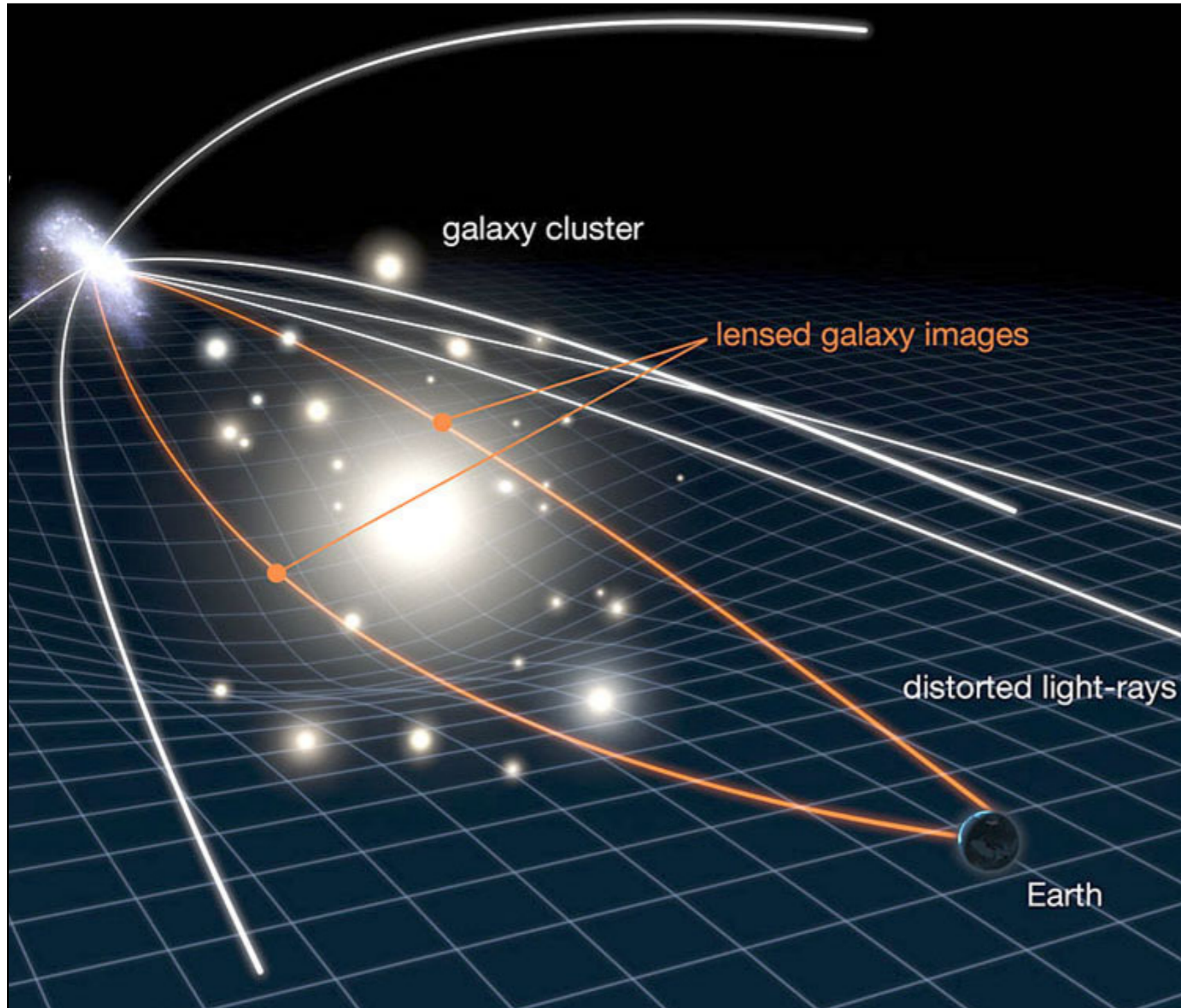


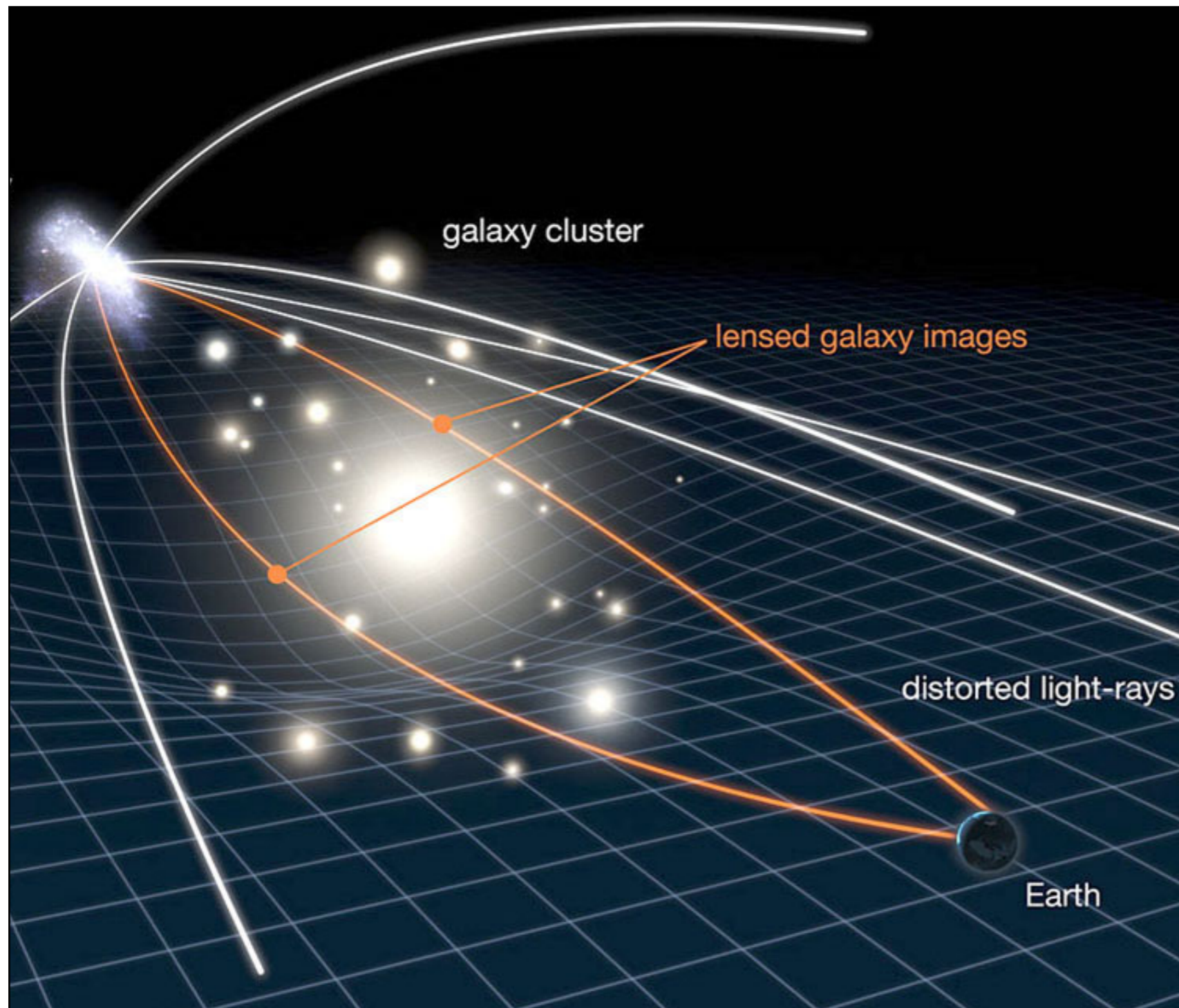


# LENSING OF GRAVITATIONAL WAVES

# GRAVITATIONAL LENSING



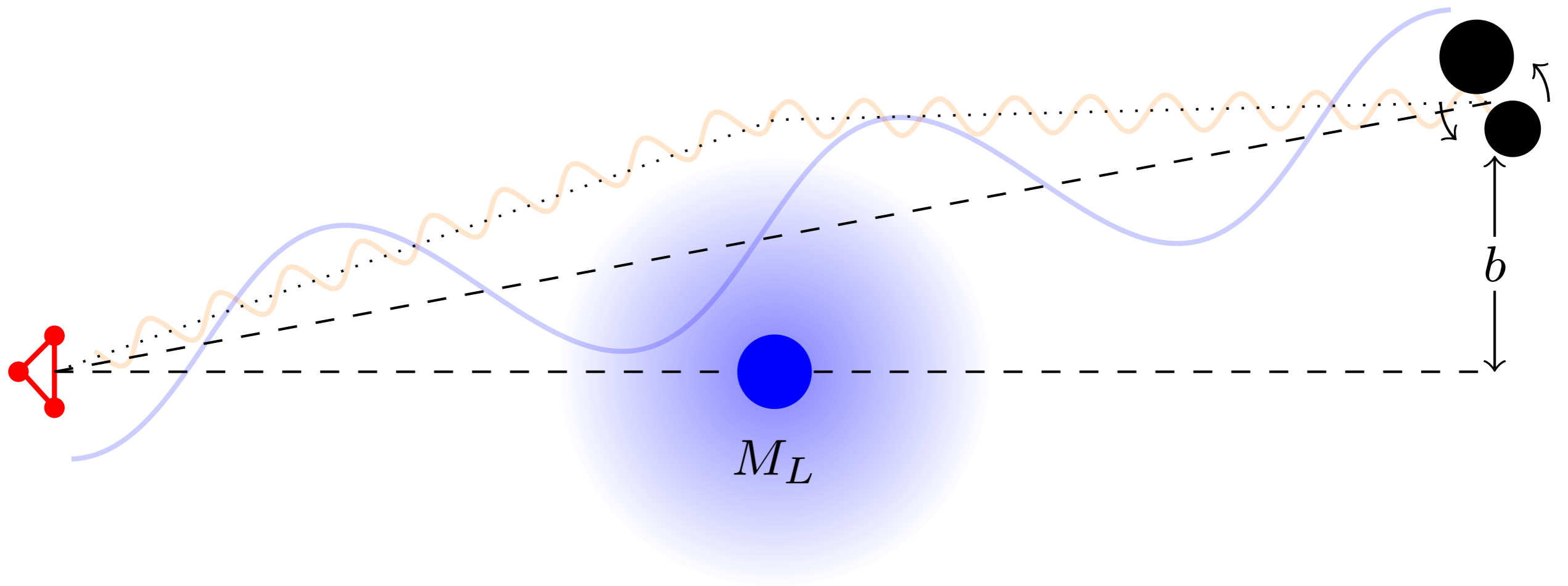
# GRAVITATIONAL LENSING



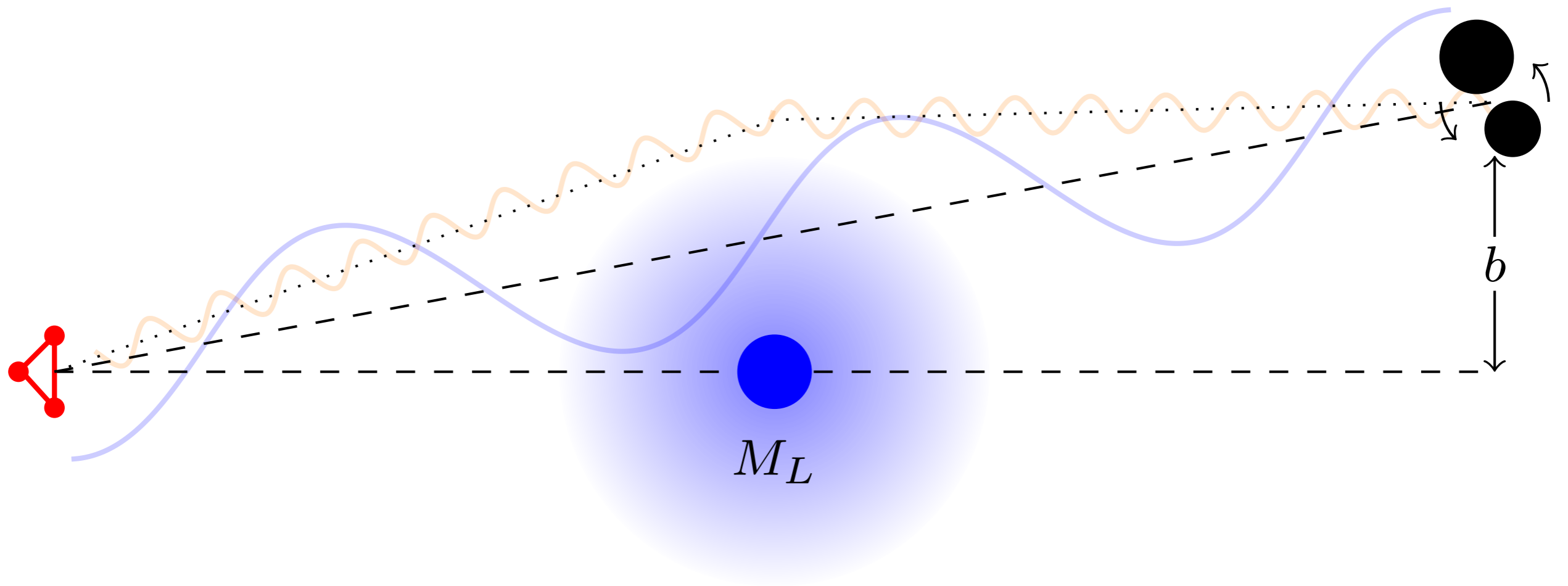
## EM Lensing

- Probe Dark Matter
