

# TENSIONS IN THE HEAVY SECTOR

# Giulia Ricciardi





Selection of flavor anomalies shown as pulls of (blue points) experiment versus (orange diamonds) theory expectation.

For each measurement the quadratic sum of the experimental and heory uncertainties is normalised to unity and the deviation of the experimental value is displayed in this unit.

D. Guadagnoli, P. Koppenburg, arXive 2207.01851

## ASSIGNMENT

Explain differences between observables and SM predictions in the heavy flavour sector

Observables in  $b \rightarrow s \ell^+ \ell^-$  driven decays (from 2013 at LHCb)

Observables in  $b \rightarrow c \,\ell v$  driven decays (from 2012 at Belle)

 $V_{ub}/V_{cb}$  exclusive/inclusive puzzle (decades of CKM fits)

# EXECUTION

Effective Field Theories and/or Model building

RESULTS

Not (yet) conclusive

Reading the assignment: Experimental situation



# Semileptonic B decays



1 loop (and CKM suppressed) in the SM BR ~  $\mathcal{O}(10^{-6})$  or lower

Neutral current

#### Discrepancy in

- R(K) and R(K\*), R(φ) testing LFU
   (FF large hadronic cancellation in SM)
- observables related to  $b \rightarrow s \ \mu^+ \mu^-$ 
  - Branching ratios
  - angular observable
- Optimized (as  $P'_5$ ) and not Expected heavy NP ~  $4 \ 10^{-5} \ G_F \rightarrow \frac{1}{(40 \ Tev)^2}$

### $b \rightarrow c$ anomalies



Tree level in the SM. Br a few %

Charged current

#### Discrepancy in

 R(D) R(D\*) R(J/Ψ) testing LFU (FF large hadronic cancellation in SM)

Expected light NP~ 
$$10^{-2} G_F \rightarrow \frac{1}{(few Tev)^2}$$

### Lepton Flavour Universality violation (LFUV)

$$R_X \equiv \frac{BR(B \to X l l / l \nu)}{BR(B \to X l' l' / l' \nu')}$$

CKM factors and hadronic (in SM) cancellations

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \to K^{(*)} \mu \mu)}{\mathcal{B}(B \to K^{(*)} e e)} \bigg|_{q^2 \in [q^2_{\min}, q^2_{\max}]} \qquad q^2 \in [1, 6] \,\text{GeV}^2 \text{ to stay away from } \bar{c}c \text{ resonances}$$

$$R_{K^{(*)}}^{\exp} < R_{K^{(*)}}^{\text{SM}}$$

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \to D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \to D^{(*)} \ell \bar{\nu})}_{\ell \in (e,\mu)}$$

$$R_{D^{(*)}}^{\exp} > R_{D^{(*)}}^{SM}$$





LHCB

$$R_{K^{*0}} = \begin{cases} 0.66 \stackrel{+ \ 0.11}{- \ 0.07} (\text{stat}) \pm 0.03 (\text{syst}) & \text{for } 0.045 < q^2 < 1.1 \ \text{GeV}^2/c^4 \\ 0.69 \stackrel{+ \ 0.11}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) & \text{for } 1.1 \\ 0.05 (\text{syst}) & \text{for } 1.1 \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) & \text{for } 1.1 \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \pm 0.05 (\text{syst}) \\ 0.69 \stackrel{- \ 0.07}{- \ 0.07} (\text{stat}) \\ 0.69 \stackrel{-$$





R(D) and R(D<sup>\*</sup>) exceed the SM predictions by 1.4 $\sigma$  and 2.8 $\sigma$  respectively

[HFLAV, 2206.07501]

#### CAUTION







JNP:Jaiswal et al. JHEP, 06 (2020) 165

DM: Dispersive Matrix method  $R(D^*) = 0.275 \pm 0.008$ 1.3 $\sigma$  compatibility

Bečirević Moriond 22

Vittorio La Thuile 2022



$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c^+ \to J/\psi \tau^+ \nu_{\tau})}{\mathcal{B}(B_c^+ \to J/\psi \mu^+ \nu_{\mu})} = 0.71 \pm 0.17 \,(\text{stat}) \pm 0.18 \,(\text{syst}).$$

 $2.1\sigma$  from SM central values ~ 0.25.

