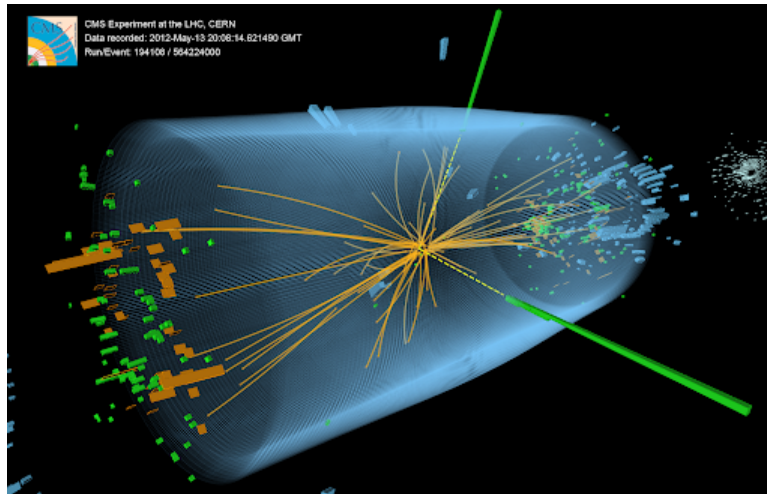


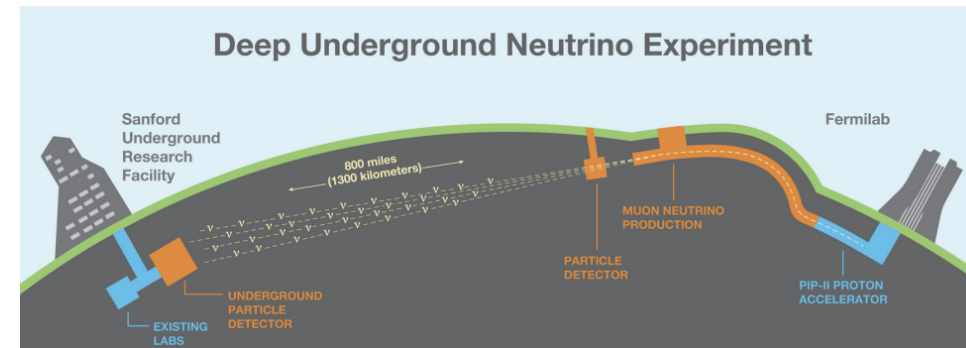
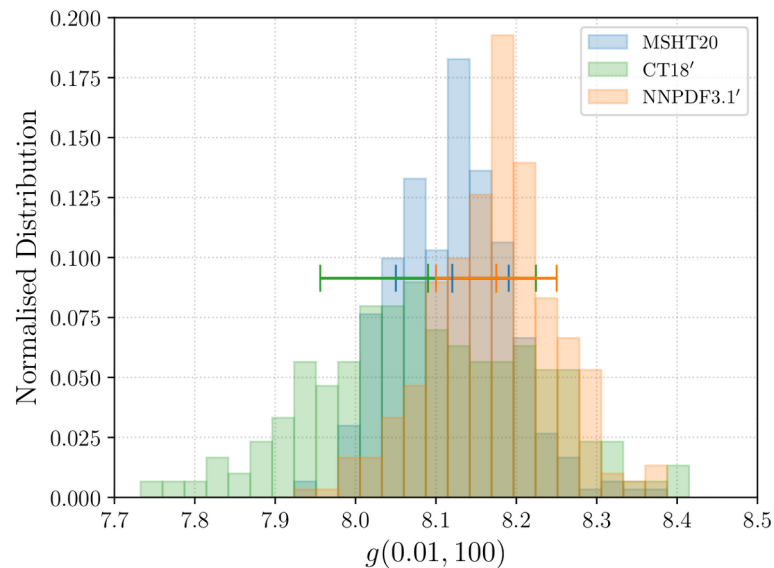
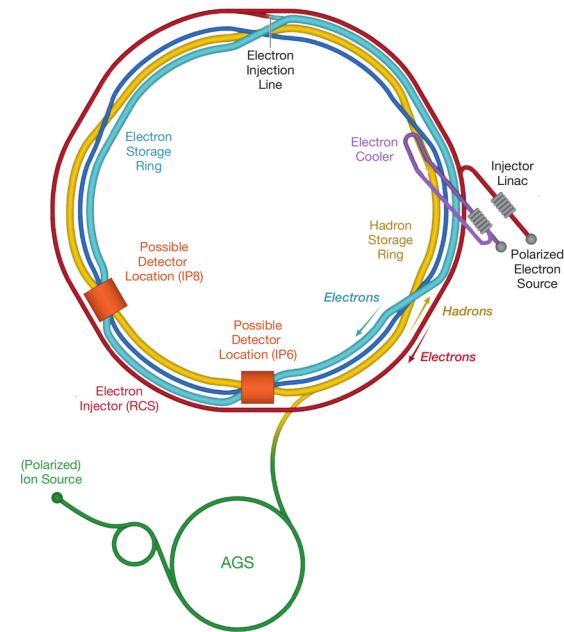
Frontiers in precision for global PDF analyses

Tim Hobbs – Fermilab, IIT

2nd August 2022



see 'roundtable':
High Precision
QCD Frontier



 **Fermilab**

ILLINOIS INSTITUTE
OF TECHNOLOGY 

this talk: PDFs central to **2 core needs in fundamental QCD**

1: precision BSM searches limited by (incomplete) proton structure info

- many standard-candle HEP measurements PDF-limited
- taming PDF dependence: knowledge of hard-to-access phase-space regions
- PDF studies vital to NP QCD (**confinement!**), mapping hadron structure

2: must interrogate (p)QCD to achieve higher theoretical accuracy

- stability of PDF extractions partly depends on pQCD formalism
- tests of, e.g., QCD factorization, (systematic) knowledge of limits needed

highlight through:

i current status of PDFs; ii experimental opportunities (EIC)

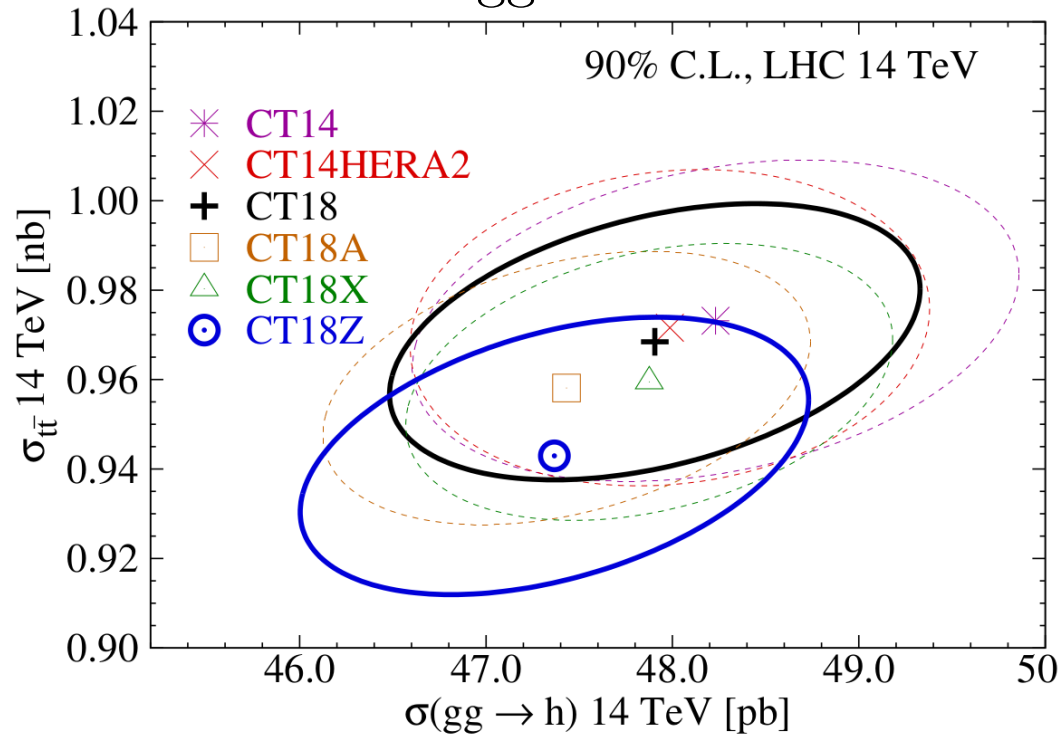
iii conclusion(s)

SM theory predictions from global analyses

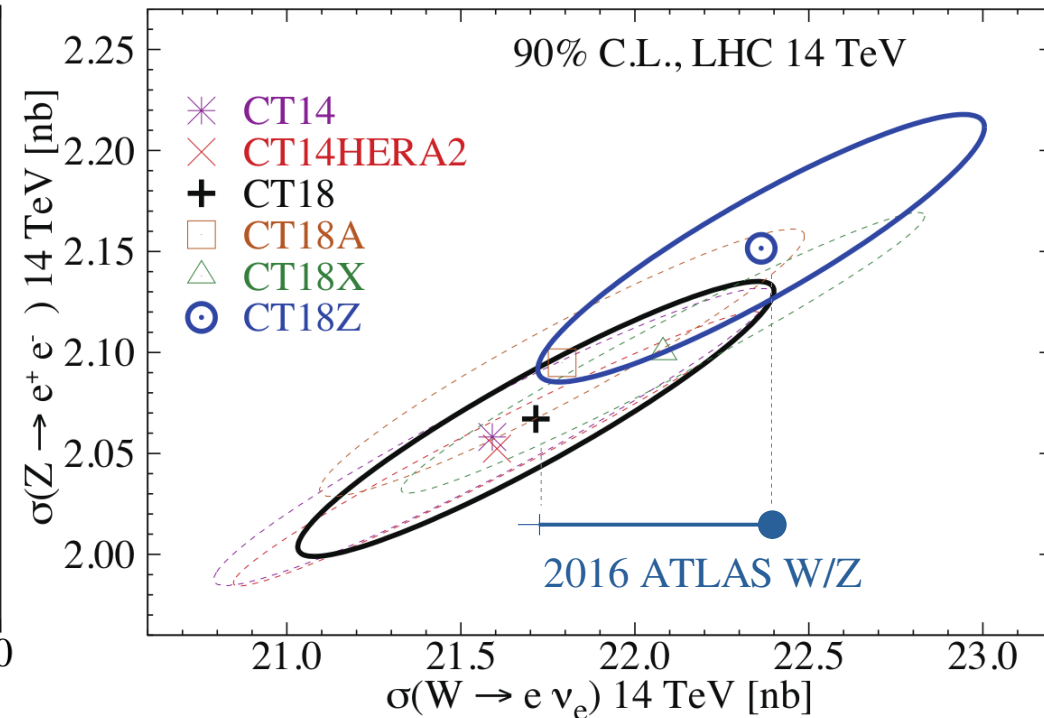
- from NNLO analyses, state-of-the-art predictions for fundamental LHC observables $\rightarrow$ *e.g.*, **total cross sections at 14 TeV**

CT18 NNLO, PRD 103 (2021) 1

Higgs and $t\bar{t}$



W and Z



Higgs, NNLO QCD: iHixs v1.3

$\mu_R = \mu_F = m_t; m_{W,Z}; m_H$

NNLO QCD: Vrap v0.9

$t\bar{t}$, NNLO+NNLL: Top++ v2.0

- significant PDF-driven uncertainties; also, systematic effects: W cross sections sensitive to inclusion of 2016 7 TeV ATLAS inclusive W/Z data

i high-interest SM quantities are precision-limited by PDFs

→ these include σ_H , $\sin^2 \theta_W$, m_W , ...

ATLAS, 1701.07240

for example:

Channel	$m_{W^+} - m_{W^-}$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$W \rightarrow e\nu$	-29.7	17.5	0.0	4.9	0.9	5.4	0.5	0.0	24.1	30.7
$W \rightarrow \mu\nu$	-28.6	16.3	11.7	0.0	1.1	5.0	0.4	0.0	26.0	33.2
Combined	-29.2	12.8	3.3	4.1	1.0	4.5	0.4	0.0	23.9	28.0

→ the PDF uncertainty can be a/the dominant uncertainty!

→ frontier efforts at the HL-LHC aim for (sub)percent precision

→ **large cross-cutting effort spanning theory/expt to improve**

- heightened theory accuracy (HO, power corrections)
- novel measurements (EIC, LHC, vA)
- generator development