- Measure  $H_0$
- See farther/lighter objects
- Exoplanets
- Primordial BHs

# GW LENSING



# GW LENSING



Main parameters of interest:  $b$ ,  $M_L$ ,  $\lambda$



# LENSING LANDSCAPE

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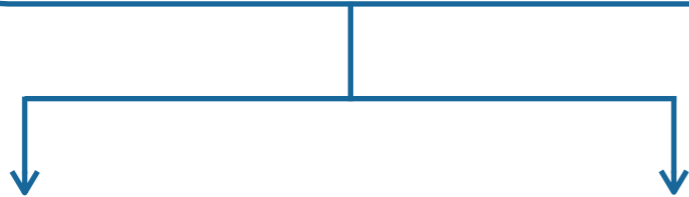
Geometric Optics

$$\lambda \ll M_L$$

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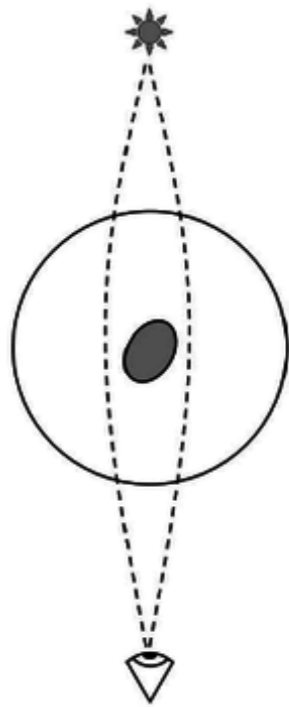
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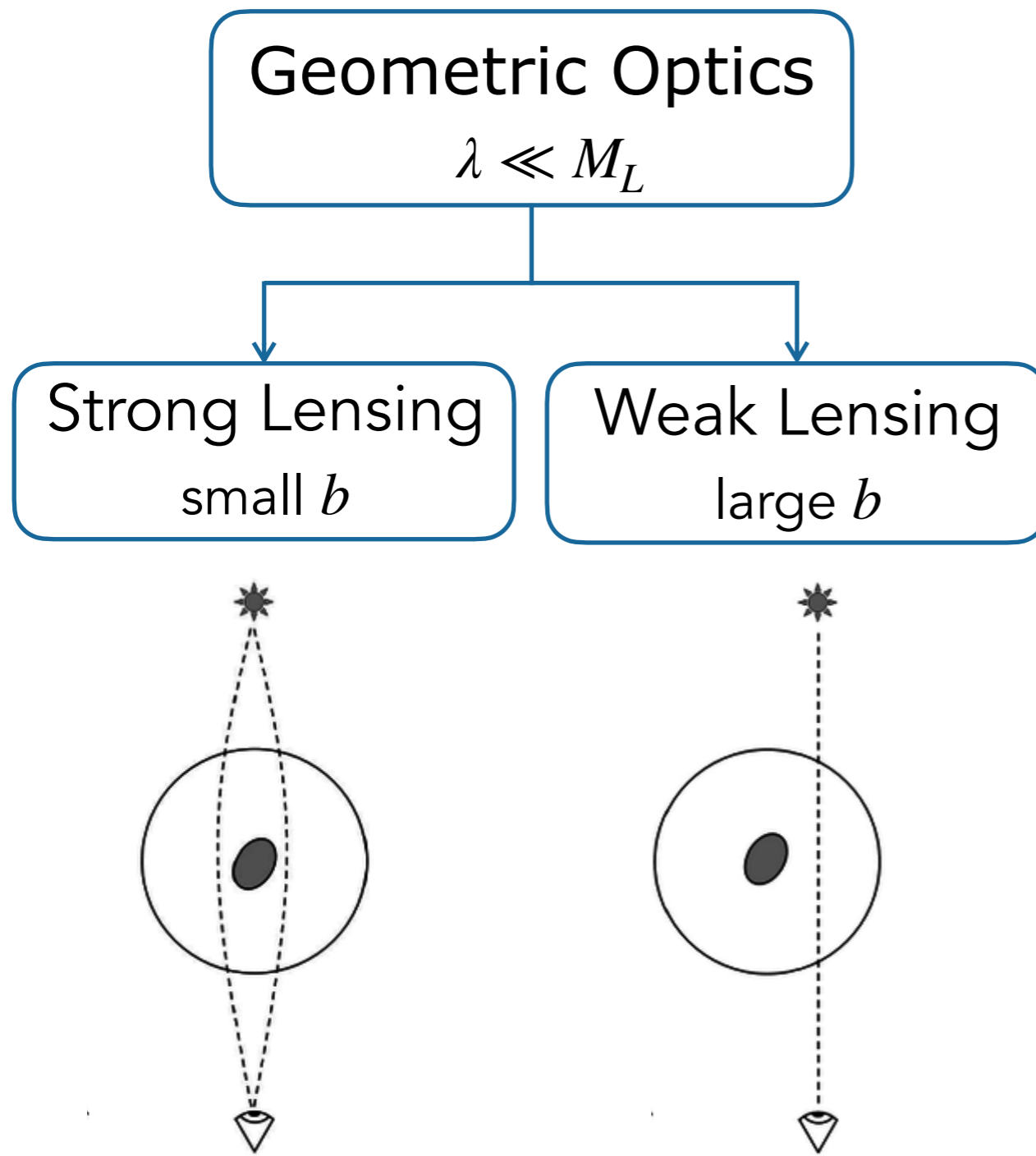
$$\lambda \ll M_L$$