LQCD 
$$R(J/\Psi) = 0.2582 \pm 0.0038$$

LHCb *Phys.Rev.Lett.* 120 (2018) 12

HPQCD Phys. Rev. Lett. 125, 222003 (2020)

$$R(\Lambda_c) = \frac{B(\Lambda_b \to \Lambda_c \tau^- \bar{\nu})}{B(\Lambda_b \to \Lambda_c \mu^- \bar{\nu})} = 0.242 \pm 0.026 \text{ (stat.)} \pm 0.040 \text{(syst.)} \pm 0.059 \text{(ext.BR.meas.)}$$

LHCb, *Phys.Rev.Lett.* 128 (2022) 19

 $R(\Lambda_c)_{\rm SM} = 0.33 \pm 0.01$ 

1σ from SM central values (agreement)

Approximate sum rule

$$\frac{R(\Lambda_c)}{R(\Lambda_c)_{\rm SM}} \simeq 0.262 \frac{R(D)}{R(D)_{\rm SM}} + 0.738 \frac{R(D^*)}{R(D^*)_{\rm SM}} = 1.15 \pm 0.04$$
Blanke et al.  
*Phys rev D 99*  
(2019) 075006

enhancement of  $R(\Lambda_c)$  if the anomaly in  $R(D^{(*)})$  holds true 12



# interpretation



### **EFFECTIVE FIELD THEORY:**

BSM at a higher kinematic range





$$\frac{\mathcal{B}(B^0 \to D^{*-} e^+ \nu)}{\mathcal{B}(B^0 \to D^{*-} \mu^+ \nu)} = 1.01 \pm 0.01 \pm 0.03$$

Belle Phys. Rev. D 100 (2019) 5, 052007,

NP generally assumed in semitauonic B decays

Effective Hamiltonian for  $b \to c\tau \; v$ 

$$H_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{cb} \left[ (1 + C_V^L) O_V^L + C_V^R O_V^R + C_S^R O_S^R + C_S^L O_S^L + C_T O_T \right]$$

 $O_V^R$  excluded by SMEFT match

Charged current process: simple (tree level) model interpretation



#### new charged states with masses at or below the TeV and with significant couplings to the third generation SM fermions **man** potential targets for direct searches at the LHC Charged W 'bosons: simplified models (spin-1 colorless weak triplet, a 2HDM, a spin-0 or spin-1 leptoquark) in tension with existing $\tau + \tau - LHC$ results. Faroughy et al.2016 Not applies to the low mass region in the W' and vector leptoquark models Charged Higgs boson H<sup>±</sup>: Crossing symmetry Greljo et al. 2019 tension with the LHC mono-τ data Alonso 2019, Akeroydet large BR(Bc $\rightarrow \tau v$ ) > 50% induced 2017, Blanke. 2019, no direct experimental bound but upper limits of 30%, and even 10% Aebischer 2021,... But as large as 60% not excluded Angelescu 2018, Leptoquarks: Babu e2021,

Generally evade the mono-T test (can induce CP-violating couplings) LHC constraints from their pair-production and t-channel mediated dilepton processes LHC searches for colour-octet resonances, often introduced together in UV-complete models

Warning: more severe constraints in concrete UV completions e.g.. including light RH neutrinos lguro 2017, Greljo 2018, Robinson 2019, Azatov 2018, Mandal<sup>7</sup>2020,...

Buttazzo 2017, Diaz

2017, Baker 2019,...

 $b \rightarrow s \ \ell^+ \ell^-$  effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb}^* V_{ts} \frac{e^2}{16\pi^2} \sum_i (C_i O_i + C'_i O'_i) + \text{h.c.}$$

$$\mathcal{O}_{7} = \frac{e}{16\pi^{2}} m_{b} (\bar{s}\sigma_{\mu\nu}P_{R}b)F^{\mu\nu}, \qquad \qquad \mathcal{O}_{7'} = \frac{e}{16\pi^{2}} m_{b} (\bar{s}\sigma_{\mu\nu}P_{L}b)F^{\mu\nu}, \\ \mathcal{O}_{9\ell} = \frac{e^{2}}{16\pi^{2}} (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\ell}\gamma^{\mu}\ell), \qquad \qquad \mathcal{O}_{9'\ell} = \frac{e^{2}}{16\pi^{2}} (\bar{s}\gamma_{\mu}P_{R}b)(\bar{\ell}\gamma^{\mu}\ell), \\ \mathcal{O}_{10\ell} = \frac{e^{2}}{16\pi^{2}} (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\ell}\gamma^{\mu}\gamma_{5}\ell), \qquad \qquad \mathcal{O}_{10'\ell} = \frac{e^{2}}{16\pi^{2}} (\bar{s}\gamma_{\mu}P_{R}b)(\bar{\ell}\gamma^{\mu}\gamma_{5}\ell), \end{cases}$$

