mathcal{D}(\alpha_s(\mu^2), \mu^2, b_T^2) F_{a \leftarrow h_A}(\alpha_s(\mu^2), b_T^2, x_A, \mu^2, \zeta)$$

Y includes the q_T^2/Q^2 power corrections to the SCET factorization formula, dubbed by CSS
 Collins et al. Nucl. Phys. B 250 (1985), 199-224; Collins et al. Phys. Rev. D 94 (2016) no.3, 034014

TMD FACTORIZATION VS DATA

CMS collaboration JHEP 12 (2019), 061



The differential cross section is integrated in the intervals $66 \text{ GeV} \le Q \le 116 \text{ GeV}$ and $0.4 \le |y| \le 0.8$.

SOURCES OF POWER CORRECTIONS

So far in power corrections: Balitsky et al. JHEP **05** (2018), 150; Balitsky et al. JHEP **05** (2021), 046; Nefedov et al. Phys. Lett. B **790** (2019), 551-556; Ebert et al. 2112.07680 [hep-ph]; Luke et al. Phys. Rev. D **104** (2021) no.7, 076018, Beneke et al. JHEP **03** (2018), 001, Mulders et al. Nucl. Phys. B **667** (2003), 201-241...

- Corrections from the relevant kinematic variable:

$$\text{DY: } x_{A(B)} = \sqrt{\frac{Q^2 + \mathbf{q}_T^2}{s}} e^{\pm y}, \quad \text{SIDIS: } \mathbf{q}_T^2 = \frac{p_\perp^2}{z^2} \frac{1 + \gamma^2}{1 - \gamma^2 \frac{p_\perp^2}{z^2 Q^2}}$$

- Matching TMDPDF(FF) onto PDF(FF)
Vladimirov et al. Eur. Phys. J. C 78 (2018) no.10, 802

$$F_{a \leftarrow h_A}(\mathbf{b}_T, x) = \sum_{r, n} \left(\mathbf{b}_T^2 M^2 \right)^n C_{a \leftarrow r}^n \left(\ln \mathbf{b}_T^2 \mu^2, x \right) \otimes f_{r \leftarrow h_A}(x)$$

- Corrections to the TMD factorization included in the Y -term

Collins et al. Nucl. Phys. B 250 (1985), 199-224; Collins et al. Phys. Rev. D 94 (2016) no.3, 034014

MODIFIED FACTORIZATION FORMULA

$$\frac{d\sigma_{h_A h_B \rightarrow ll' X}}{dQ^2 dy d\mathbf{q}_T^2} = \sum_{a,b,c} \sigma_c^{\text{Born}} \int d^2 \mathbf{p}_{Ta} d^2 \mathbf{p}_{Tb} d^2 \mathbf{q}'_T \delta^{(2)}(\mathbf{q}_T - \mathbf{p}_{Ta} - \mathbf{p}_{Tb} - \mathbf{q}'_T)$$

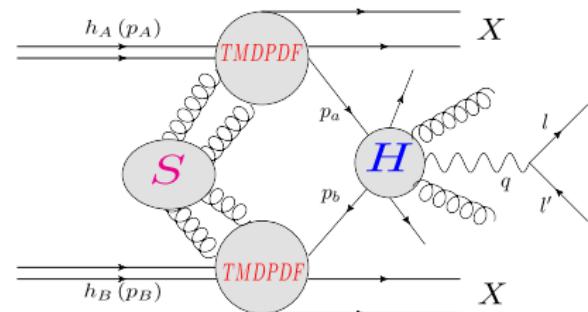
$$\int_{x_A}^1 \frac{dz_a}{z_a} \int_{x_B}^1 \frac{dz_b}{z_b} \theta \left(\frac{(z_a - x_A)(z_b - x_B)}{x_A x_B} - \frac{\mathbf{q}_T^{2\prime}}{Q^2 + \mathbf{q}_T^2} \right) \tilde{H}_{c \leftarrow a, \bar{c} \leftarrow b} \left(\alpha_s, Q^2, \frac{x_A}{z_a}, \frac{x_B}{z_b}, \mathbf{q}_T^{2\prime}, \mathbf{q}_T^2 \right)$$

$$F_{a \leftarrow h_A} \left(\alpha_s, z_a, \mathbf{p}_{Ta}^2 \right) F_{b \leftarrow h_B} \left(\alpha_s, z_b, \mathbf{p}_{Tb}^2 \right)$$