Strong Lensing

small  $b$



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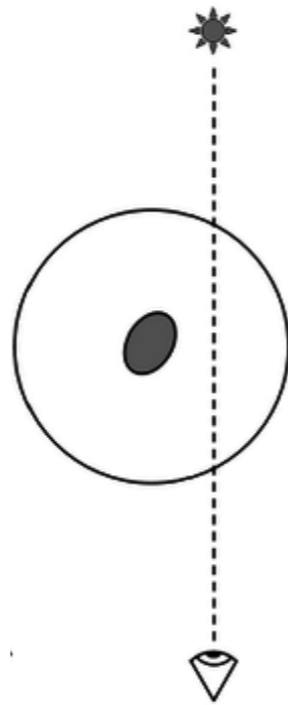
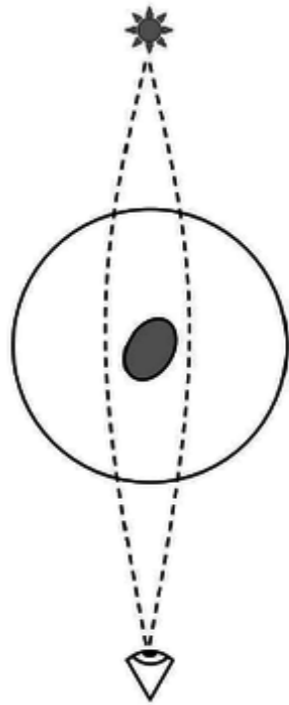
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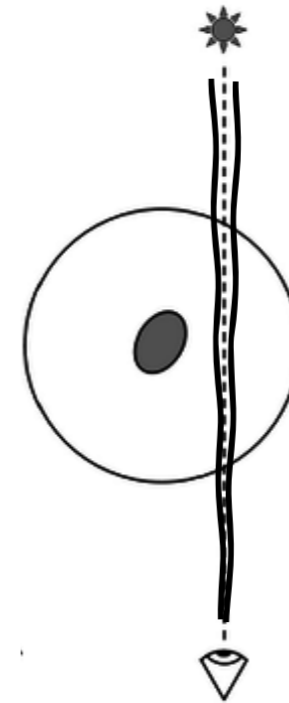
Weak Lensing