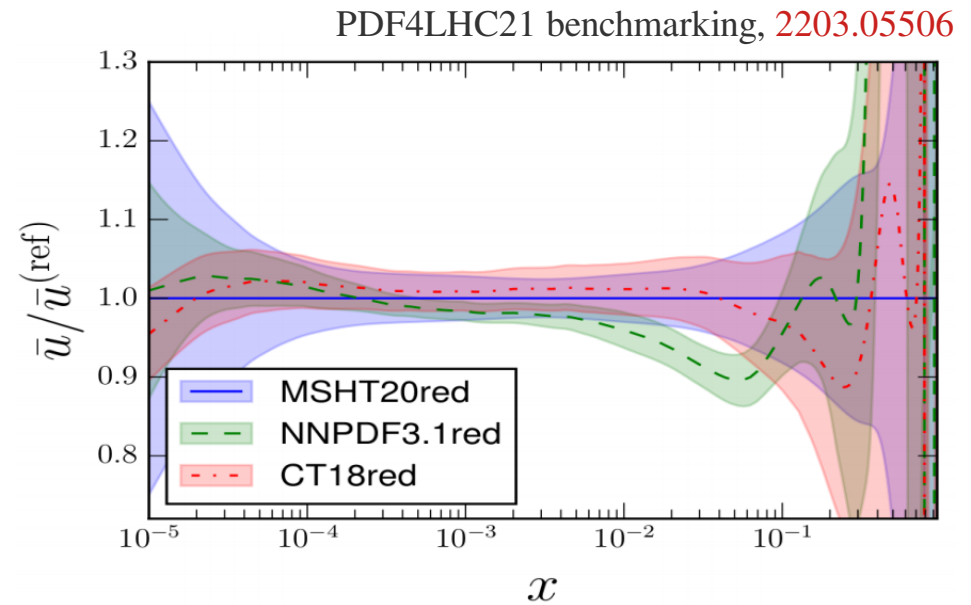
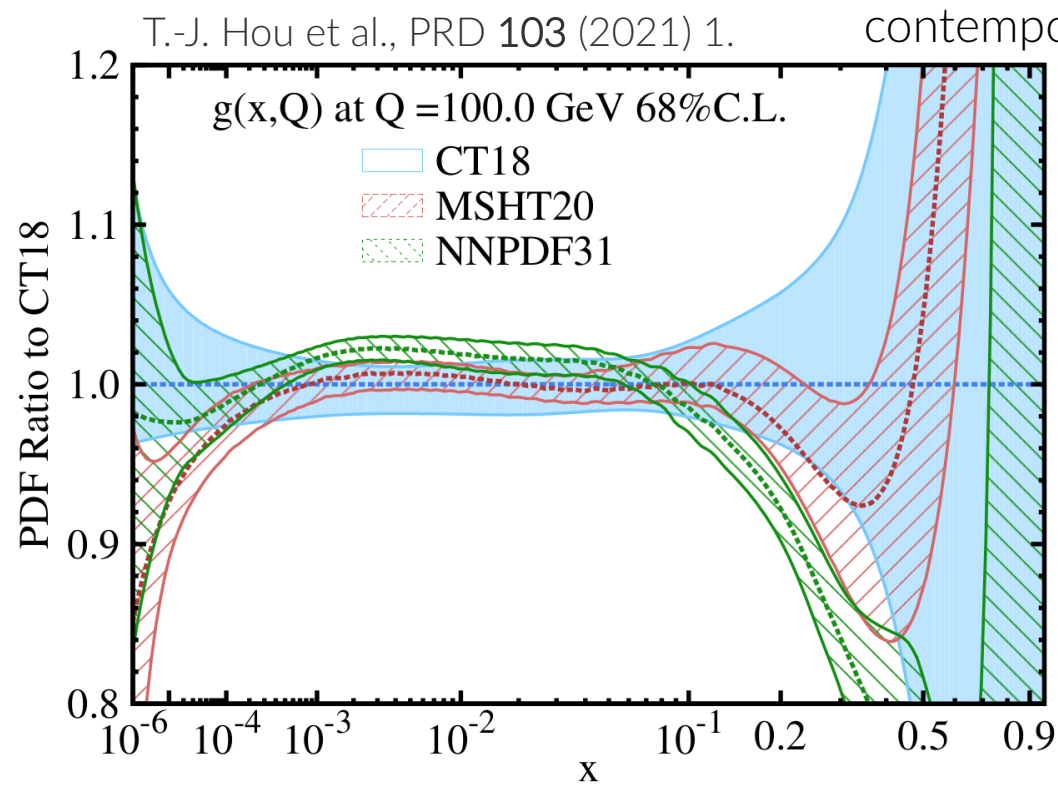
Snowmass21, Campbell et al.: 2203.11110

PDFs critical to next-generation precision

Snowmass21, Amoroso et al.: [2203.13923](#)

→ driven by marriage of latest theory, high-energy hadronic data

$$\sigma(AB \rightarrow W/Z + X) = \sum_n \alpha_s^n \sum_{a,b} \int dx_a dx_b f_{a/A}(x_a, \mu^2) \hat{\sigma}_{ab \rightarrow W/Z+X}^{(n)}(\hat{s}, \mu^2) f_{b/B}(x_b, \mu^2)$$



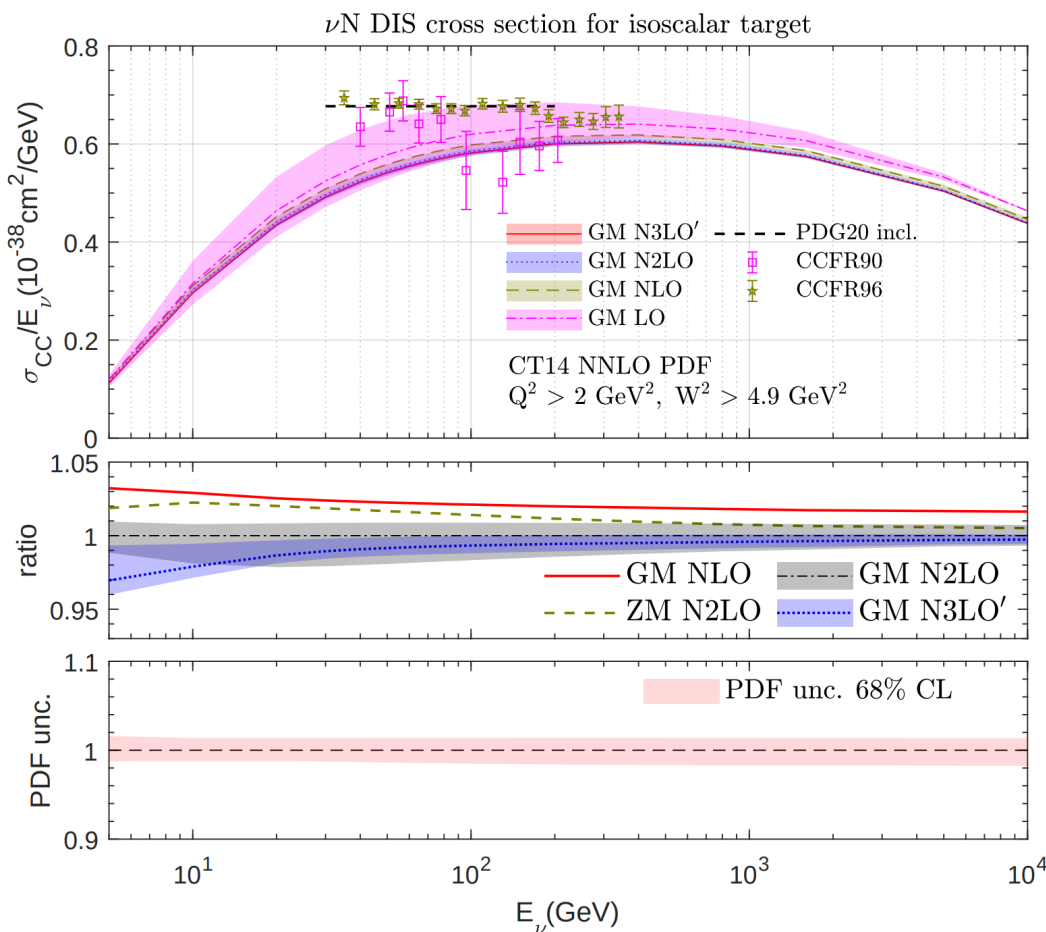
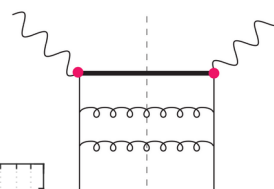
- periodic benchmarking (PDF4LHC21) valuable to cross-check treatment of data

→ seek methodological independence in identifying data-driven PDF features

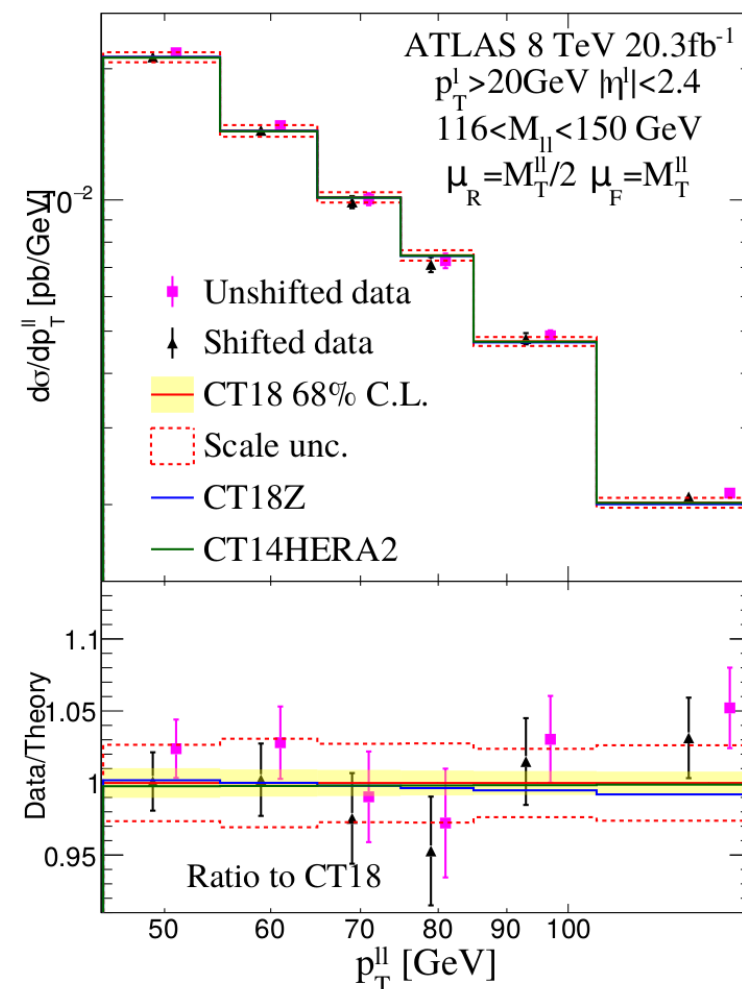
- current/future analyses involve interplay between pQCD & other dynamics
- NNLO+ necessary to stabilize scale uncertainties; especially over wide scales

charge-current DIS

Gao, TJH, Nadolsky, Sun, Yuan: PRD105 (2022) 1, L011503



NNLO scale variations at LHC



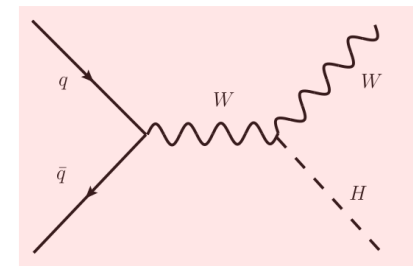
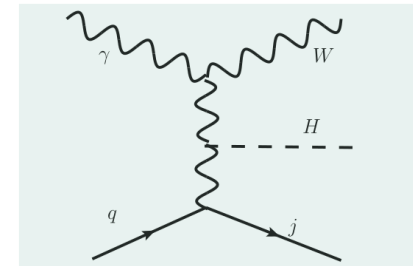
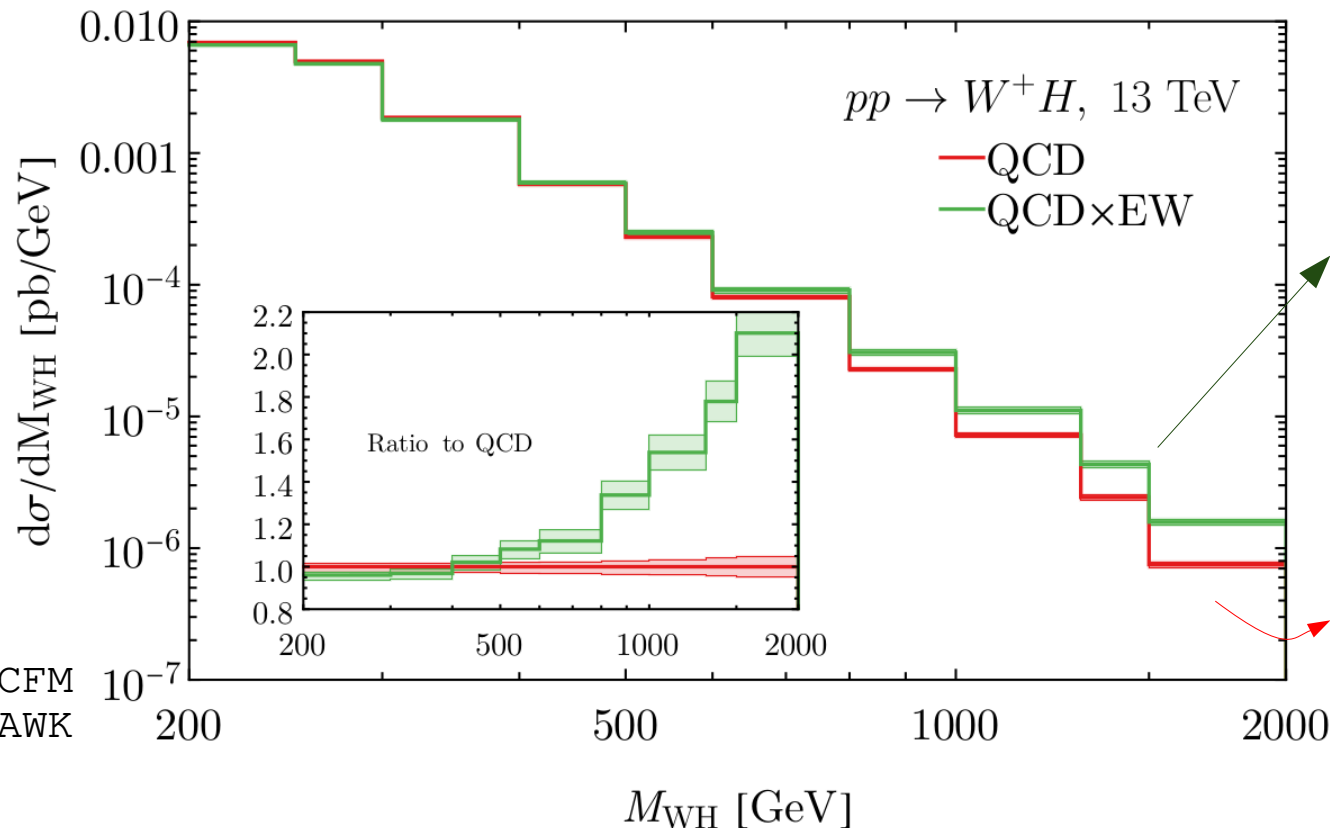
→ needed for DUNE, FASERν, EIC

electroweak (EW) corrections also vital

- at $\mathcal{O}(\alpha_s^2)$ accuracy, EW corrections and explicit $\gamma(x, \mu^2)$ needed

Xie, TJH, Hou, Schmidt, Yan, Yuan: PRD105 (2022) 5, 054006

- important for high-energy LHC processes: *e.g.*, 13 TeV W+H production



- TeV-scale NLO EW corrections dominated (60%) by single-photon (PDF) contributions

→ requires **delicate** treatment along with QCD perturbative effects

i necessary for electroweak precision: photon PDF

- at $\mathcal{O}(\alpha_s^2)$ accuracy, EW corrections and explicit $\gamma(x, \mu^2)$ needed