- The origin of θ is pure kinematic.
- The coefficient \tilde{H} is free of large logarithm contributions. All of them are absorbed by the TMDPDF.
- The TMD operators are unchanged and their evolution remains the same.

$$\zeta = \mu_F^2 = \mu_R^2 = \frac{(Q^2 + \mathbf{q}_T^2) z_a z_b}{x_A x_B}$$

$$x_{A(B)} = \sqrt{\frac{Q^2 + \mathbf{q}_T^2}{s}} e^{\pm y}$$



SUBTRACTION METHODS

Grazzini QCD@LHC 2019

NNLO methods

Broadly speaking there are two approaches that we can follow:

- Organise the calculation from scratch so as to cancel all the singularities

- Sector Decomposition (SD)

Binoth, Heinrich (2000,2004)
Anastasiou, Melnikov, Petriello (2004)

- antenna subtraction

Gehrmann, Glover (2005)
Somogyi, Trocsanyi, Del
Duca (2005, 2007)

- colourful subtraction

Czakon (2010,2011)

- subtraction+sector decomposition
(stripper, nested subtractions...)

Boughezal, Melnikov, Petriello (2011)
Caola, Melnikov, Rontsch (2017)

- Start from an inclusive NNLO calculation (sometimes obtained through resummation) and combine it with an NLO calculation for n+1 parton process

- q_T subtraction

Catani, MG (2007)

- N-jettiness method

Boughezal, Focke, Liu, Petriello (2015)
Tackmann et al. (2015)

- born projection (P2B) method

Cacciari, Dreyer, Karlberg, Salam, Zanderighi (2015)

PDF → TMDPDF

Search for an “ideal” subtraction method that can be applied as easily as CS or FKS at NLO is still subject of intense work

APPROACH

We use ideas from q_T -subtraction method: Catani, Grazzini et al. Nucl. Phys. B 596 (2001), 299-312; Catani, Grazzini et al. Phys. Lett. B 696 (2011), 207-213; Catani, Grazzini et. al. Phys. Rev. Lett. 98 (2007), 222002

$$d\sigma = \lim_{q_T \rightarrow 0} d\sigma + \left[d\sigma - \lim_{q_T \rightarrow 0} d\sigma \right]$$

- In our case the first term is well described by TMD factorization.
- It contains large logs (due to the expansion) that need to be resummed. TMD formalism is quite convenient for this task.
- The second term includes our power corrections as the difference at partonic level and fixed order.
- Typically the second term is computed using Monte-Carlo event generators. We provide an analytical computation at NLO+NLL.
- We modified the TMD factorization formula for DY to include this second term.