large  $b$

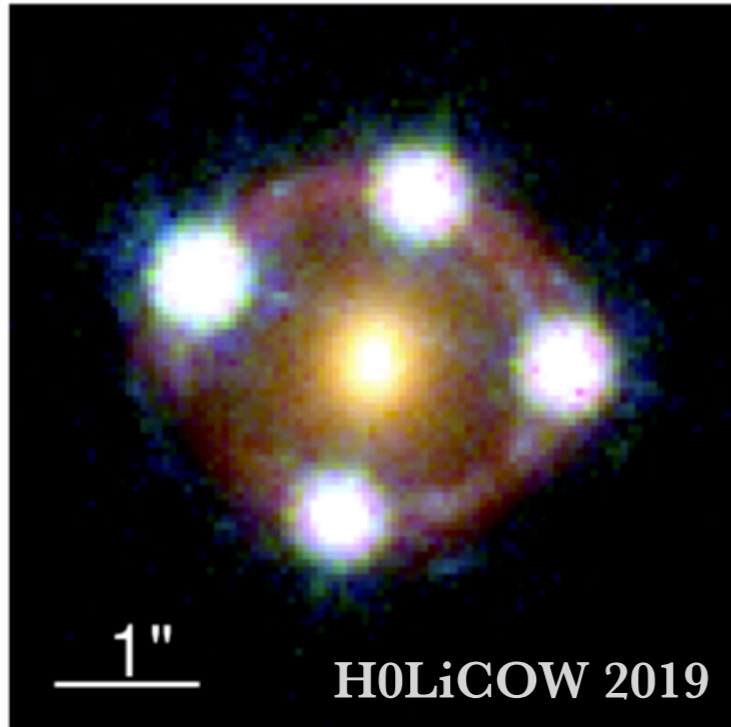


Wave Optics

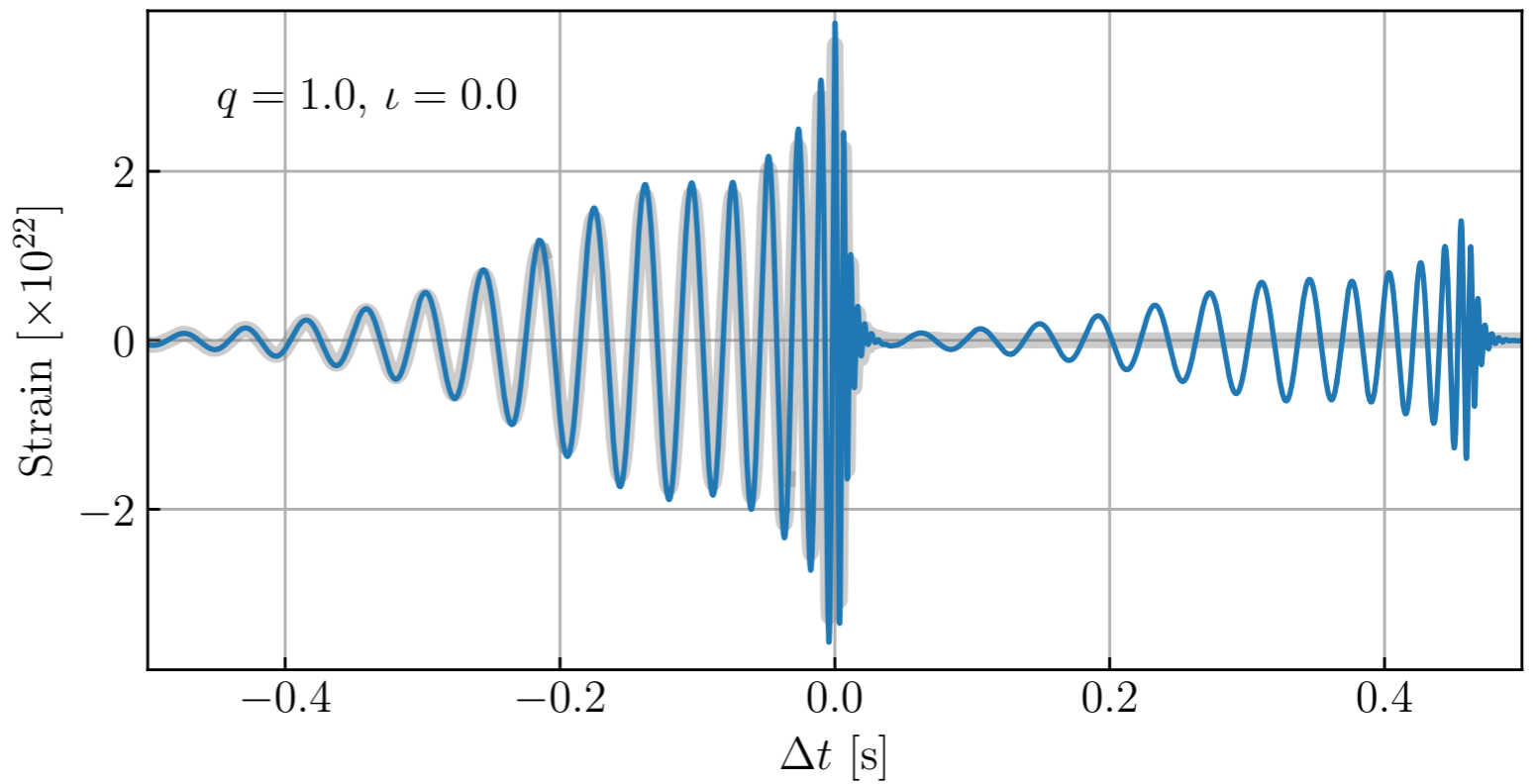
$$\lambda \sim M_L$$



# GW STRONG LENSING