Two sources of hadronic uncertainties for exclusive  $\downarrow l^+$   $\downarrow l^+$  $\downarrow$ 

Global fits
- Fully Data Driven: no
assumption about charming
penguins
- Partly or fully Model
Dependent: assume LCSR
result for charming
penguins 18

 $\ell = \mu, e$ 

#### About 250 obs All, 25 LFUV

#### 1D Scenarios for Ciu

$$\mathcal{C}_{i\ell} = \mathcal{C}^{\mathrm{SM}}_{i\ell} + \mathcal{C}^{\mathrm{NP}}_{i\ell}$$

	All			LFUV				
1D Hyp.	Best fit	$1 \; \sigma/2 \; \sigma$	$\mathrm{Pull}_{\mathrm{SM}}$	p-value	Best fit	$1~\sigma/~2~\sigma$	$\operatorname{Pull}_{\mathrm{SM}}$	p-value
$\mathcal{C}_{9\mu}^{ m NP}$	-1.01	[-1.15, -0.87]	7.0	24.0 %	-0.87	[-1.11, -0.65]	4.4	40.7%
		[-1.29, -0.72]				[-1.37, -0.45]		
$\mathcal{C}^{\rm NP} = \mathcal{C}^{\rm NP} = 0.45$	-0.45	$\left[-0.52, -0.37 ight]$	65	16.0%	0.30	[-0.48, -0.31]	5.0	73 5 %
$c_{9\mu} = -c_{10\mu}$	$-c_{10\mu}$    $-0.45$   $[-0.59, -0.30]$   $0.5$   $10.970$    $-0.59$	-0.59	[-0.56, -0.23]	5.0	10.070			
$\mathcal{C}_{9\mu}^{ m NP}=-\mathcal{C}_{9'\mu}$	-0.92	[-1.07, -0.75]	5.7	8.2%	-1.60	[-2.10, -0.98]	3.2	8.4%
		[-1.22, -0.59]				[-2.49, -0.46]		

Pull<sub>SM</sub> is quoted in units of standard deviation. The p-value of the SM hypothesis is 0.44% for the fit "All" and 0.91% for quantities assessing LFUV

M. Algueró et al. EPJC 82 (2022)

Global fits: general agreement

Alguero 21, Geng 21, Cornella 21, Angelescu 21, Hurth 21...



Allowing for the presence of lepton flavour universal NP in addition to LFUV contributions to muons only.

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J. Matias

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#### Mainstream models:

- loop-induced NP
- tree-level NP contributions

Z' gauge bosons changing coupling to LH quarks VL couplings to leptons FV or FNU in lepton sector



Leptoquarks scalar or vectors



 $\Box$   $\Lambda_{NP} \sim 40$  TeV no direct production of new particles at the (HL-)LHC Limited reach for searches for deviations from the SM in high- $p_T$  di-muon tails

 $\Box$  bsZ<sup>'</sup> coupling stringently constrained by B<sub>s</sub>-B<sup>'</sup> mixing data  $\overline{B_s}$ 

greljo 2017

vector leptoquark. Solution to b-> c and b-> s anomalies [cons UV completion, possible large number of parameters and assumptions] Cornella 21 LHCb prospects



[arXiv:2101.08326, arXiv:1808.08865]



### |V<sub>xb</sub>| puzzle

- Semileptonic decays most precise determination of  $|V_{ub}| \& |V_{cb}|$
- Tree level: no loop suppression & assumed largely free of BSM

 Exclusive/Inclusive determinations: different techniques: check of our theoretical tools for QCD

 $b \rightarrow c \ell v (B \rightarrow D^{(*)} \ell v / B \rightarrow X_c \ell v) \qquad b \rightarrow u \ell v (B \rightarrow \pi(...) \ell v / B \rightarrow X_u \ell v)$ 

Long standing excl/incl tension in  $|V_{xb}|$ 

### Inclusive decays $B \rightarrow X_c \ell \nu$

Heavy Quark Expansion for sufficiently inclusive quantities (total width, moments of kinematical distributions) double series in  $a_s & \Lambda_{QCD}/m$ 

$$\Gamma(B \to X_q l \nu) = \frac{G_F^2 m_b^5}{192\pi^3} |V_{qb}|^2 \left[ c_3 \langle O_3 \rangle + c_5 \frac{\langle O_5 \rangle}{m_b^2} + c_6 \frac{\langle O_6 \rangle}{m_b^3} + O\left(\frac{\Lambda_{QCD}}{m_b^4}, \frac{\Lambda_{QCD}}{m_b^3 m_c^2} + \dots\right) \right]$$