COMPUTATION AT NLO+NLL

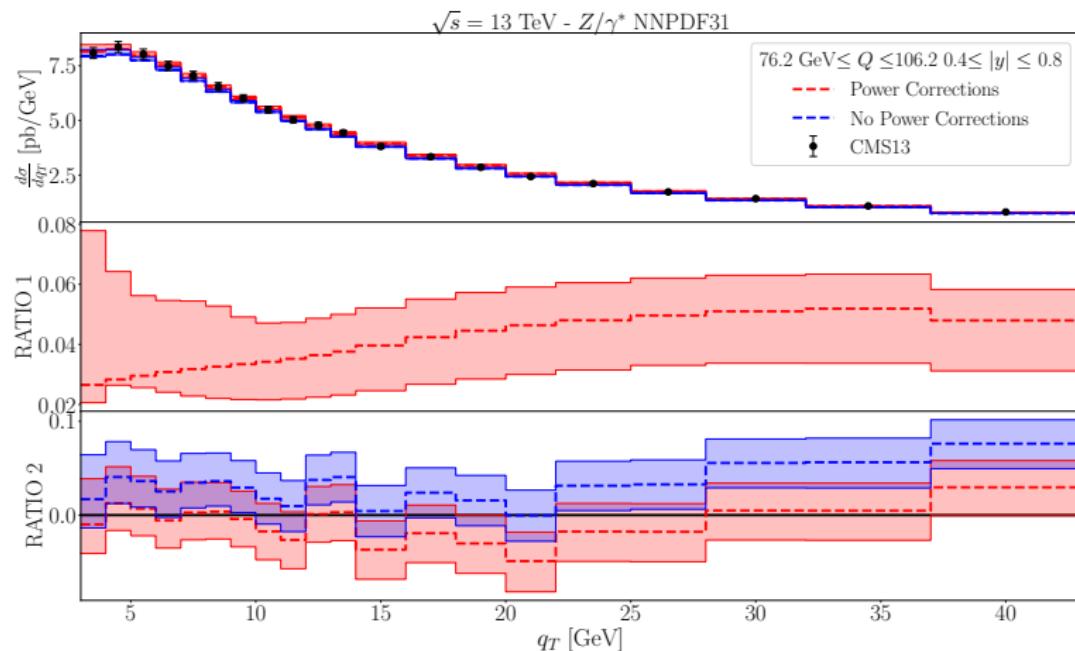
We compute

$$\frac{d\sigma_{h_A h_B \rightarrow ll' X}}{dQ^2 dy d\mathbf{q}_T^2} = \frac{d\sigma_{h_A h_B \rightarrow ll' X}^{\text{TMD}}}{dQ^2 dy d\mathbf{q}_T^2} + \left[\frac{d\sigma_{h_A h_B \rightarrow ll' X}}{dQ^2 dy d\mathbf{q}_T^2} - \frac{d\sigma_{h_A h_B \rightarrow ll' X}^{\text{TMD}}}{dQ^2 dy d\mathbf{q}_T^2} \right]$$

- The first term contains large logs due to the expansion in $\mathbf{q}_T^2 / (Q^2 + \mathbf{q}_T^2)$.
- We perform a NLO+NLL analytic computation of the second term.
- No need to regularize divergences using +-distributions
- The logarithmically enhanced contributions cancel out order by order in α_s .
- We seek for a modified factorization formula that at fixed order reproduces powers behaviour.

POWER CORRECTIONS VS LEADING POWER

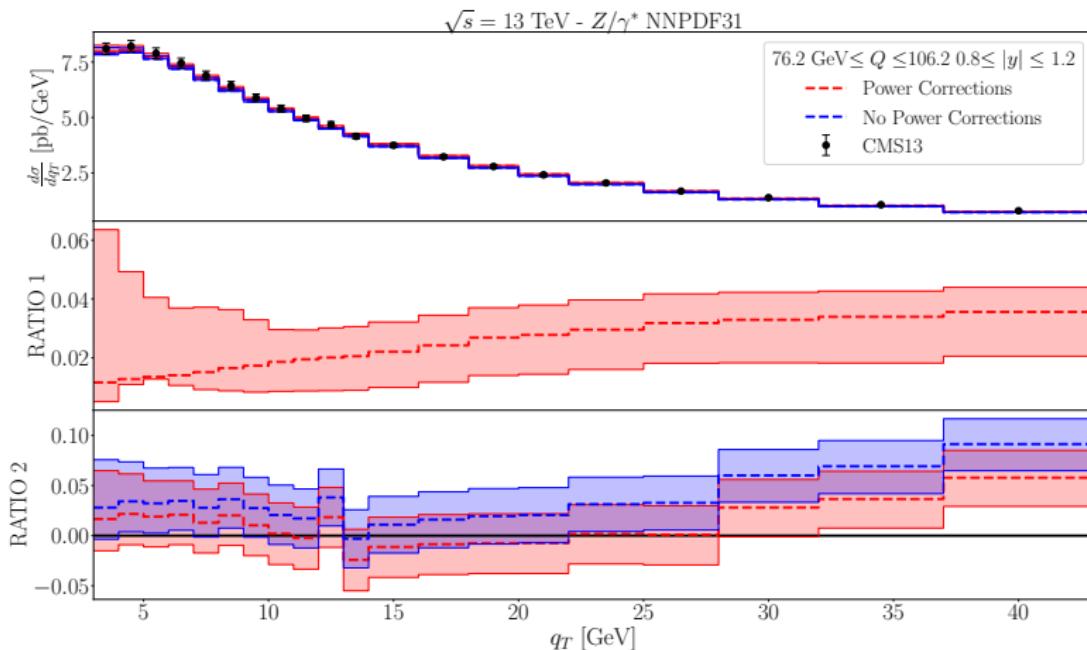
Preliminary CMS collaboration JHEP 12 (2019), 061



$\text{RATIO } 1 = 1 - d\sigma^{\text{NPC}}/d\sigma^{\text{PC}}$, $\text{RATIO } 2 = 1 - d\sigma^{\text{PC(NPC)}}/d\sigma^{\text{DATA}}$. Bigger than electroweak corrections
Grazzini et al. Phys. Rev. Lett. 128 (2022) no.1, 012002; Sborlini et al. JHEP 08 (2018), 165