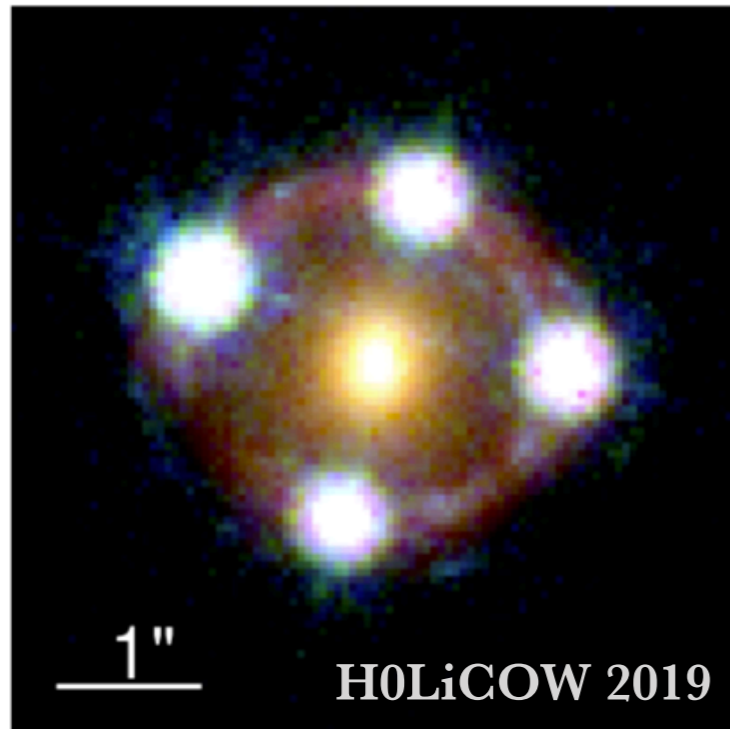


(c) HE 0435-1223

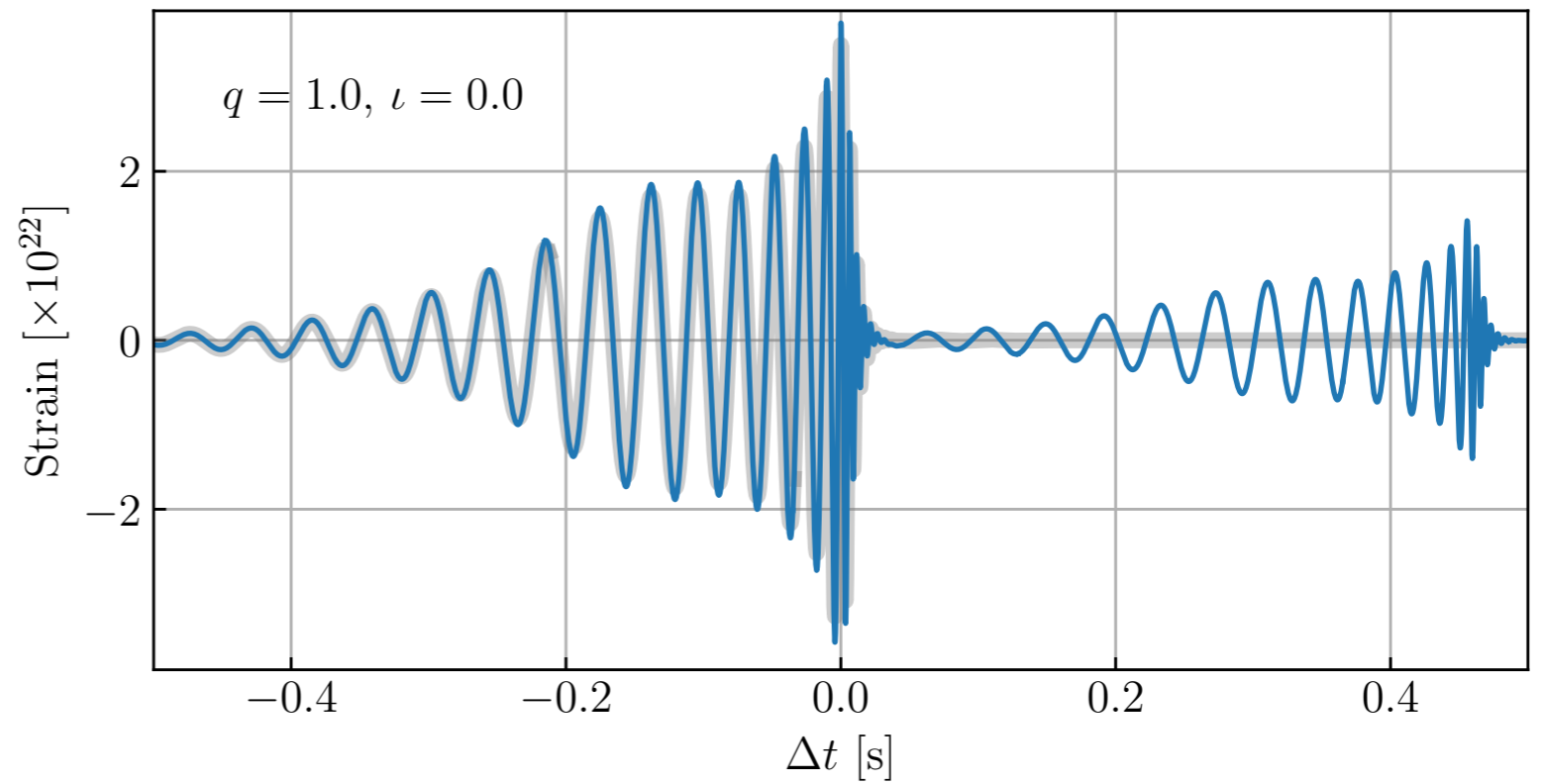


Ezquiaga, Holz, Hu, Lagos+ 2020

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