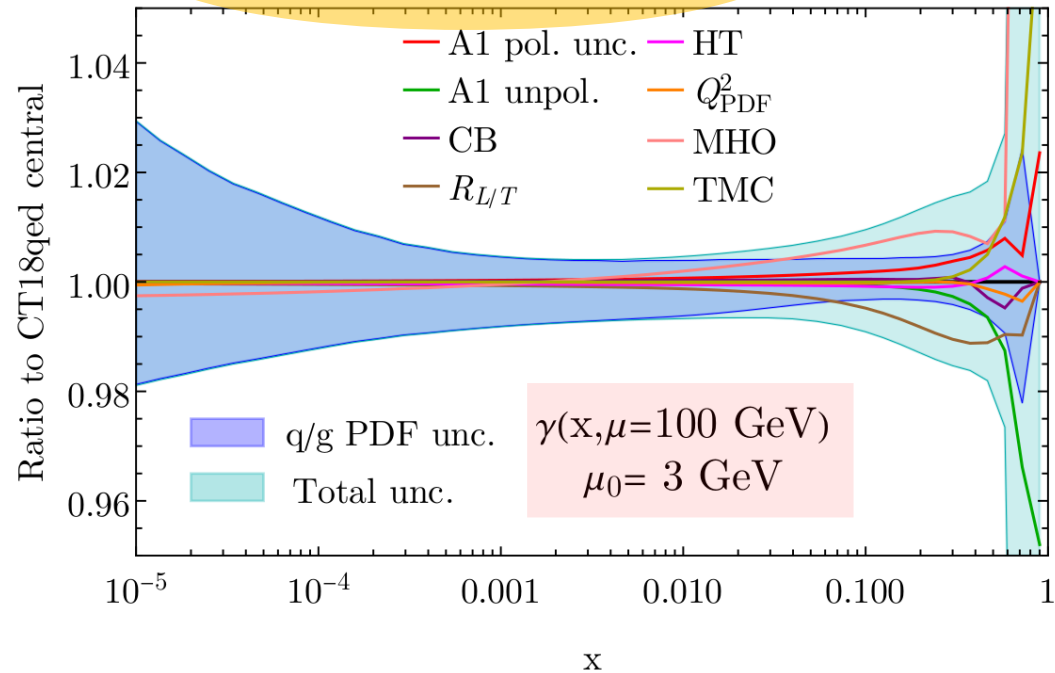
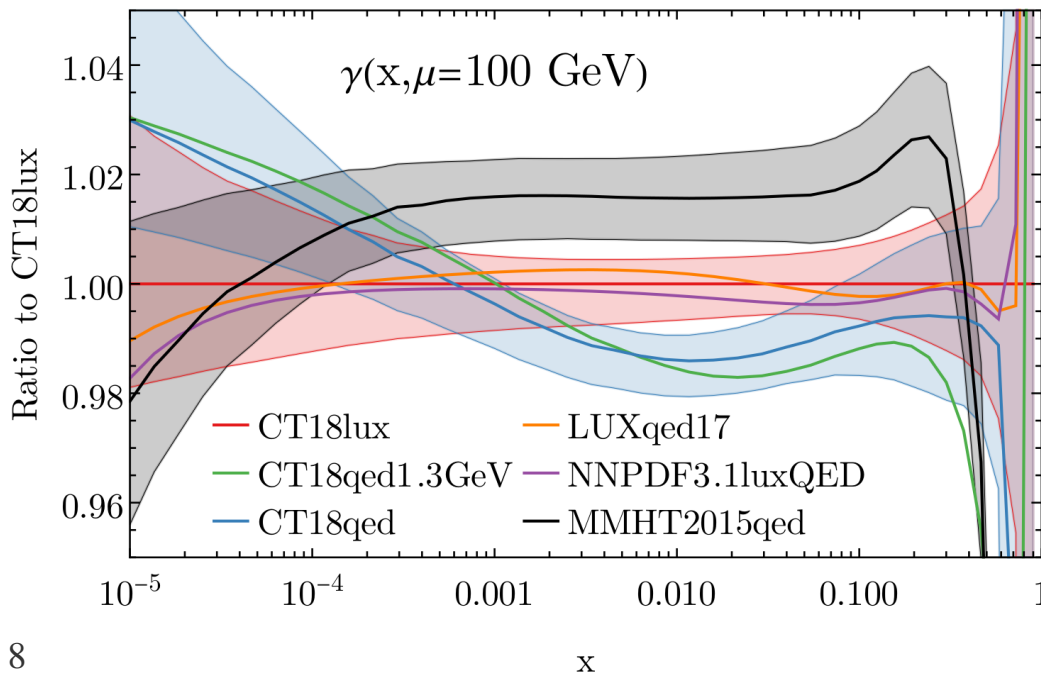
Xie, TJH, Hou, Schmidt, Yan, Yuan: PRD105 (2022) 5, 054006

- following CT14QED, CT18QED now interfaces LUX formalism

$$x\gamma(x, \mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_x^1 \frac{z}{z} \left\{ \int_{\frac{x^2 m_p^2}{1-z}}^{\frac{\mu^2}{1-z}} \frac{Q^2}{Q^2} \alpha_{\text{ph}}^2(-Q^2) \left[\left(zp_{\gamma q}(z) + \frac{2x^2 m_p^2}{Q^2} \right) F_2(x/z, Q^2) - z^2 F_L(x/z, Q^2) \right] - \alpha^2(\mu^2) z^2 F_2(x/z, \mu^2) \right\} + \mathcal{O}(\alpha^2, \alpha\alpha_s)$$

- depends on nonperturbative inputs [kinematical cuts alone can't avoid this]

[e.g., large- x physics...]

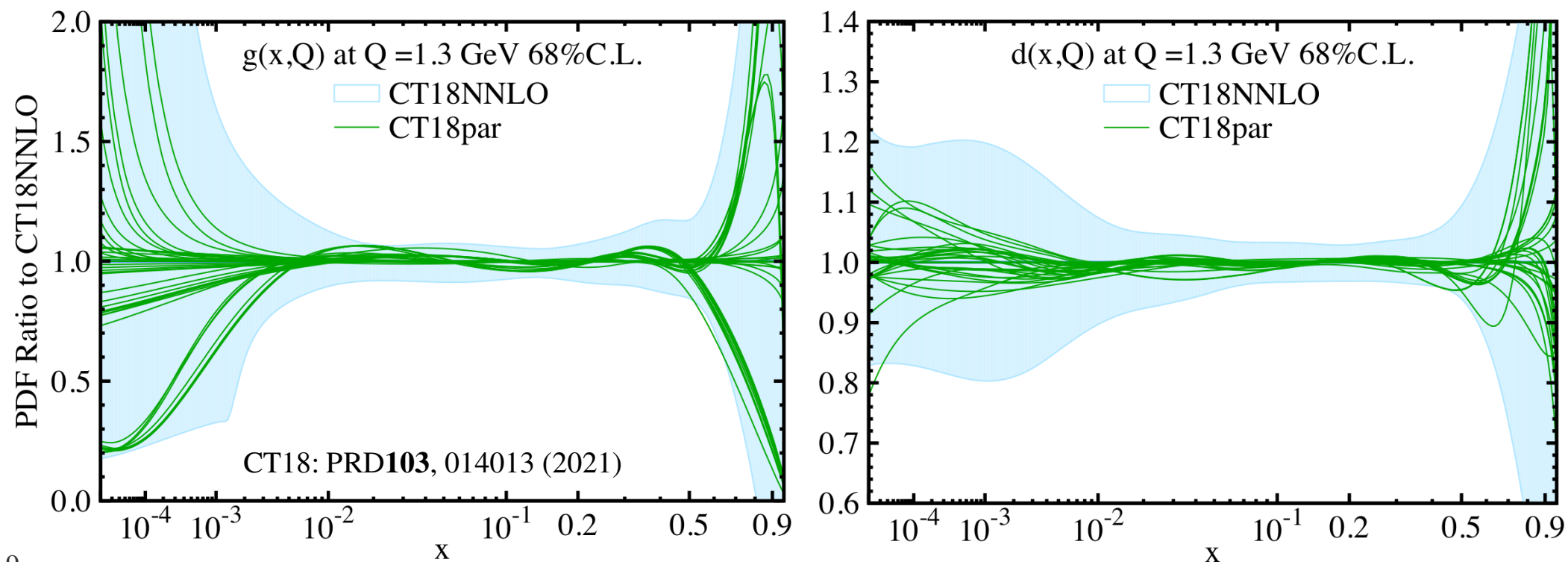


i

parametrization uncertainty: nonperturbative fitting forms

- initial PDFs still not generally calculable through rigorous QCD at $Q = Q_0 = m_c$ (to the needed precision...)
 - subject to complex nonperturbative dynamics
 - practice agnosticism w.r.t. initial parametrization
 - (some guidance from QCD, QCD-inspired models)
 - explore model uncertainty with many forms

parametrization uncertainties largest in extrapolated regions



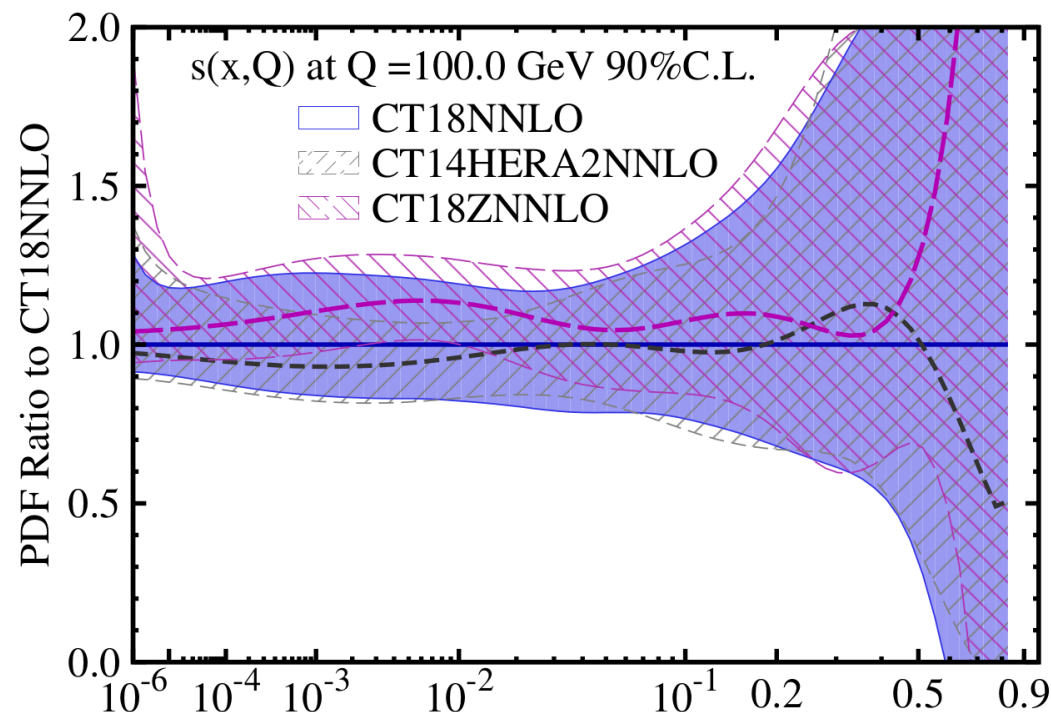
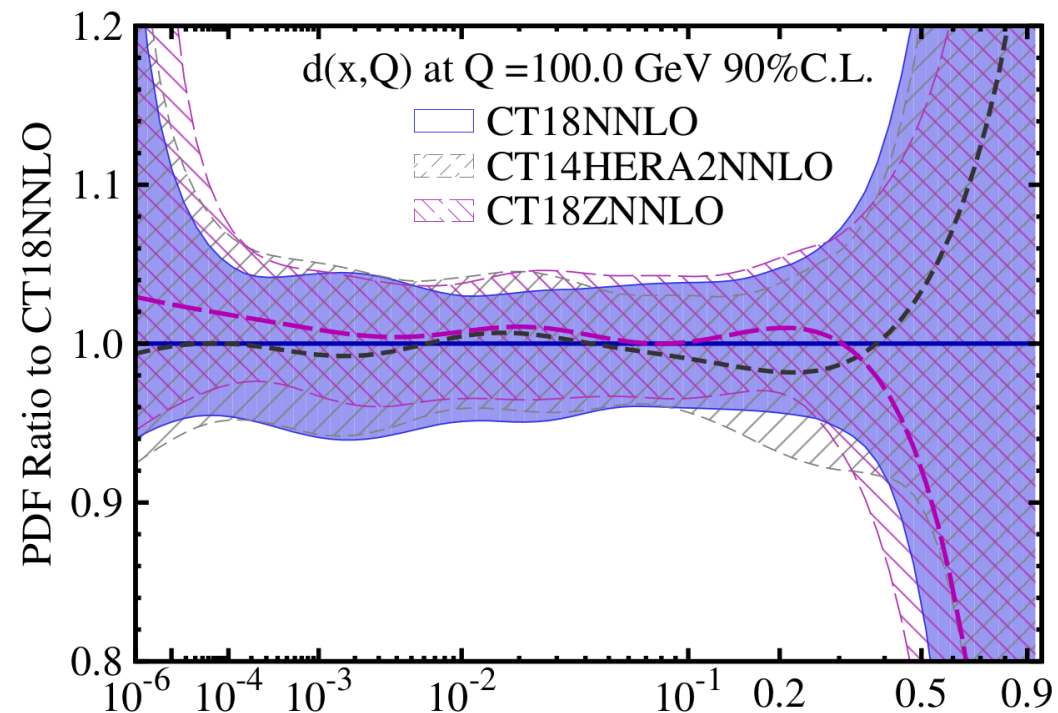
high- x PDFs remain dominated by large uncertainties