POWER CORRECTIONS VS LEADING POWER

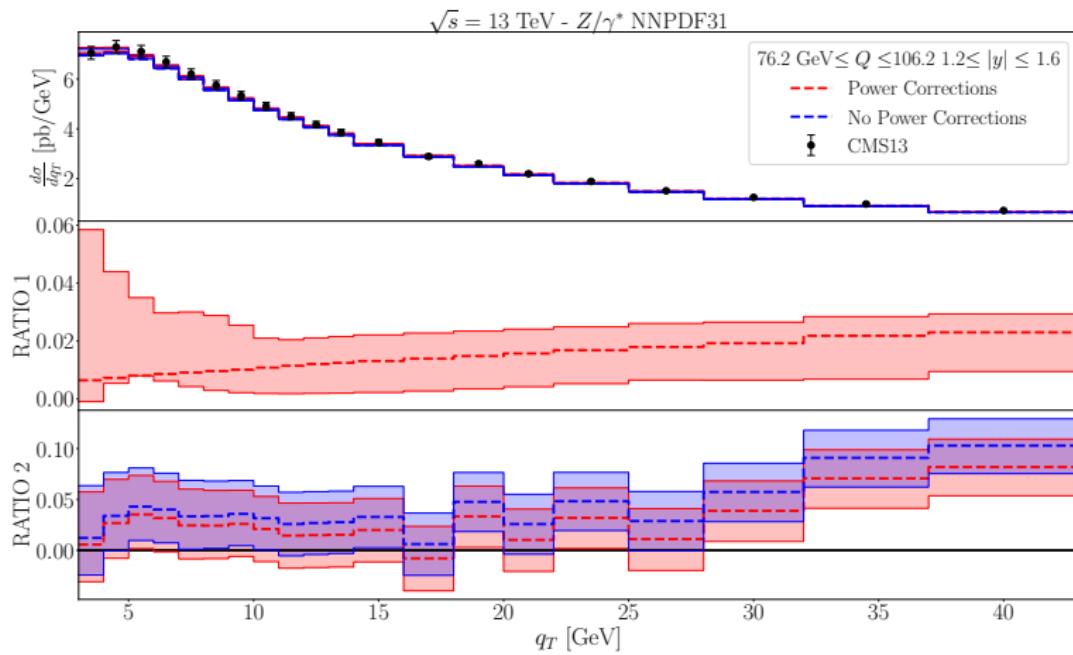
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SUMMARY & OUTLOOK

SUMMARY

- At small q_T^2/Q^2 our factorization formula reproduces TMD factorization.
 - At $|q_T| = Q \cdot 0.10$ we start to appreciate the effects of power corrections.
 - The power corrections increase the cross section at large q_T , making it closer the experimental data.
 - Electroweak corrections are subleading compared to power corrections [Grazzini et al. Phys. Rev. Lett. 128 \(2022\) no.1, 012002; Sborlini et al. JHEP 08 \(2018\), 165](#)

OUTLOOK

- Improvement of the code for integration in \mathbf{p}_T of the TMDPDF.
 - Extension to e^+e^- to jets/hadrons.
 - Study of polarized processes.
 - New extraction of TMDPDFs.
 - Inclusion of power suppressed terms in the matching of TMDs onto PDFs.

INTRODUCTION
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POWER CORRECTIONS
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SUMMARY & OUTLOOK
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THANK YOU FOR YOUR ATTENTION

INTRODUCTION
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POWER CORRECTIONS
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SUMMARY & OUTLOOK
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Backup

LARGE LOGS

- Momentum Space \mathbf{q}_T

$$\frac{d\sigma}{dQ^2 dy d\mathbf{q}_T^2} \sim c_1^{[1]} \frac{\alpha_s}{\mathbf{q}_T^2} \log \frac{Q^2}{\mathbf{q}_T^2} + \frac{\alpha_s^2}{\mathbf{q}_T^2} \left(c_1^{[2]} \log \frac{Q^2}{\mathbf{q}_T^2} + c_2^{[2]} \log^2 \frac{Q^2}{\mathbf{q}_T^2} + c_3^{[2]} \log^3 \frac{Q^2}{\mathbf{q}_T^2} \right) + \dots$$