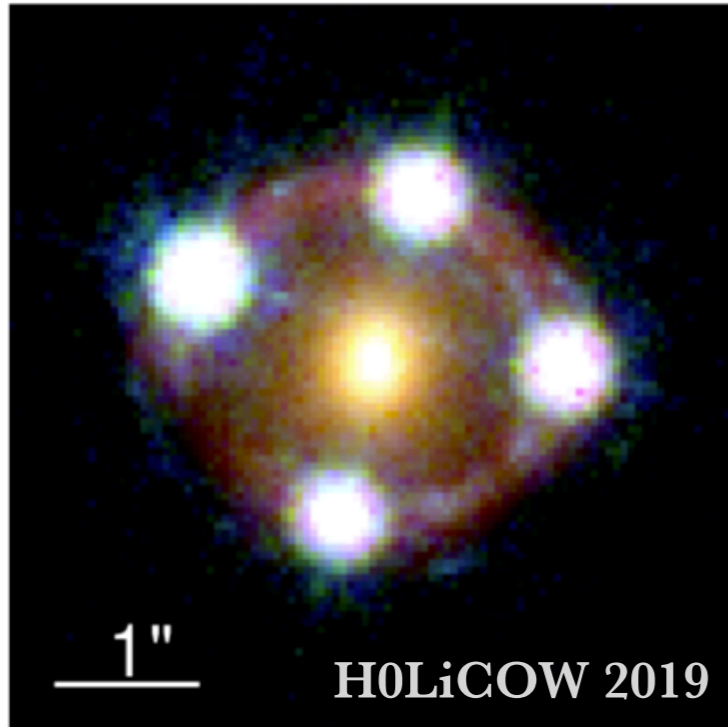
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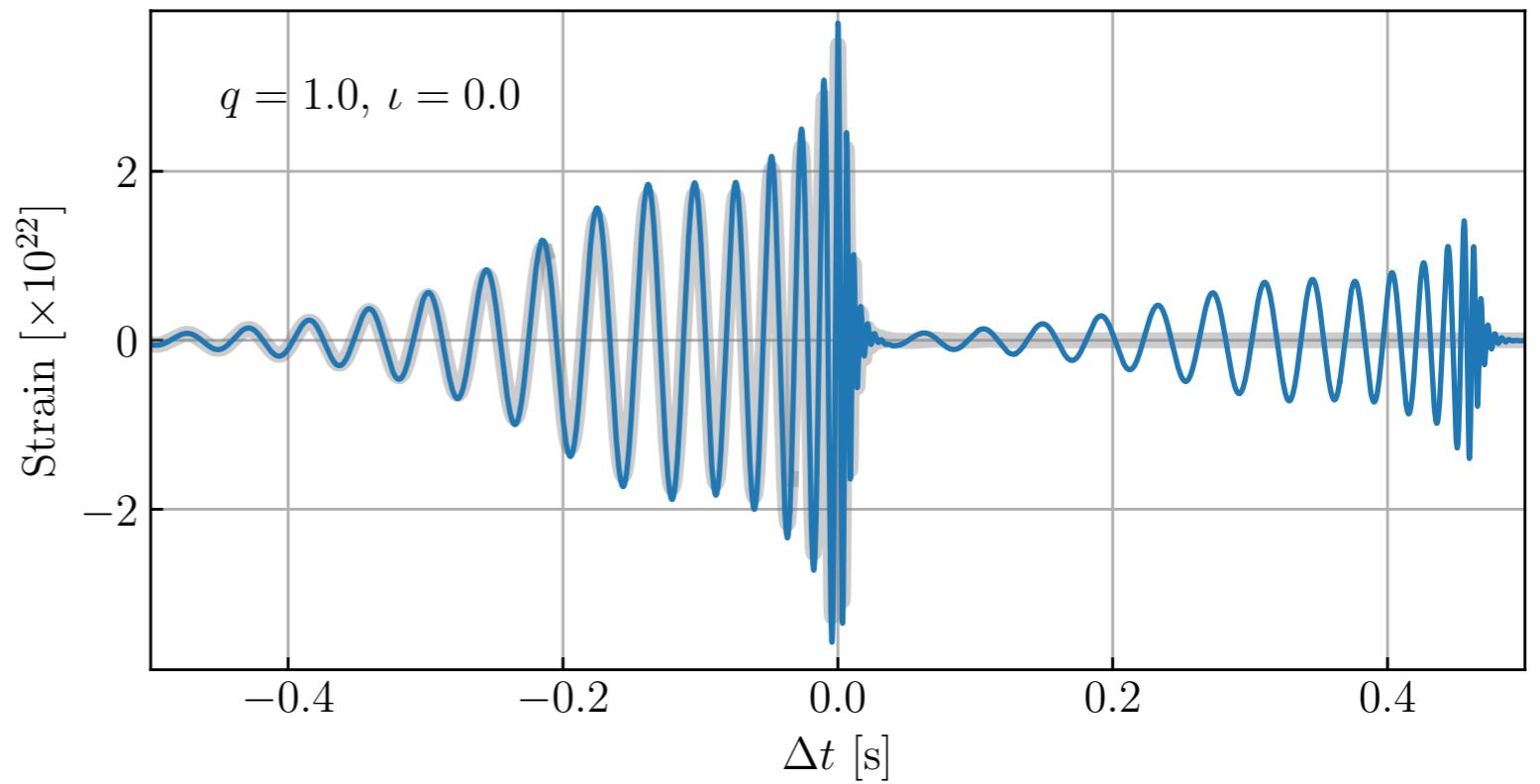
Ezquiaga, Holz, Hu, Lagos+ 2020