 $\succ c_d$  (d = 3, 5, ...) calculable in perturbation theory as a series in  $a_s$ 

> Non perturbative matrix elements of local operators expressed in terms of HQE parameters, whose number grows with powers of  $\Lambda_{QCD}/m$ 

### HQE status and prospects

• High order proliferation of NP parameters [also IR sensitivity to charm mass ( $\log m_c$ ,  $\frac{\Lambda_{QCD}^5}{m_b^3 m_c^2}$ , ... )]

I. Bigi et al 0911.3322, Breidenbachet al 08...

✓ Computed/estimated up order 
$$(\frac{\Lambda_{QCD}^5}{m_b^5})$$

Gremm et al 96, Dassinger et al 14, Mannel et al 10, Heinonen et al 14, Gambino et al. 16...

If included in global fit with *Lowest Lying State* Approximation --sub-percent reduction in  $|V_{cb}|$ , not appreciable at the current level of precision.

Gambino et al. 1606.06174

✓ Part of 
$$\left(\frac{\alpha_s \Lambda_{QCD}^3}{m_b^3}\right)$$
 corrections completed:  $\rho_D^3$ 

Mannel & Pivovarov 1907. 09187

First steps toward transition rates from lattice

Hashimoto 1703.01881, Gambino & Hashomoto 2005.13730 Gambino et al. 2203.11762

Using moments of the dilepton moment q2 spectrum recently been measured for the first time by both Belle (2021) and Belle II (2022)

Fael et al JHEP 02 (2019) 177, Bernlochner et al 2022 **Global HFLAV fit from the theoretical viewpoint** 

✓ includes all 
$$O\left(\alpha_s^2, \frac{\Lambda_{QCD}^2 \alpha_s}{m_b^2}, \frac{\Lambda_{QCD}^3}{m_b^3}\right)$$
 corrections

 $\checkmark$  include 6 NP parameters  $m_b, m_c, \mu_{\pi}^2, \mu_G^2, \rho_D^3, \rho_{LS}^3$ 

 $\checkmark$  moments determine combinations of  $m_b$  &  $m_c$ —additional constraint from external determination of  $m_c$  (sum rules+pert)

Chetyrkin, et al. (2009) 0907.2110

✓ low-scale OPE-compatible masses + other assumptions: *kinetic scheme* 

I.Bigi et al. hep-ph/9704245, hep-ph/940410, Benson et al. hep-ph/0302262, Gambino & Uraltsev hep-ph/0401063

$$|V_{cb}| = (42.19 \pm 0.78) \times 10^{-3}$$

$$\chi^2/ndf = 0.32$$

# Exclusive $|V_{cb}|$ determination

- Systematic approach exploiting dispersion relations & unitarity bounds
  - ✓ Boyd-Grinstein-Lebed 1994 (BGL)—FF expressed as a series (versions differ e.g. by order of truncation)
  - ✓ Caprini-Lelloch-Neubert 1997 (CLN)—reduce the number of parameters by HQS relations
  - Bourrely-Caprini-Lellouch 2008 (BCL)--improves the convergence of BGL series by removing an unphysical singularity at the pair production threshold and correcting the large q<sup>2</sup> behavior<sup>10</sup>
- ✓ Fit: lattice calculations at non-zero recoil ( $\omega \neq 1$ ) + exp

the role of parameterization becomes less relevant: the extrapolation to zero recoil reduces to an interpolation between experimental results and different theory points.

$$|V_{cb}| \times 10^3 = 39.36(68)$$

FLAG Review 2021 [arXiv:2111.09849]

~ 
$$2.7\sigma$$
 difference excl./incl.

INCLUSIVE:

$$|V_{cb}| \times 10^3 = 42.16(50)$$

Bordone et al., Phys.Lett.B [2107.00604]

# Inclusive |V<sub>ub</sub>|



Need experimental phase space cuts to reduce large  $b \rightarrow c$  background;



Threshold phase space region dominance

- Final gluon radiation strongly inhibited: soft and collinear singularities
- Iarge logarithms  $a_s^n \log^{2n}(2 E_X/m_X)$  (E<sub>X</sub> << m<sub>X</sub>)
   to be resummed at all orders in PT
- non-perturbative effects related to a small vibration of the *b*-quark in the B meson (Fermi motion) enhanced