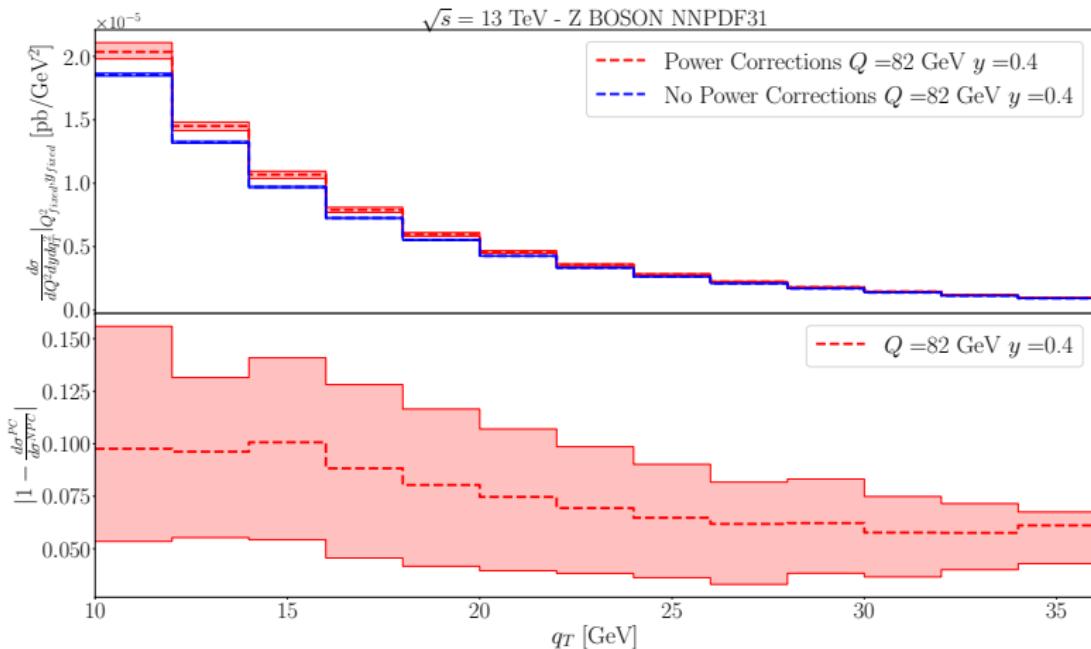
- Impact parameter space \mathbf{b}_T

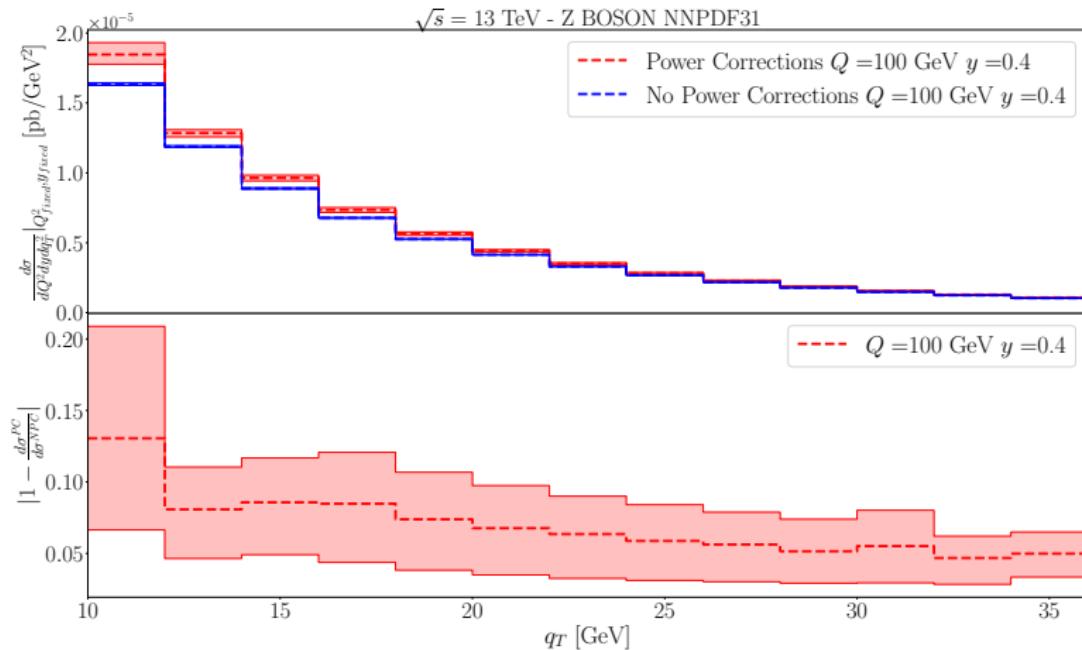
$$\begin{aligned} \frac{d\sigma}{dQ^2 dy d\mathbf{b}_T^2} &\sim \alpha_s \left(c_0^{[1]} \log \frac{Q^2 \mathbf{b}_T^2}{4e^{-2\gamma_E}} + c_1^{[1]} \log^2 \frac{Q^2 \mathbf{b}_T^2}{4e^{-2\gamma_E}} \right) + \\ &\alpha_s^2 \left(c_0^{[2]} \log \frac{Q^2 \mathbf{b}_T^2}{4e^{-2\gamma_E}} + c_1^{[2]} \log^2 \frac{Q^2 \mathbf{b}_T^2}{4e^{-2\gamma_E}} + c_2^{[2]} \log^3 \frac{Q^2 \mathbf{b}_T^2}{4e^{-2\gamma_E}} + c_3^{[2]} \log^4 \frac{Q^2 \mathbf{b}_T^2}{4e^{-2\gamma_E}} \right) + \dots \end{aligned}$$