- PDF (Hessian) uncertainties enlarge dramatically in high- x limit

→ limited data

→ extrapolation

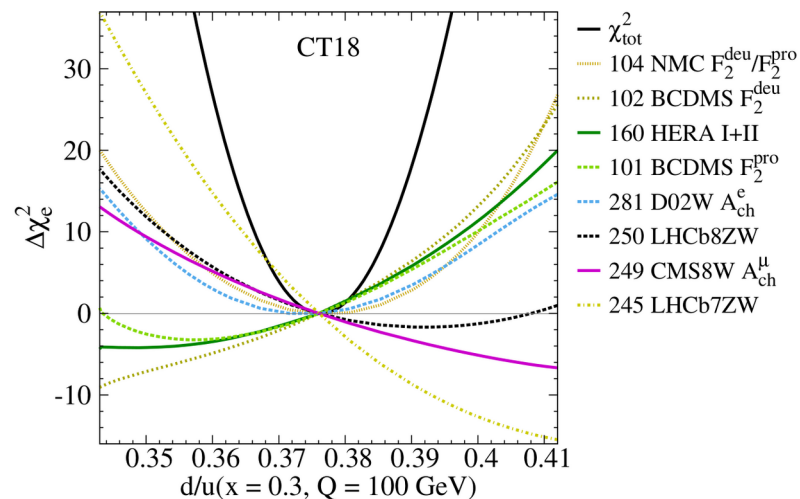
→ data tensions



- competing pulls of fitted data at high- x also restrict precision; *e.g.*,

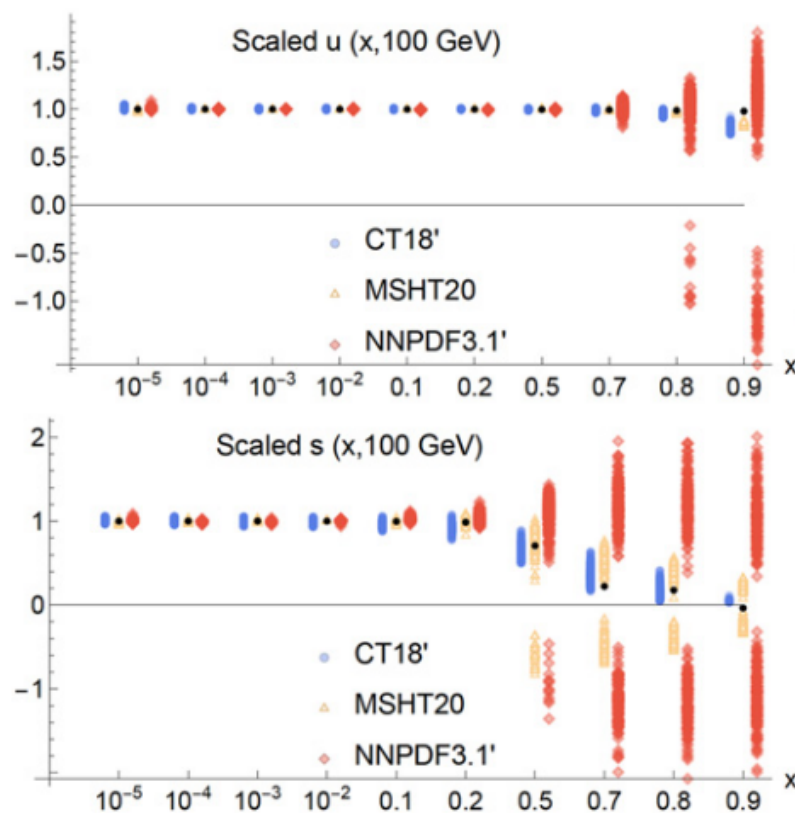
→ BCDMS, F_2^d

→ LHCb, W/Z 7 TeV

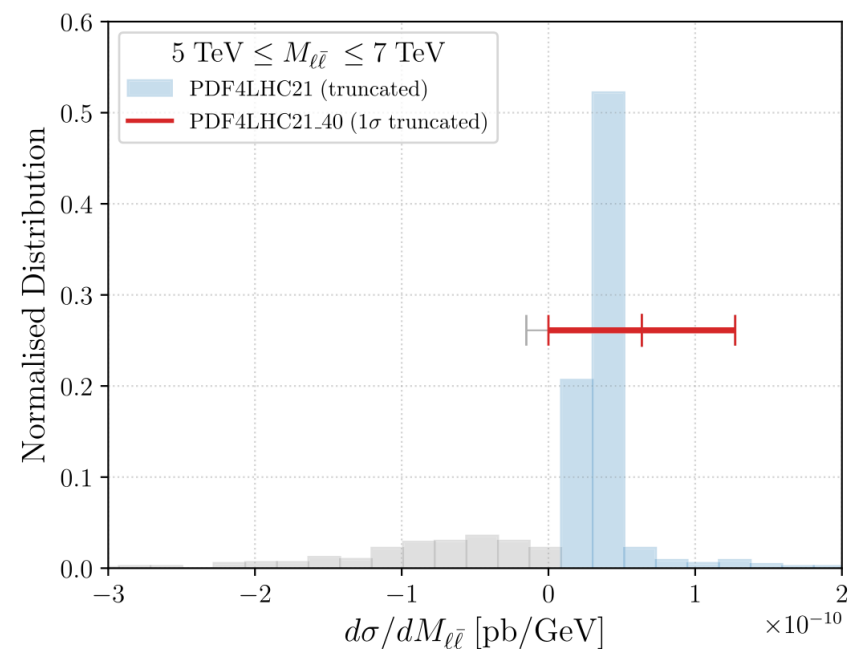


- MC sampling of high- x PDFs can sometimes produce irregularities

→ *e.g.*, positive-definiteness not always guaranteed for $x \rightarrow 1$



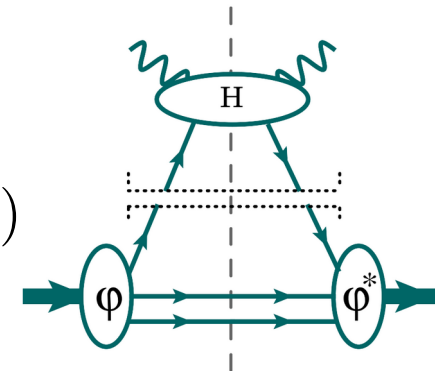
→ can produce subtle but non-negligible phenomenological consequences:



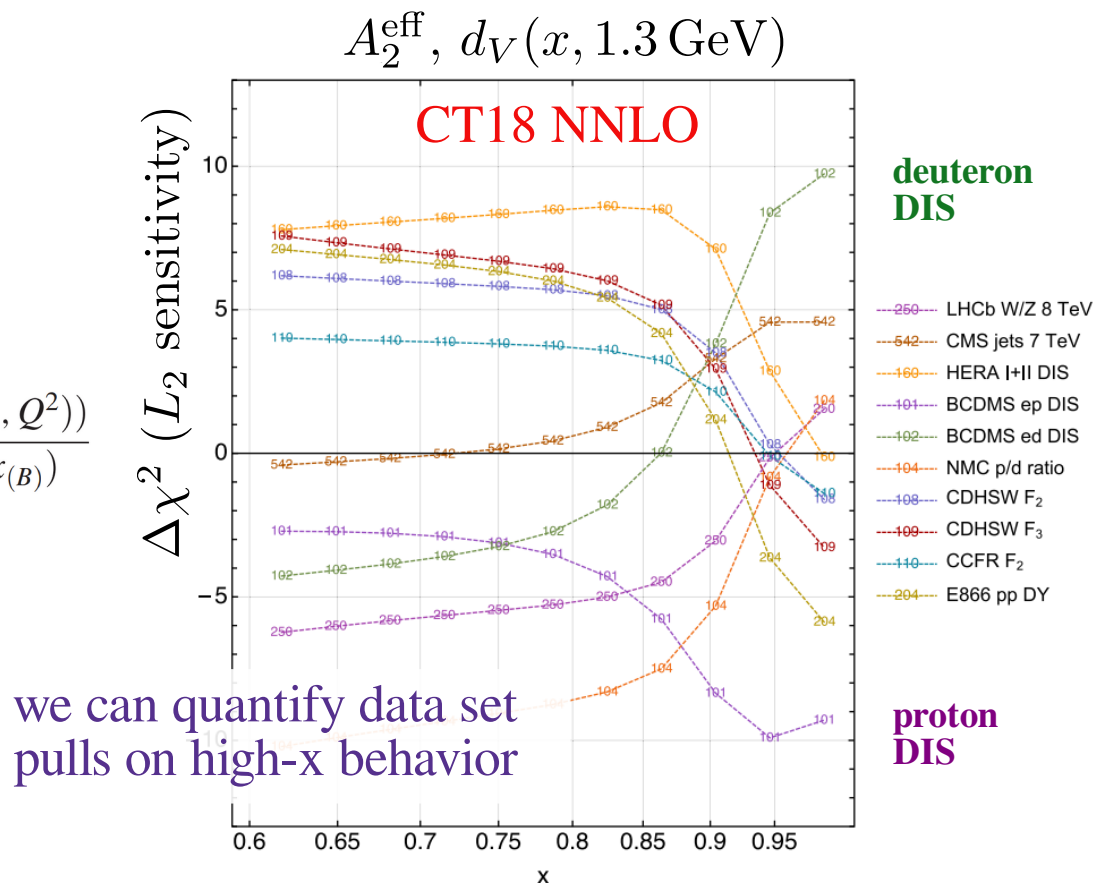
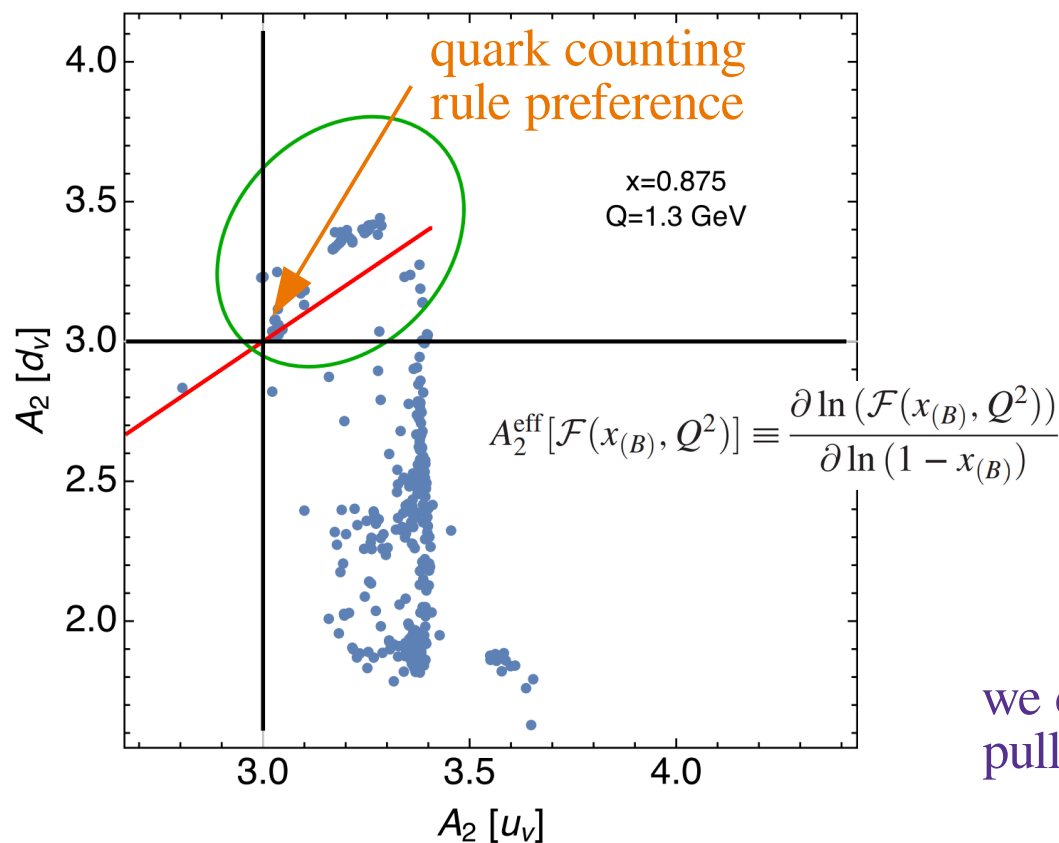
- strong need for high- x sensitive data: JLab12 [24]; (HL-)EIC; FASER ν

extracting high- x dependence in PDF fits

- high- x PDFs, ratios [e.g., d/u] connected to details of proton WF
- behavior at $x \rightarrow 1$ an important nonpert. discriminator
- CT18, parametrize $f_{a/A}(x, Q_0^2) = x^{A_{1,a}}(1-x)^{A_{2,a}} \times \Phi_a(x)$



Courtoy and Nadolsky, PRD103, 054029 (2021)