### Theoretical approaches

#### redictions based on parameterizations of shape function

✓ several cuts Bosch, Lange, Neubert, Paz (BLNP), Gambino, Giordano, Ossola, Uraltsev (GGOU), neural network fit (Gambino, Healey, Mondino) Bauer, Ligeti, Luke (BLL)

Lepton momentum spectrum

Leibovich, Low, Rothstein (LLR), Lange, Neubert, Paz (LNP)

✓ global fit

Ligeti, Stewart, Tackmann

✓ predictions led by anlytical structure of resummed pQCD Andersen, Gardi (DGE), Aglietti, Di Lodovico, Ferrera, GR (ADFR) Fit kinematic distributions and measure partial BF

$$|V_{ub}| = \sqrt{\frac{\Delta \mathcal{B}(B \to X_u \,\ell^+ \,\nu_\ell)}{\tau_B \cdot \Delta \Gamma(B \to X_u \,\ell^+ \,\nu_\ell)}}$$

Result for most inclusive

4 predictions of the

3 phase-space regions

Phase-space region  $M_X < 1.7 \,\text{GeV}$   $M_X < 1.7 \,\text{GeV}, q^2 > 8 \,\text{GeV}^2$  $E_\ell^B > 1 \,\text{GeV}$ 



# **Inclusive decays**



Martinov,

MITP 2022

Belle II

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#### **Prospects**

Inclusive hadronic tagged analysis

Start from **Belle strategy**: signal/background modeling, BDT/NN selection,

Improved hardware/software + larger data set (ultimately 50 ab<sup>-1</sup>)

	Statistical	Systematic	Total Exp	Theory	Total
		(reducible, irreducible)			
$5 \text{ ab}^{-1}$	1.1	(1.3, 1.6)	2.3	2.5 - 4.5	3.4 - 5.1
$50 \text{ ab}^{-1}$	0.4	(0.4, 1.6)	1.7	2.5 - 4.5	3.0 - 4.8
				The Belle II	Physics Book

Model independent/global fit: differential spectra measurement:  $q^2$ ,  $m_X$ , E

### $|V_{ub}|$ exclusive determination

 $\Box$  Traditionally extracted by the decay  $B \rightarrow \pi \ell v$  (only a single form factor in massless limit)



$$|V_{ub}| = 3.63(14) \times 10^{-3}$$

1.5-2 $\sigma$  difference, still reduced with DM approach

Source	$10^{-3} \times  V_{ub} $ EXCL	USIVE
LQCI	)	• from the semileptonic $B \to \pi$ decays
Fermilab/MILC [33, 34]	$3.72 \pm 0.16$	
RBC/UKQCD [35]	$3.61\pm0.32$	$ V_{ub}  \cdot 10^3 = 3.62 \pm 0.47$
combination w/ Pade approx. $[5]$	1] $3.53 \pm 0.08_{\rm stat} \pm 0.06_{\rm syst}$	
HFLAV [8]	$3.70\pm0.10_{\rm stat}\pm0.12_{\rm syst}$	• from the semileptonic $B_s \to K$ processes
LCSF		
Duplancic et al. [16]	$3.5 \pm 0.4 \pm 0.2 \pm 0.1$	$ V_{ub}  \cdot 10^3 = 3.77 \pm 0.48$
Imsong et al. $[21]$	$3.32\substack{+0.26\\-0.22}$	
this work	$3.28\substack{+0.33\\-0.28}$	by averaging
LCSR + I	.QCD	
HFLAV [8]	$3.67\pm0.09_{\rm stat}\pm0.12_{\rm syst}$	$ V_{ub}  \cdot 10^3 = 3.69 \pm 0.34$
this work	$3.77\pm0.15$	
	Only $I\sigma$ from the model of th	ost recent Belle result on inclusive  Vub
		Martinelli et al.
D.Leijak et al JHEP 07 (2021)		2202.10285
D. MELIK FULLOLUSE ZUZI		

#### Prospects for $B \rightarrow \pi \ell \nu$ at Belle II

Ongoing **tagged** and **untagged** analyses with **more statistics** Potential to **reduce uncertainty on**  $|V_{ub}|$  by a significant margin



# Conclusions

- ✓ LFNU: progress in lattice and global fits
  - ✓ Patterns emerge in EFT but no definite BSM yet
  - Surviving exp scrutiny, but no measurement alone claim discovery
- ✓  $|V_{cb}| \& |V_{ub}|$  puzzles incl/excl getting closer; almost there (?)
- Next decade: Belle II major player (& LHCb powerful ally)