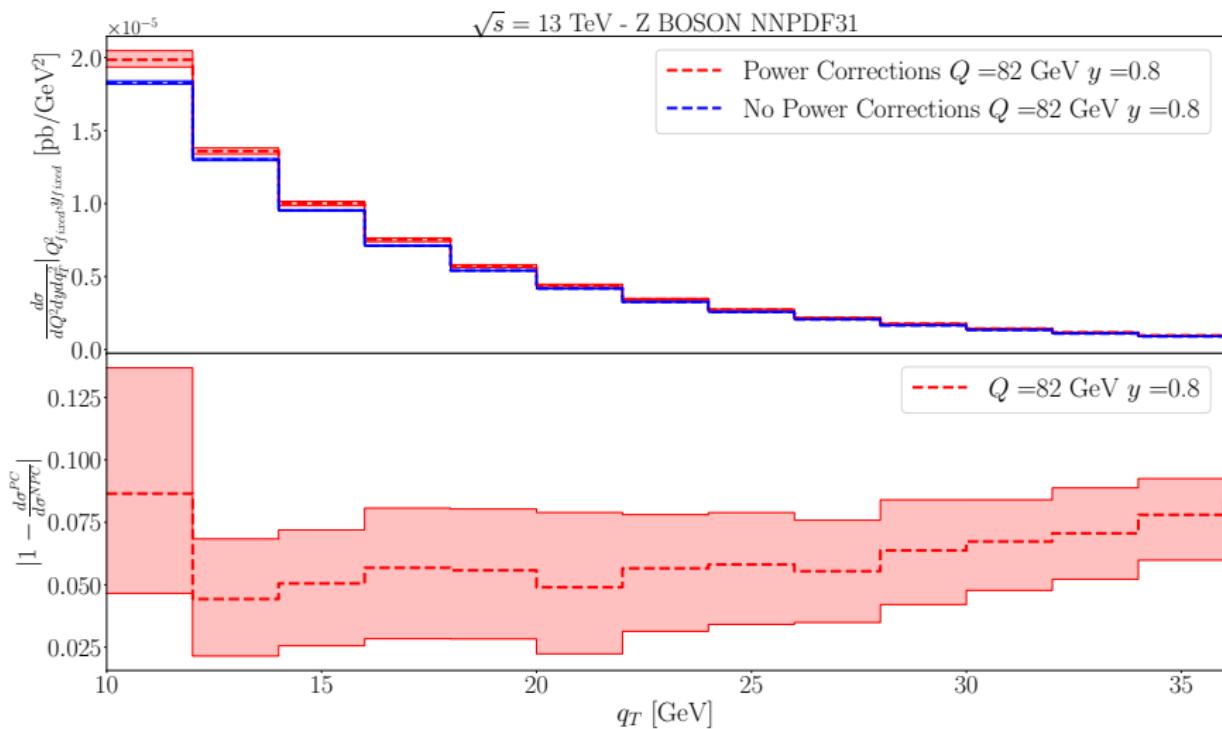
SMALL \mathbf{q}_T EXPANSION AT NLO.