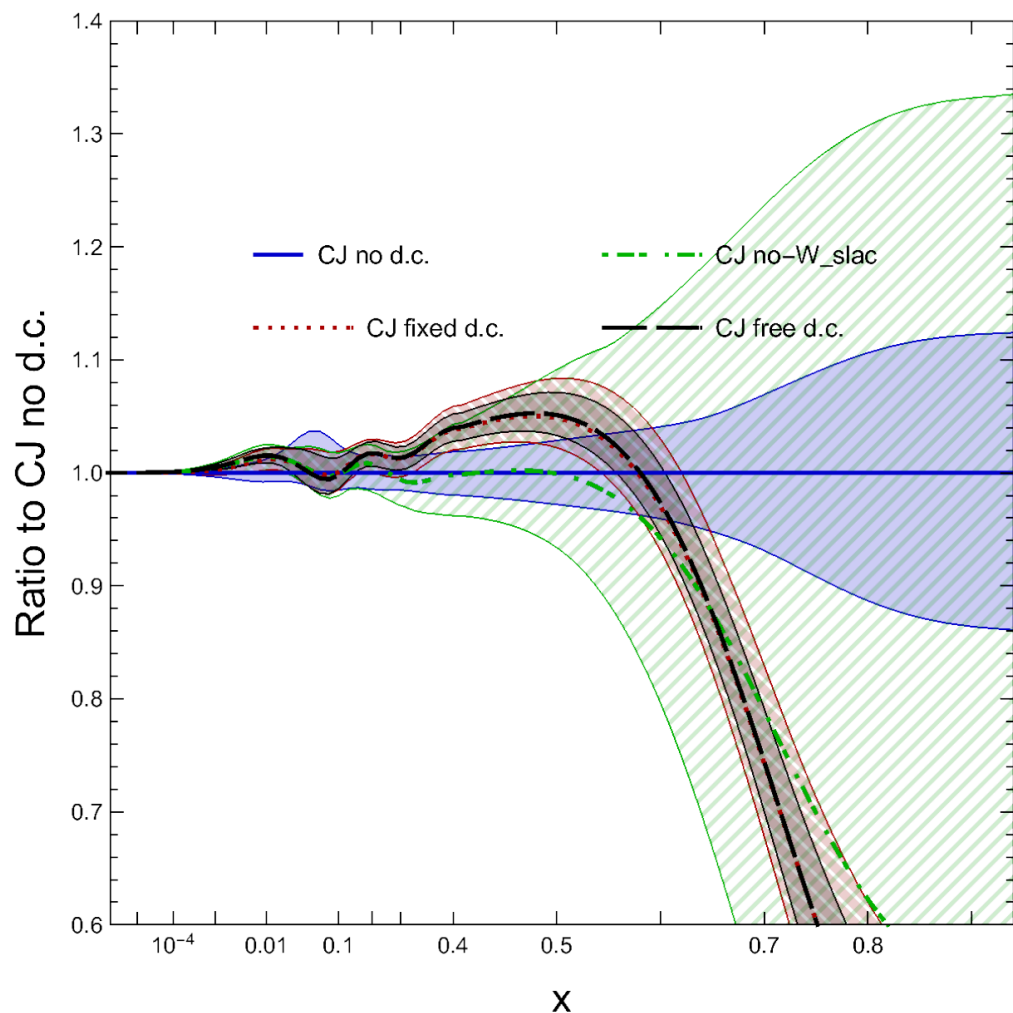


- d -PDF information from deuteron scattering; nuclear corrections relevant

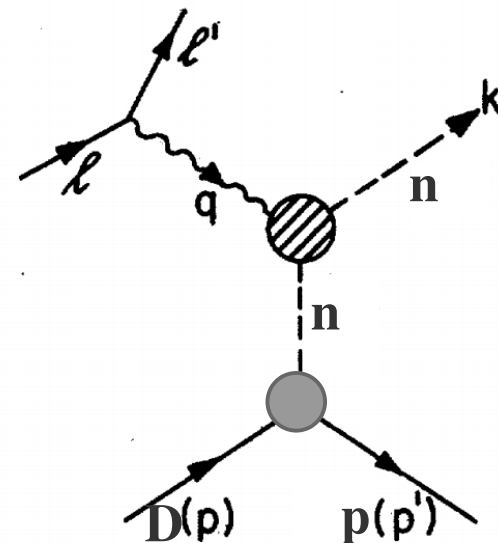
$$f^d(x, Q^2) = \int \frac{dz}{z} \int dp_N^2 \mathcal{S}^{N/d}(z, p_N^2) \tilde{f}^N(x/z, p_N^2, Q^2)$$

$d(x, Q)/u(x, Q)$ at $Q=2.0$ GeV, $T^2 = 10$

Accardi, TJH, Jing, Nadolsky: EPJC81 (2021) 7, 603

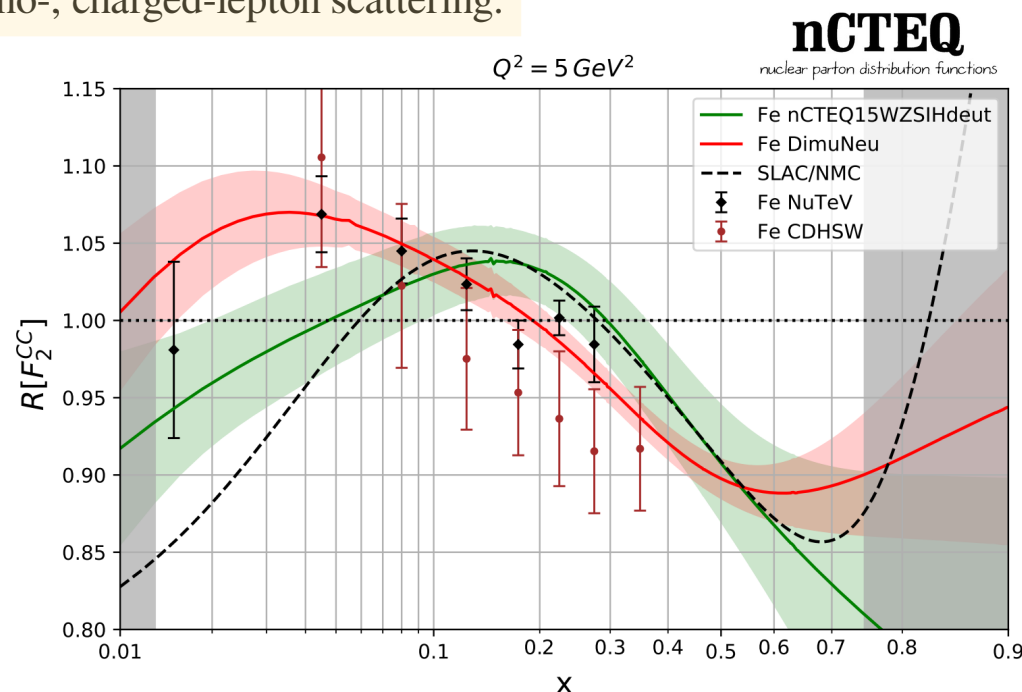
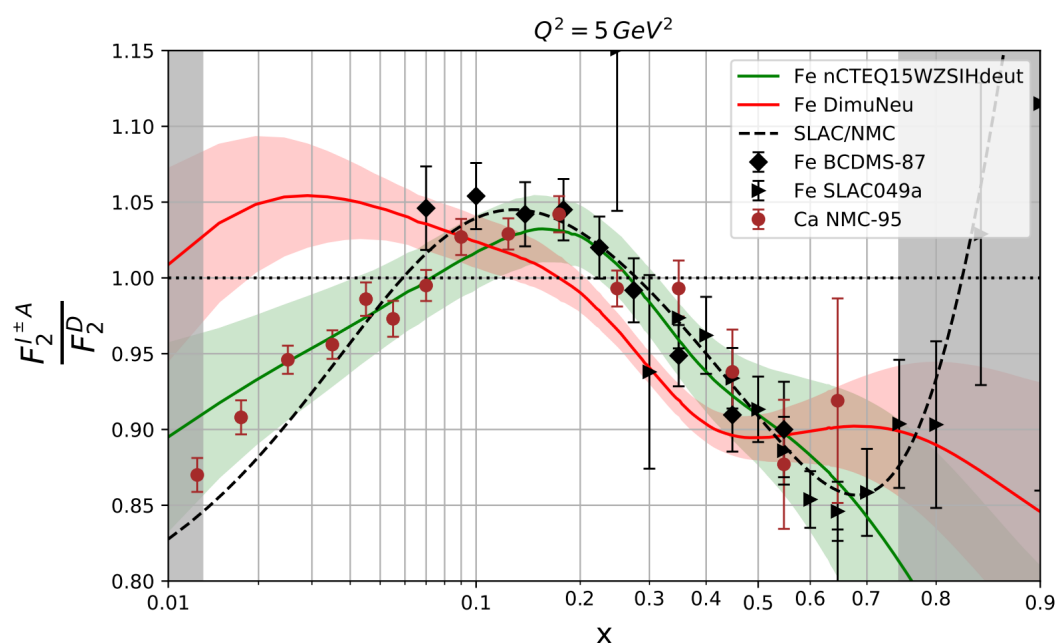


- corrections are generally ~percent-level, but can become larger, especially at high x
- impacts LHC observables; necessary for high precision



- beyond few-body systems, CT, other analyses use heavy-nuclei for flavor separation
[e.g., νA for strangeness]
- requires knowledge of nuclear corrections; these directly fitted by nPDF analyses
→ better control over x , A dependence can benefit nucleon PDF extractions

ongoing questions of statistical compatibility of neutrino-, charged-lepton scattering:



Muzakka, Duwentäster, TJH et al., 2204.13157

- (HL-)EIC can help unravel these issues

→ higher luminosity helpful for nuclear collisions, which have lower $\sqrt{s}$

nonperturbative theory developments: lattice QCD inputs

- recent years: progress in *ab initio* hadron-structure calculations from LQCD

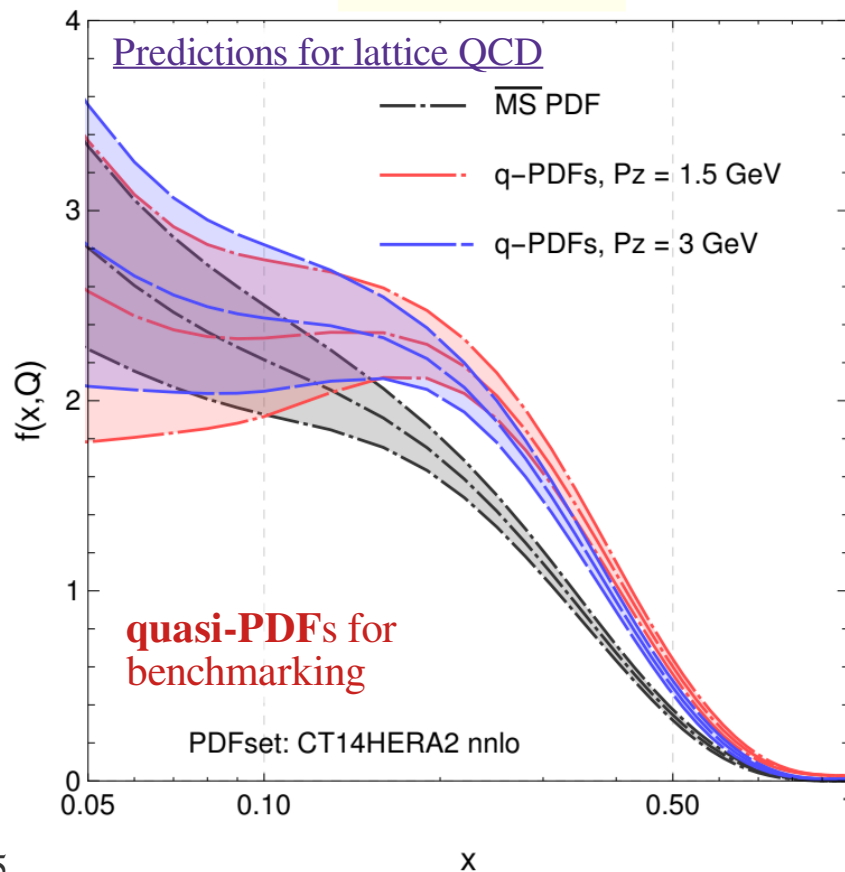
→ quasi-PDFs, pseudo-PDFs, quasi-TMDs, ...

there are be important synergies between PDF fitting and lattice QCD

[overlaps with EIC; vDIS; LHC]

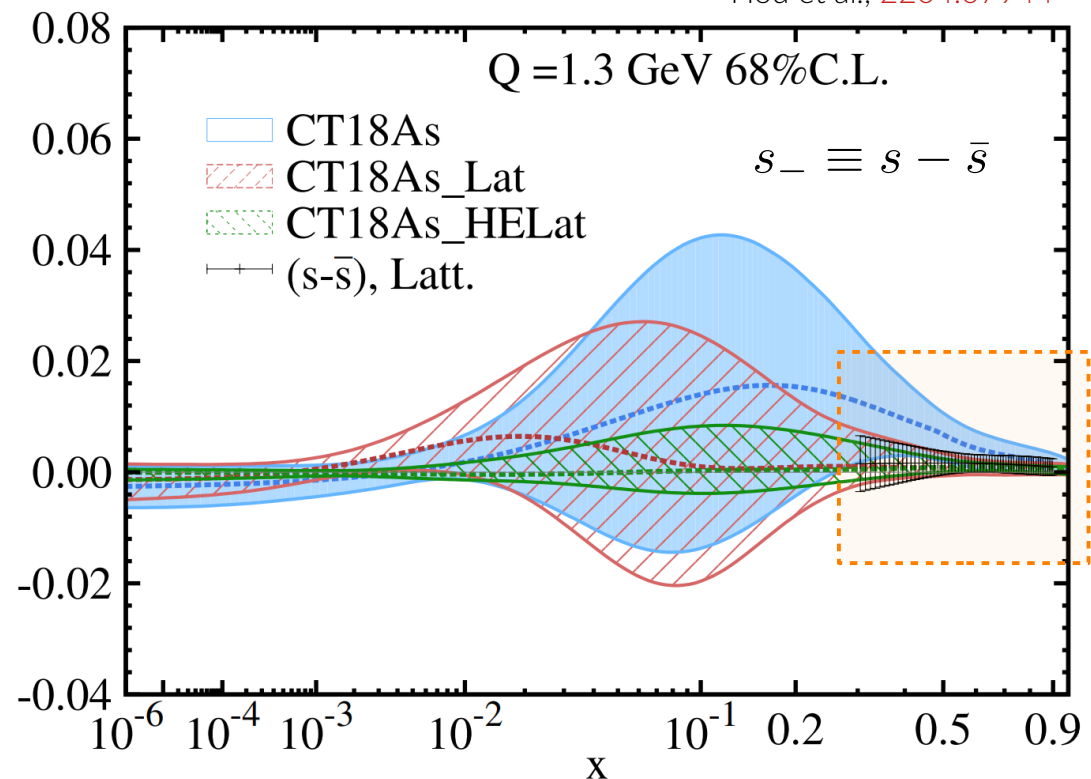
TJH, Wang, Nadolsky, Olness, PRD **100** (2019) 9, 094040

u-d at $\mu_F = 3\text{GeV}$



- lattice data can potentially inform high- x behavior of quark sea

Hou et al., [2204.07944](#)



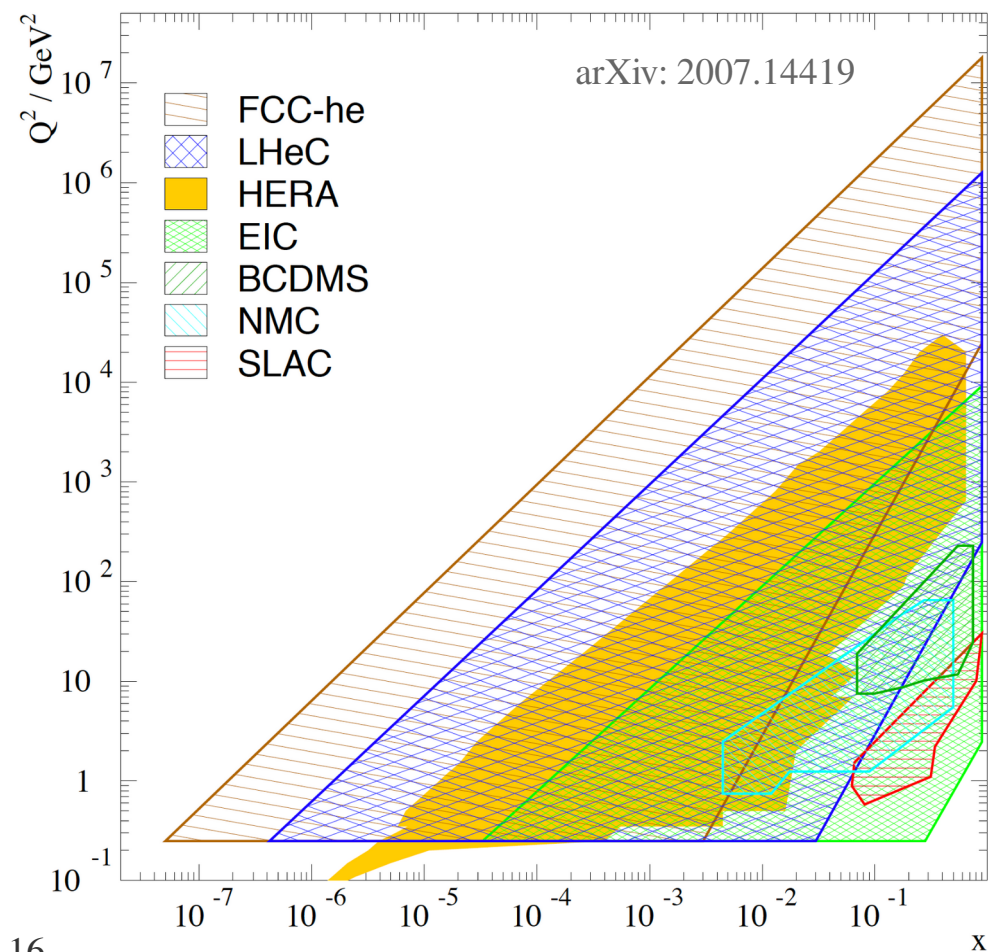
PDF precision both aided and challenged by experiments

- array of (DIS) measurements needed as kinematical lever-arm; distinct EW probes

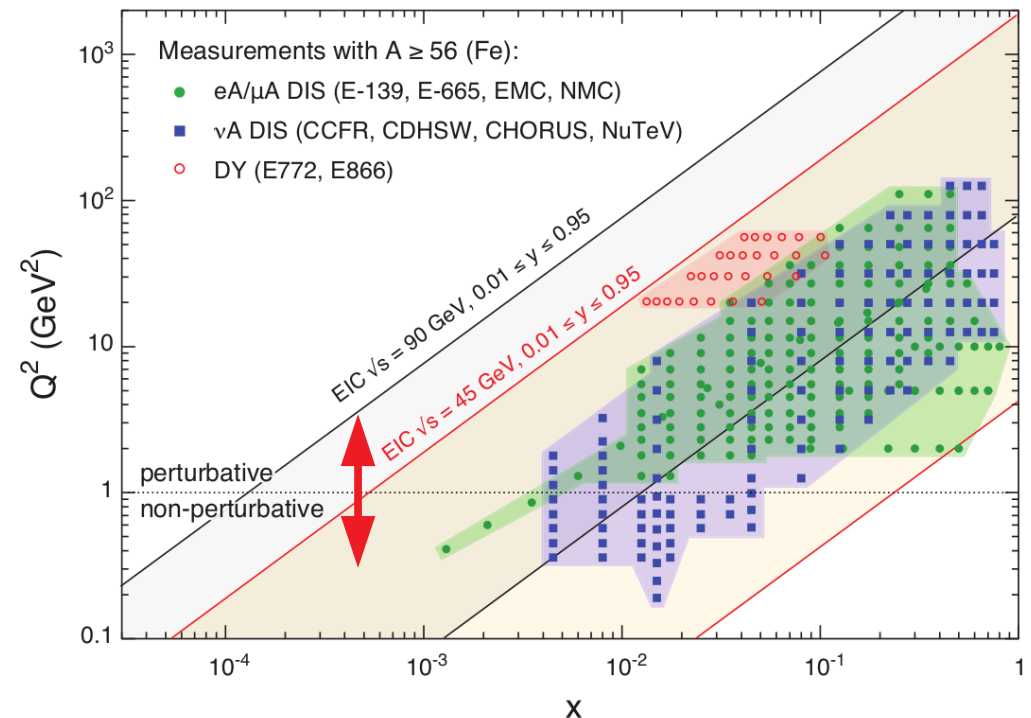
→ as proxy, consider role of EIC program: impacts on high x , HEP pheno.

- EIC explores unique, complementary region in $[x, Q^2]$

→ strong coverage of **quark-to-hadron transition** region between HERA, JLab12



analogous nuclear DIS coverage:



PDF impacts compared to high-value fixed-target DIS

ePump: Schmidt, Pumplin, and Yuan; PRD98 (2018) no.9, 094005

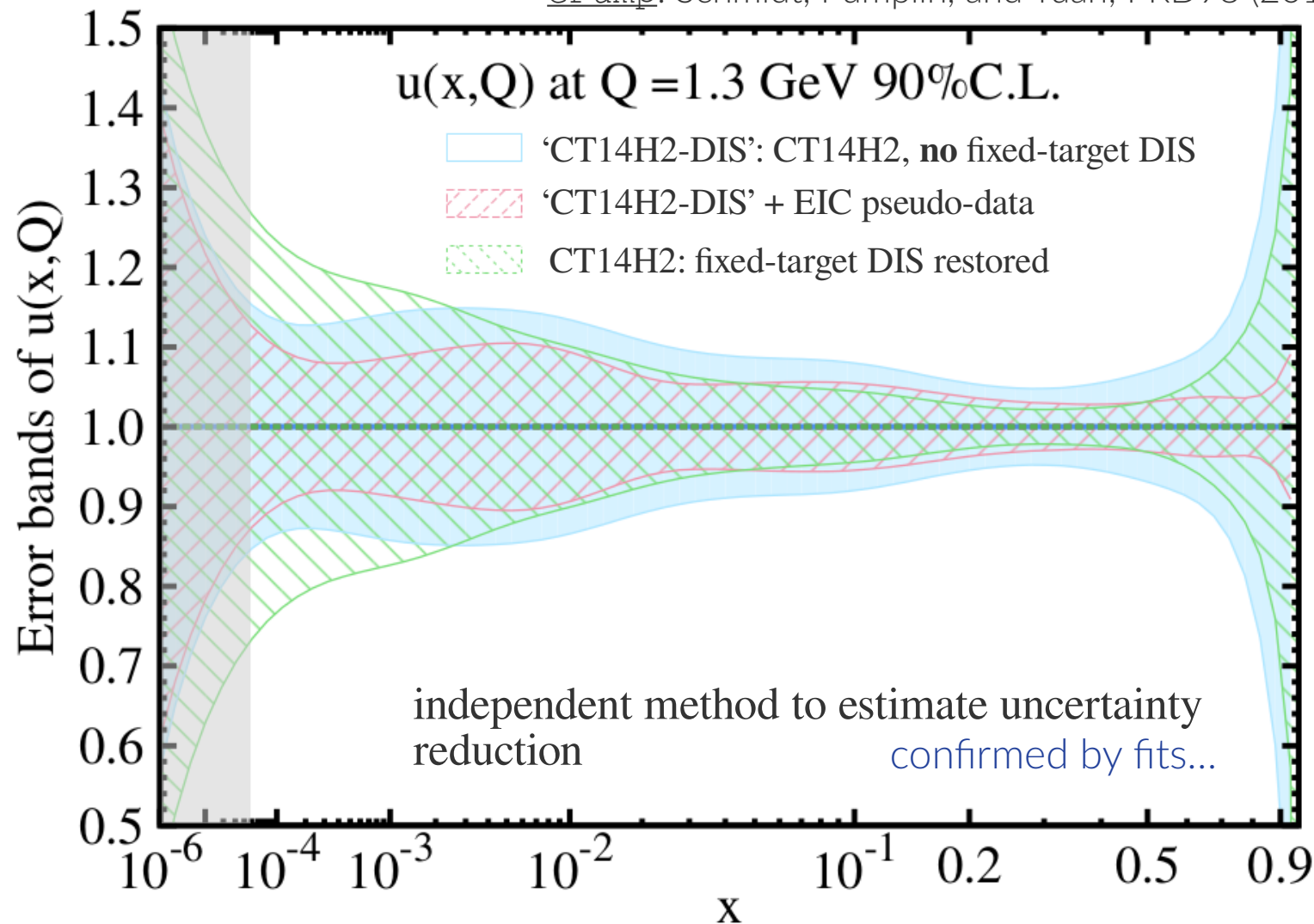


figure: S. Dulat

- **inclusive EIC may surpass total impact of fixed-target DIS in modern fits**

→ useful for negotiating among existing high-impact data; high lumi could extend further

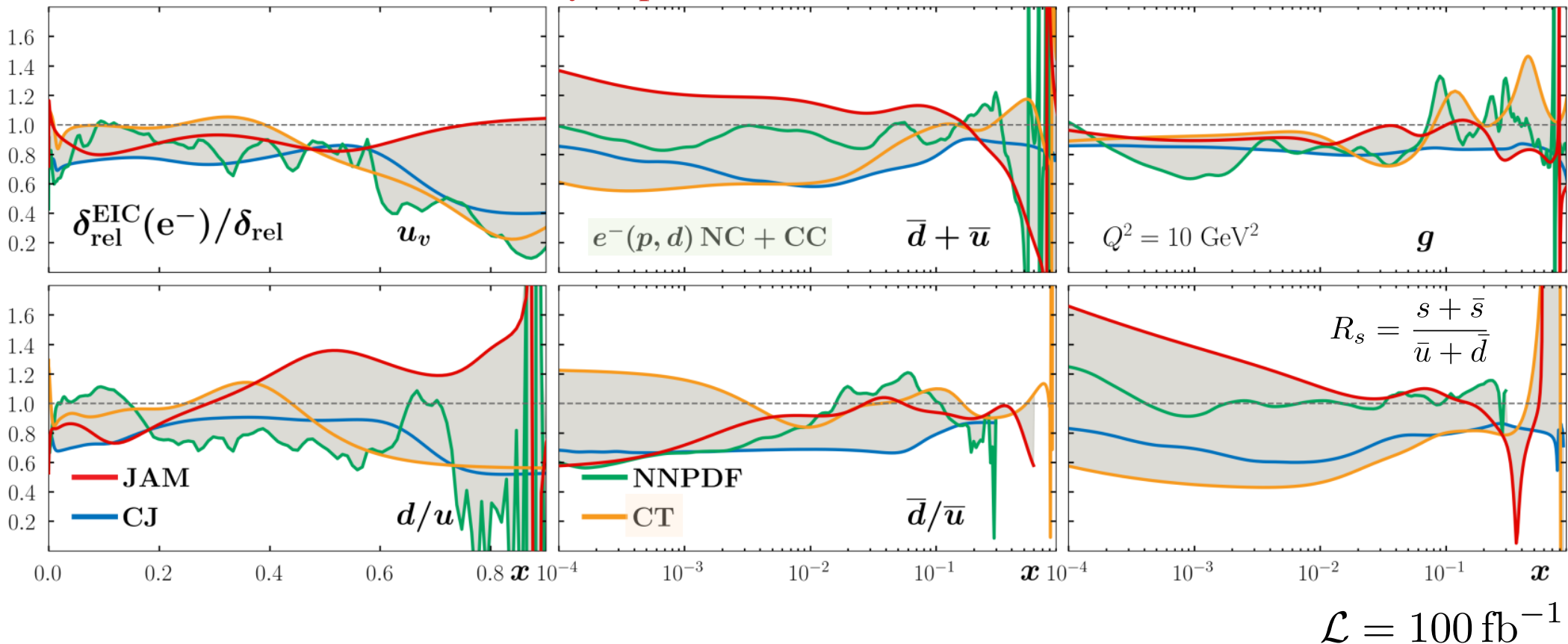
reductions to PDF uncertainties: inclusive DIS data

- impact from simulated (optimistic) pseudodata; estimated by various methods, groups

EIC YR, 7.1.1

PDF uncertainty improvement

~1 year of [peak] data-taking



- broad impact, including on high- x u -, d -PDFs; probes of gluon, quark sea to low x

→ inclusive studies – indications of systematics limitations; **must also investigate**