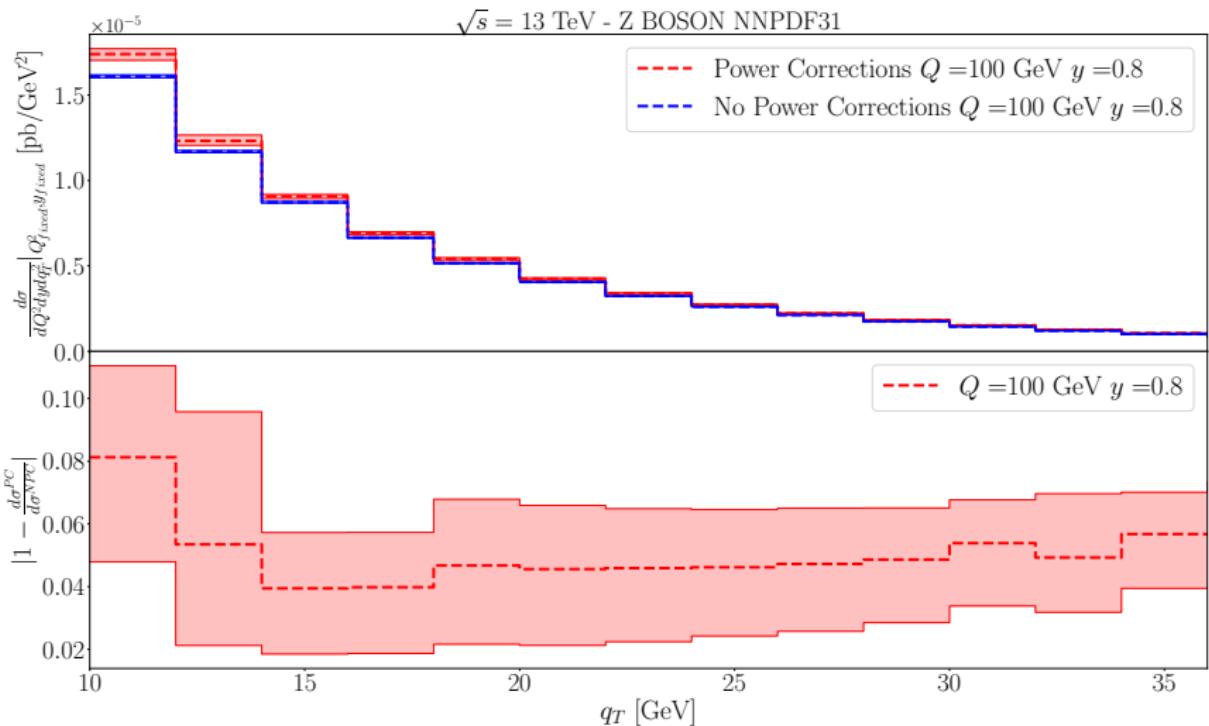
Using the methods presented in Bacchetta et al. JHEP 08 (2008), 023; Soper et al. Phys. Rev. D 54 (1996), 1919-1935

$$\delta \left((\rho_a - \rho_b - q)^2 \right) = \\ \frac{1}{Q^2 + \mathbf{q}_T^2} \left[\frac{1}{(1 - x_a)_+} \delta(1 - x_b) + \frac{1}{(1 - x_b)_+} \delta(1 - x_a) - \delta(1 - x_a) \delta(1 - x_b) \ln \frac{\mathbf{q}_T^2}{Q^2 + \mathbf{q}_T^2} \right] + \mathcal{O} \left(\frac{\mathbf{q}_T^2}{Q^2} \right)$$