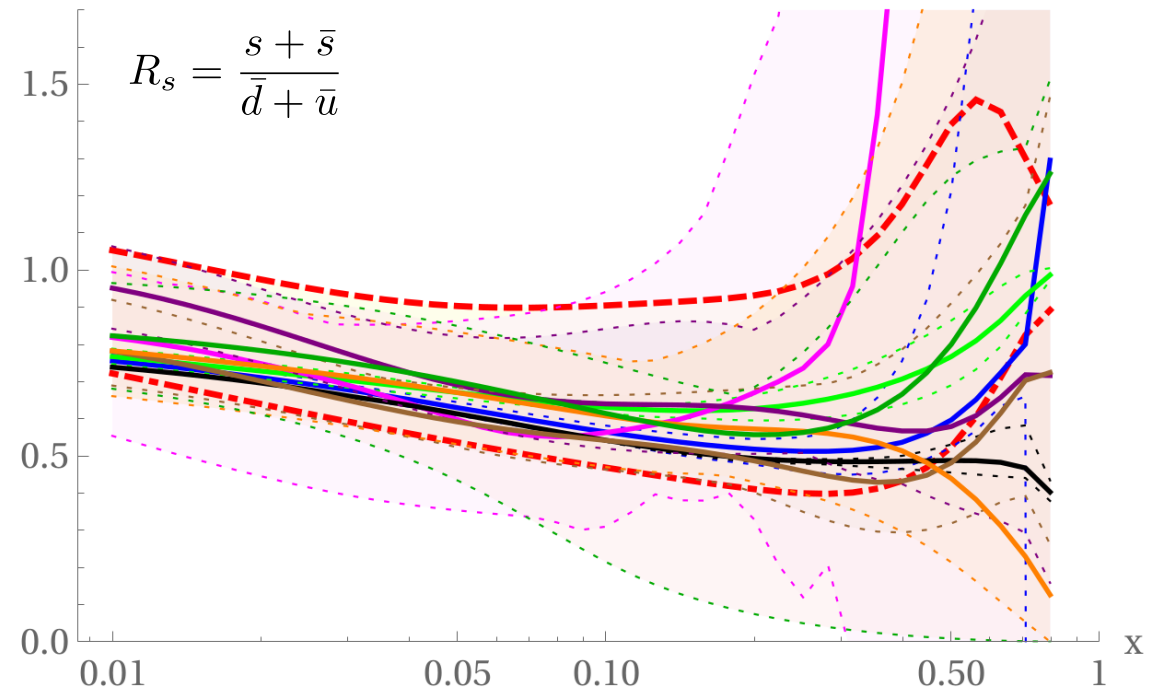
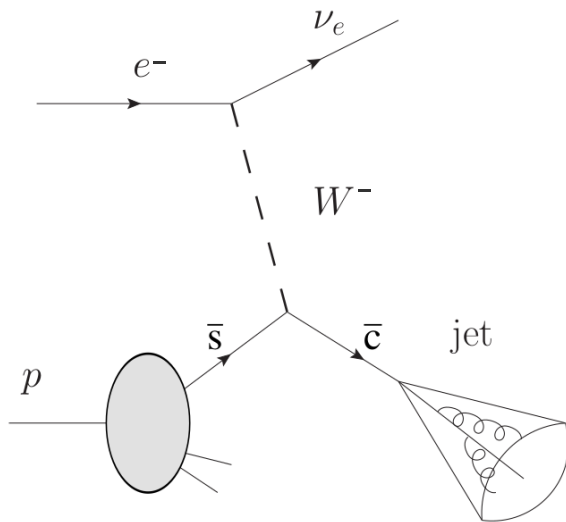
precision QCD through jet and heavy-flavor production

- DIS jet production, including through charge-current interactions, provides further access to quark-level information

Arratia, Furletova, TJH, Olness, Sekula; PRD 103 (2021) 7, 074023

$R_s(x, Q)$ $Q=10$ GeV

100 fb⁻¹ CC DIS (10M simulated events),
at 10x275 GeV (e^- on p); $Q^2 > 100$ GeV²

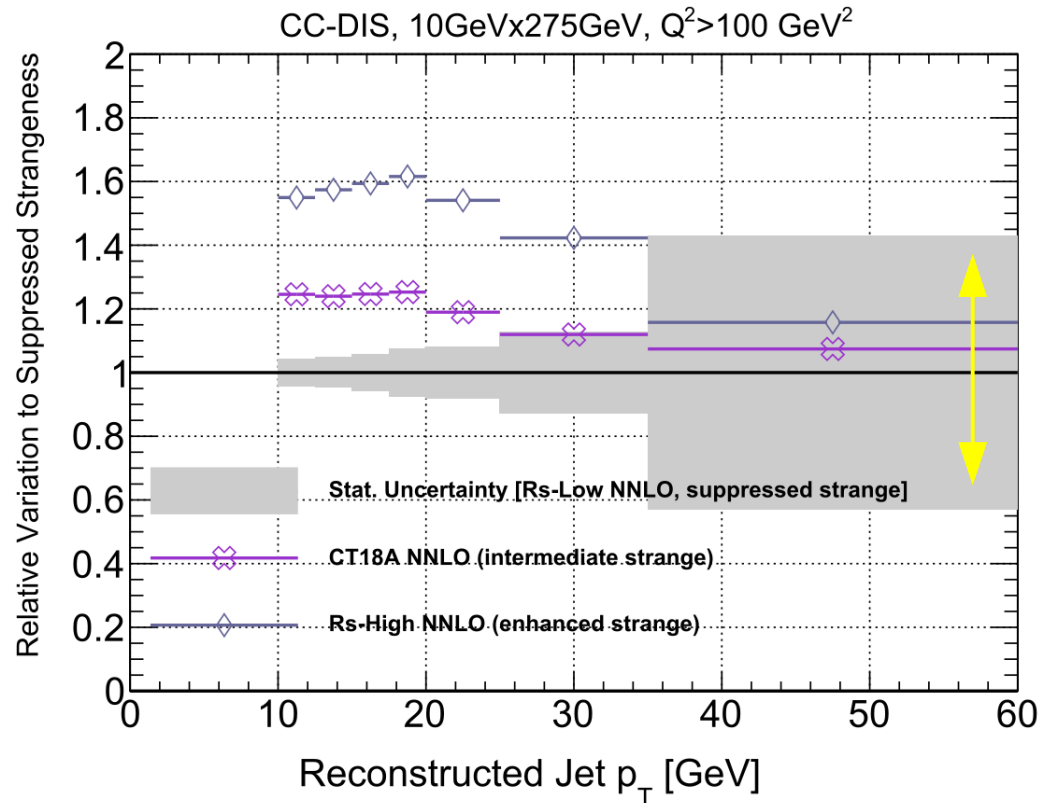


final-state tagging provides lever arm for flavor separation (here, strangeness)

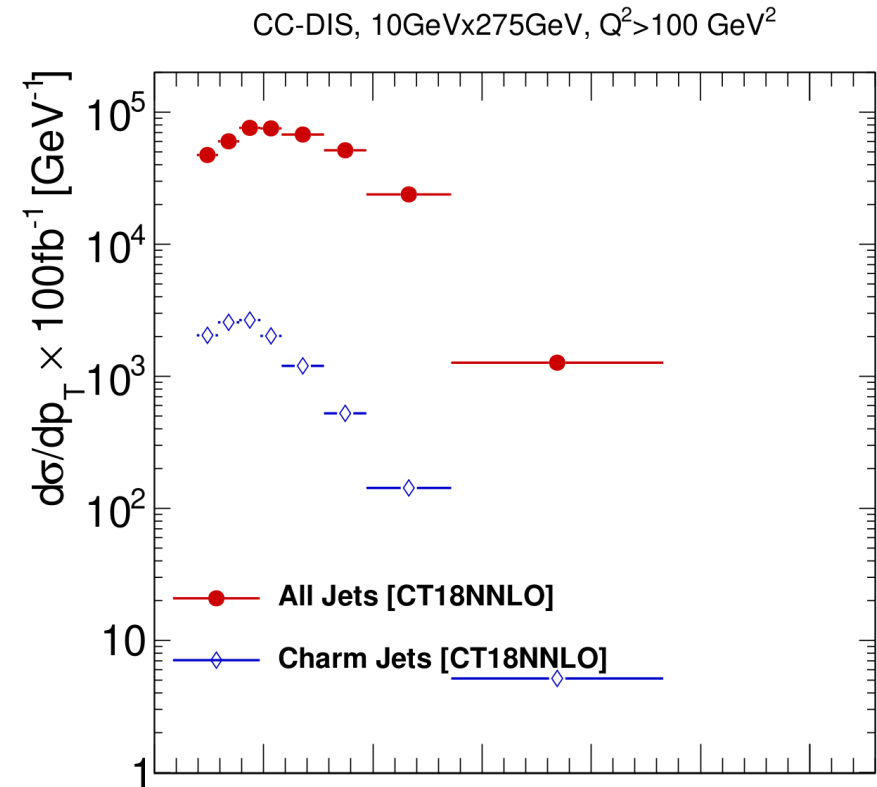
- n.b.: event generation, detector sim from PYTHIA8 + DELPHES; FASTJET reconstruction
→ analogous jet measurements might be extended to nonperturbative heavy flavor

precision QCD through jet and heavy-flavor production

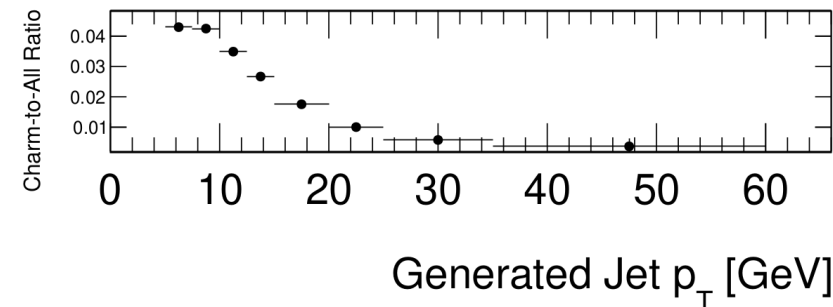
- challenging measurement: final-state flavor tagging; Jacquet-Blondel reconstruction



Arratia, Furlletova, TJH, Olness, Sekula; PRD 103 (2021) 7, 074023



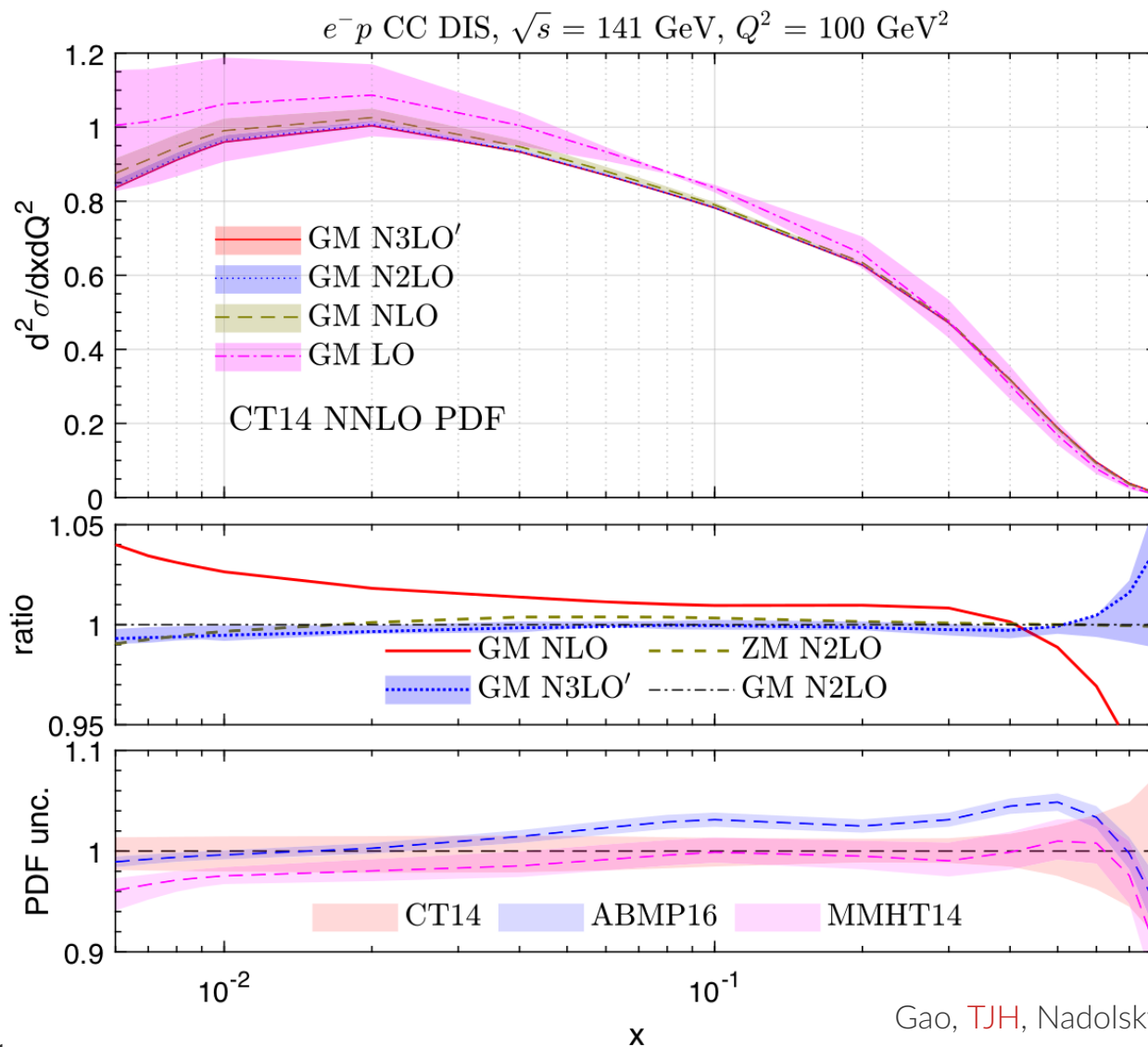
- charm production suppressed by >2 orders of magnitude; p_T cross section steeply falling
- reduced δ_{stat} could significantly enhance knowledge of p_T dependence



→ greater event rates may furnish enhanced discriminating power

(CC) DIS at NNLO and beyond

- extracting PDF information from CC DIS requires robust theory accuracy
 - can compute NNLO, approximate N³LO corrections for highest energies at EIC



- strong perturbative convergence

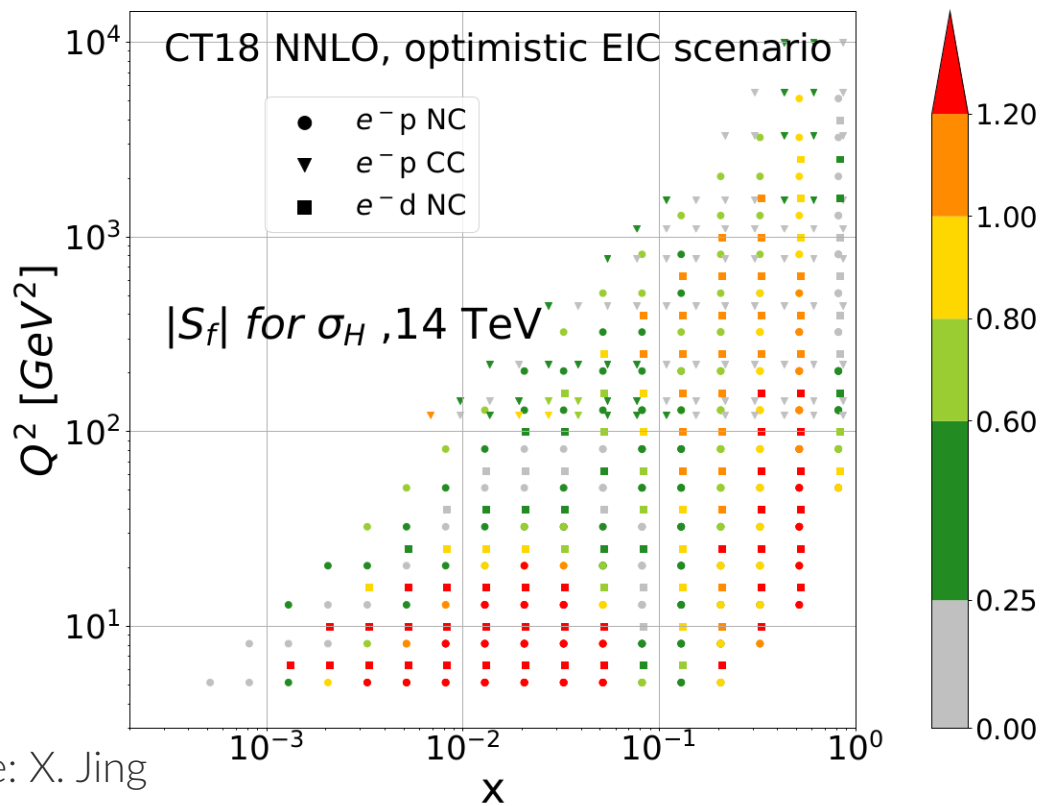
→ for N³LO', scale variations generally contained to $\lesssim 0.5 - 1\%$

- significantly smaller than PDF-driven uncertainties, which can be as large as $\approx 2\%$

vital ingredient in EIC PDF program

- note improvements at high x : suggests possible synergy with high-luminosity measurements

ii

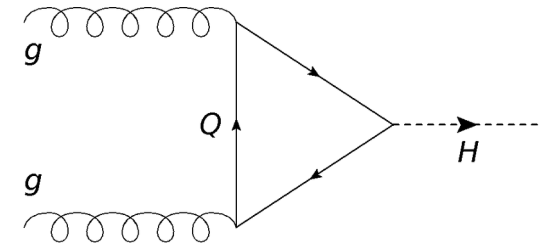
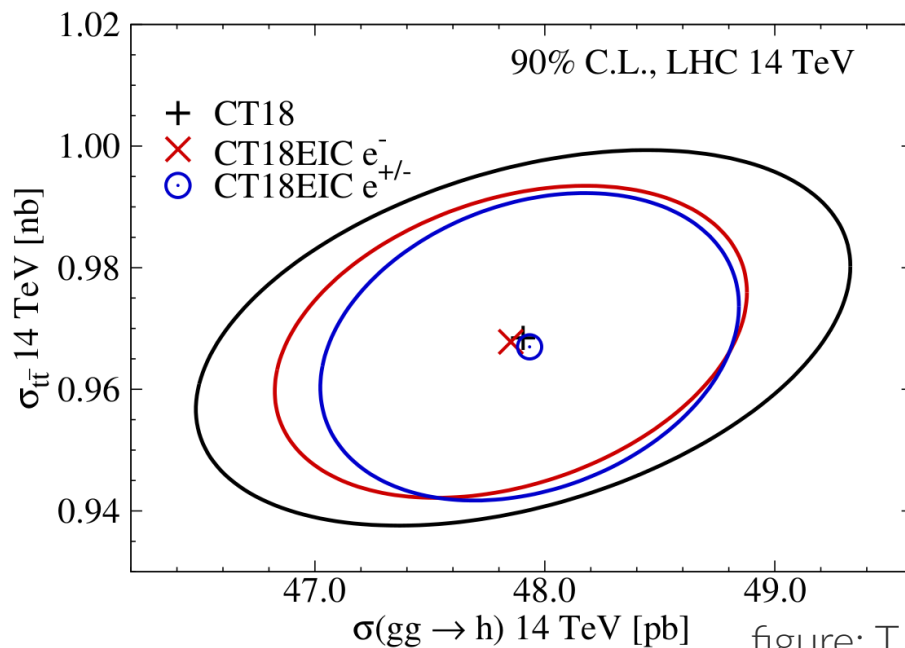


precise EIC data impact
high-energy predictions

example:

- PDF-driven improvement to **Higgs-production** cross section
- EIC impact on Higgs theory from broad region of the kinematical space it can access

figure: X. Jing

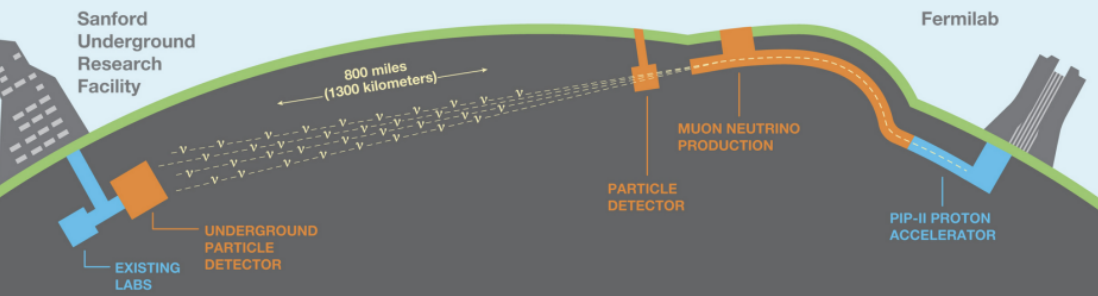


- impact closely tied to that of the integrated gluon PDF

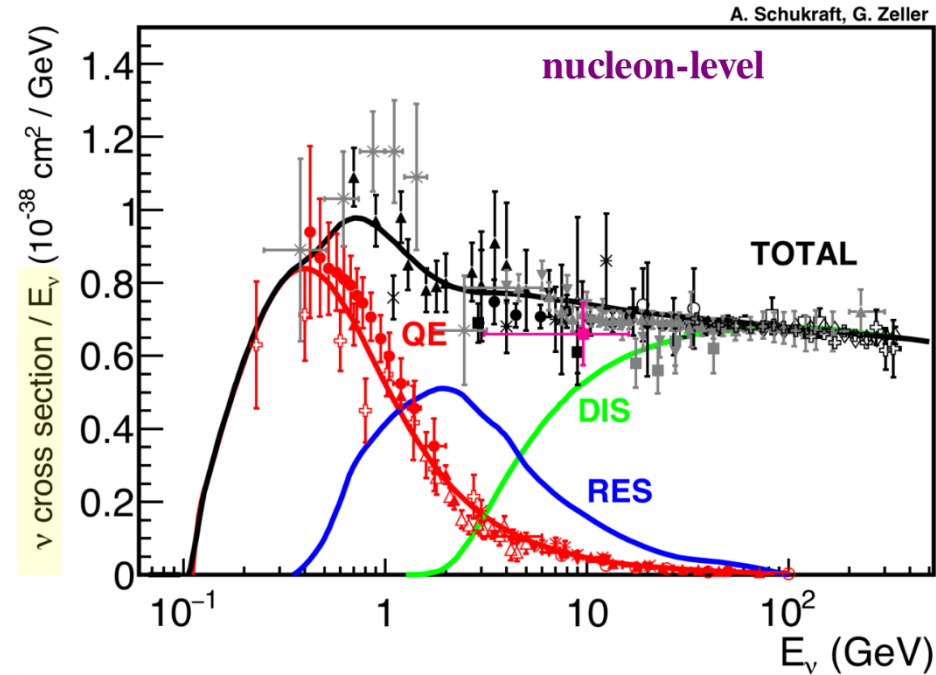
→ similar impacts on EW observables

figure: T.-J. Hou

Deep Underground Neutrino Experiment



nPDFs key to ν DIS precision

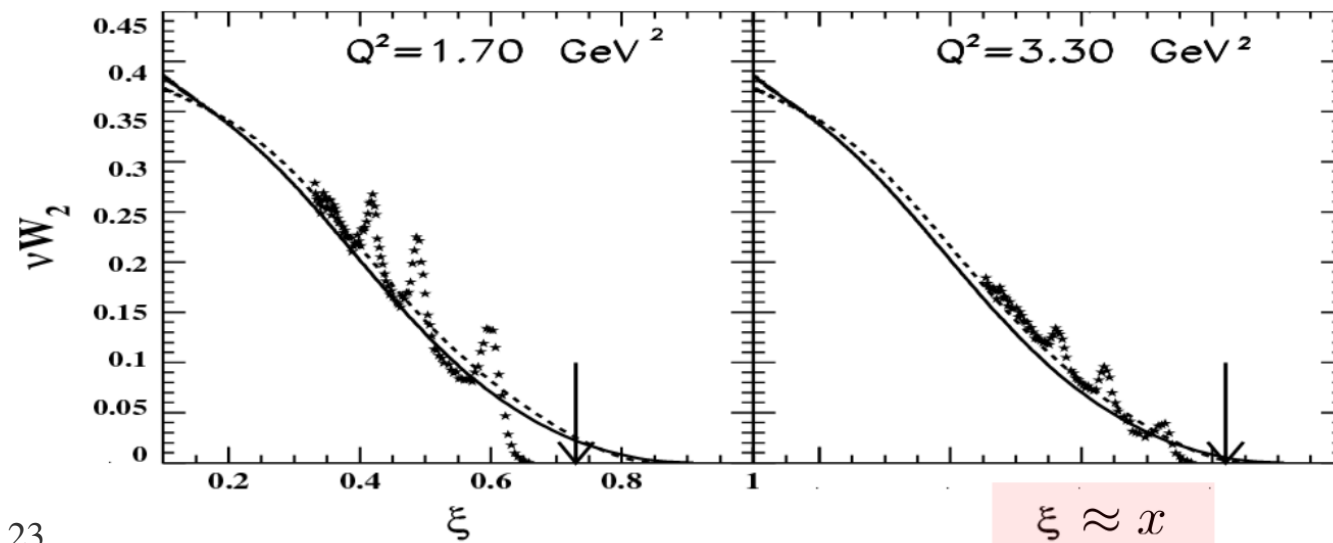


■ neutrino oscillation searches (e.g., DUNE) require accurate knowledge of νA interaction

→ $E_\nu \sim \text{few GeV}$ dominated by RES/DIS

→ DIS subject to finite- Q^2 , nuclear effects
(HTs; TMCs; few- and large- A)

→ ν generators generally implement phenomenological models at LO; minimal error quant.

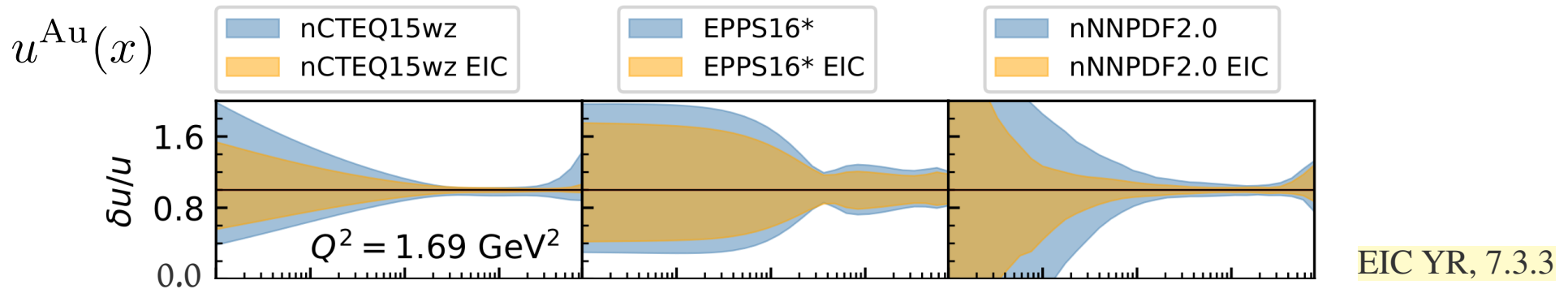


■ nPDFs, QCD-based approaches to low- Q , W ν DIS badly needed

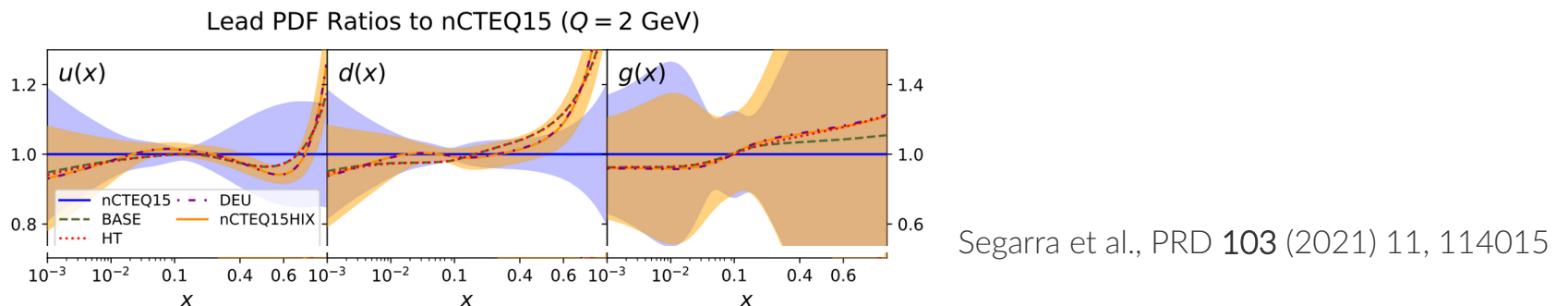
■ future near-detector ν expts may yield more QCD information

understanding nuclear effects

→ EIC: measure only “clean” DIS from hadrons; but also explore nuclear medium!



▪ nPDFs can inform nuclear effects in free-nucleon studies and *vice versa*:



→ nuclear effects: jet production, hadronization; implications for AA, UPC programs

▪ nuclear A dependence requires copious data: **high luminosity essential**

- signatures of nonperturbative QCD are etched upon the PDFs
 - flavor-symmetry breaking ($\bar{d}/\bar{u}$); wave function effects [$d(x \approx 1)$]
 - nuclear effects [$q(x)$, intermediate x]; description of deuterium data
- critical for understanding QCD; **necessary for precision HEP measurements**
 - limit EW precision, sensitivity of BSM tests, neutrino programs
 - closely related to challenge of flavor separation
- recent theory progress: pQCD now at (N)NNLO; interfacing with PDFs
 - higher perturbative accuracy suggests parallel theory improvements
 - EW higher-order accuracy; introduction of nuclear, nonpert. effects
 - next-gen unraveling of statistical influence of fitted experiments

closely linked to physics of confinement

future experiments central: JLab12 → EIC, HL-LHC, LBNF, ...