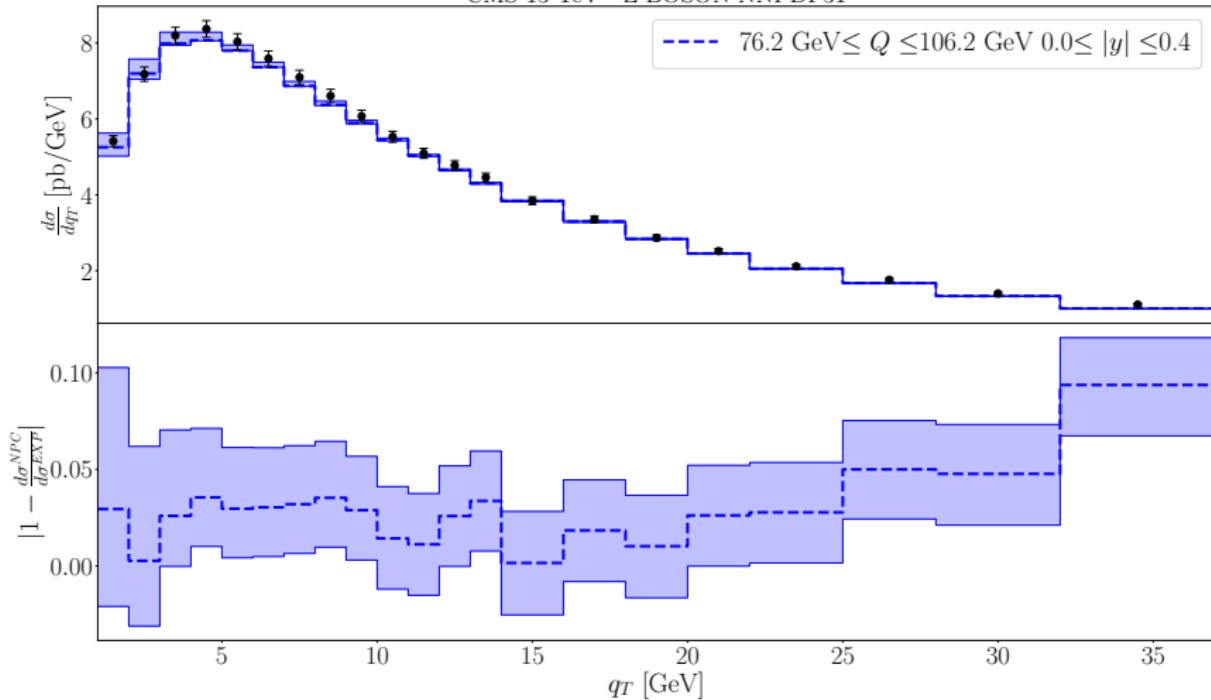




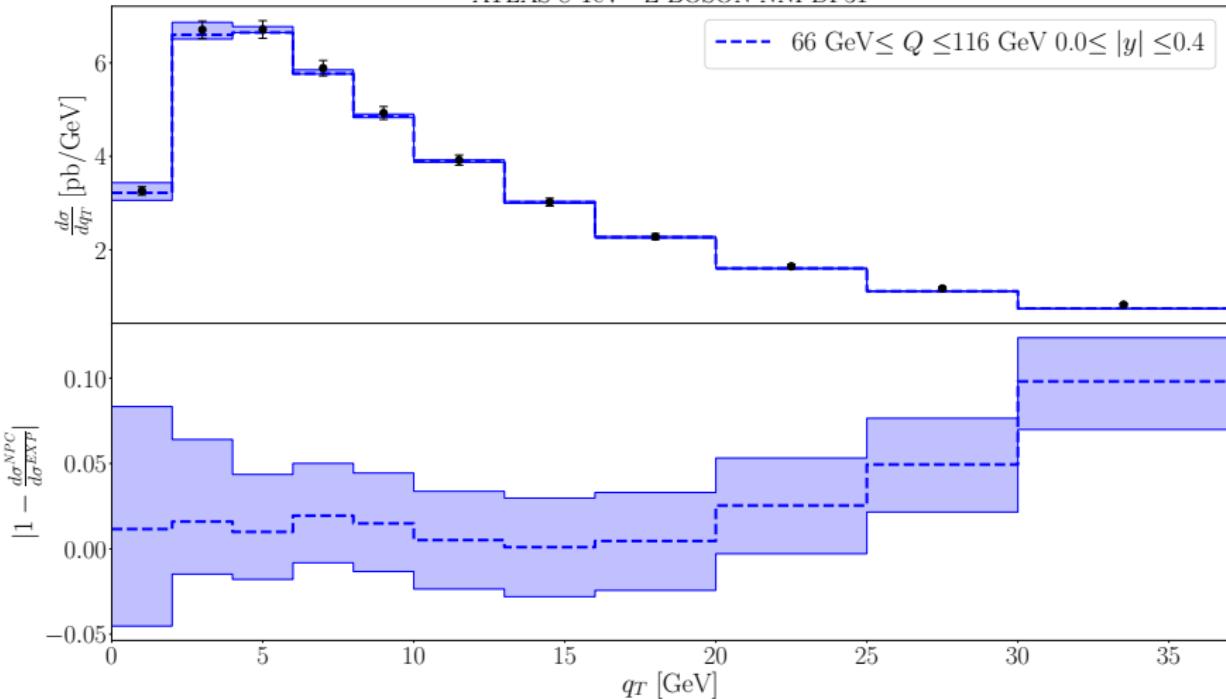




CMS 13 TeV - Z BOSON NNPDF31



ATLAS 8 TeV - Z BOSON NNPDF31



ATLAS 8 TeV - Z BOSON NNPDF31