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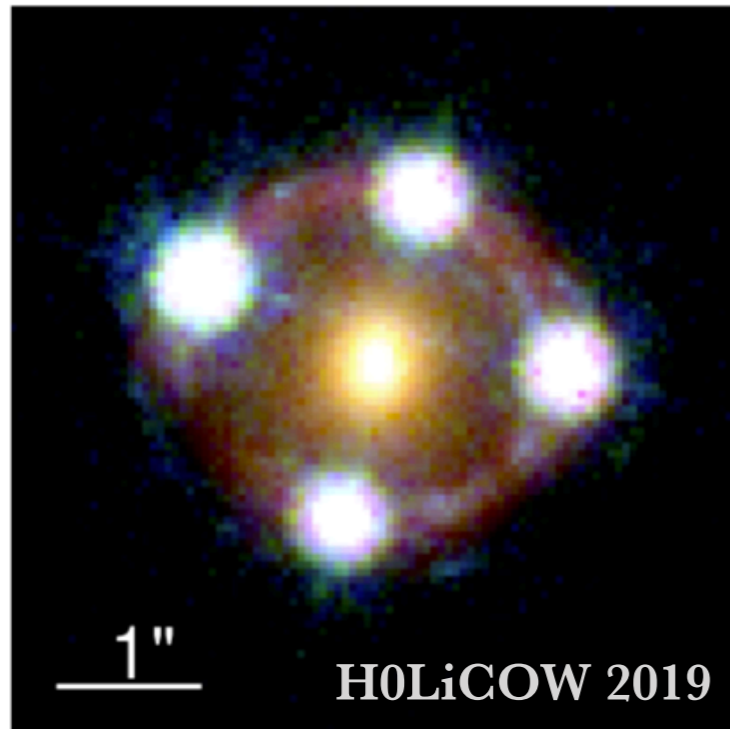
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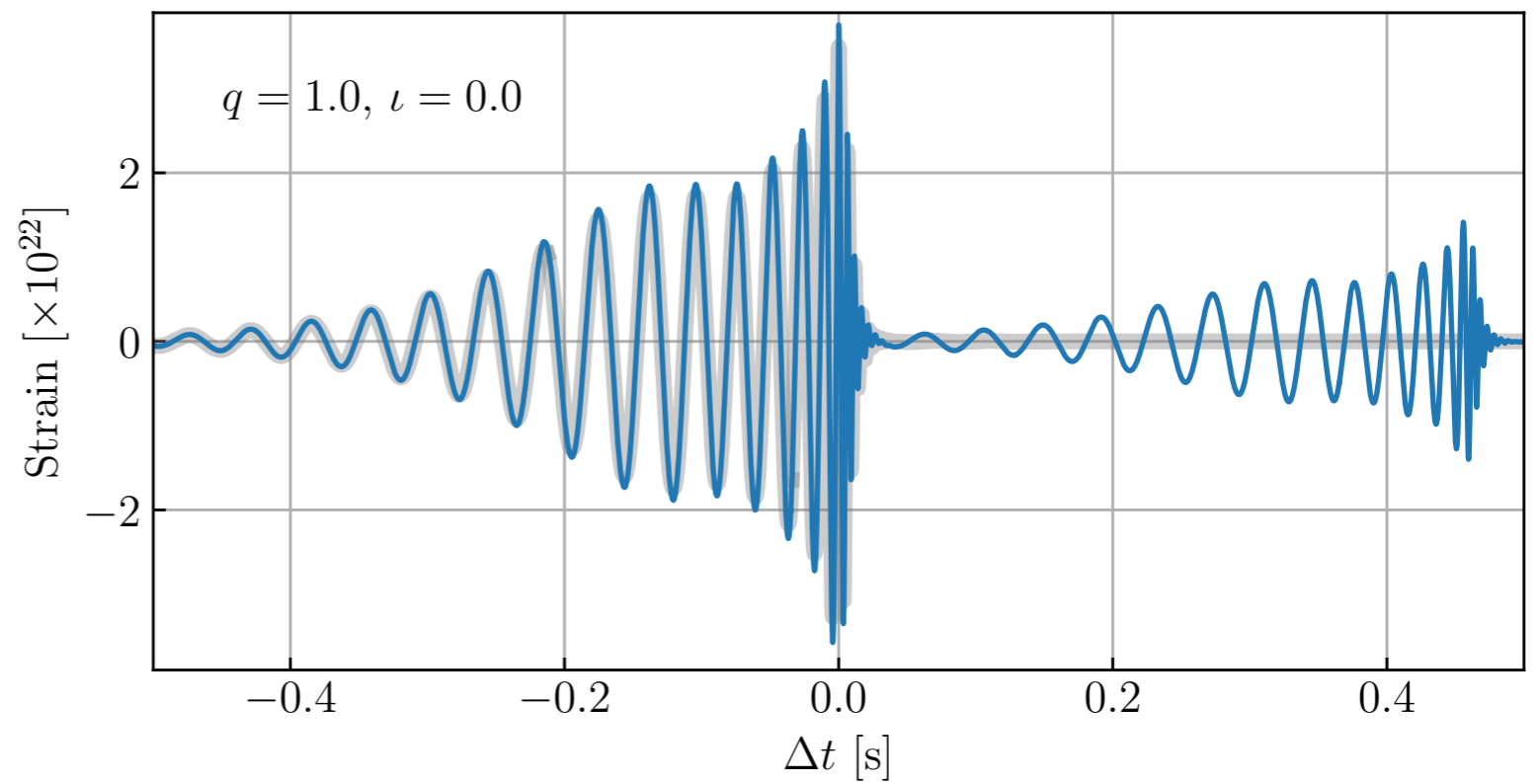
Ezquiaga, Holz, Hu, Lagos+ 2020

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- Science:

# GW STRONG LENSING



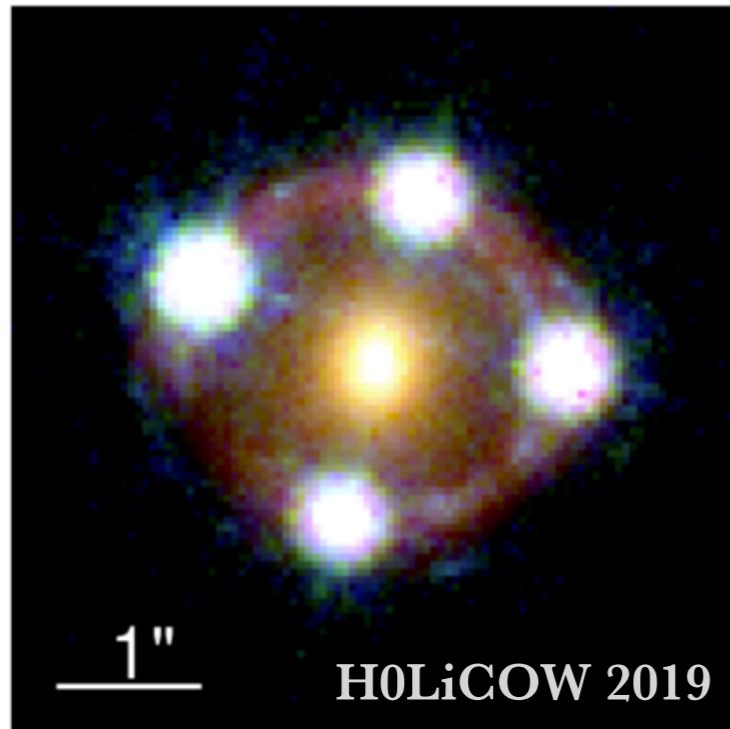
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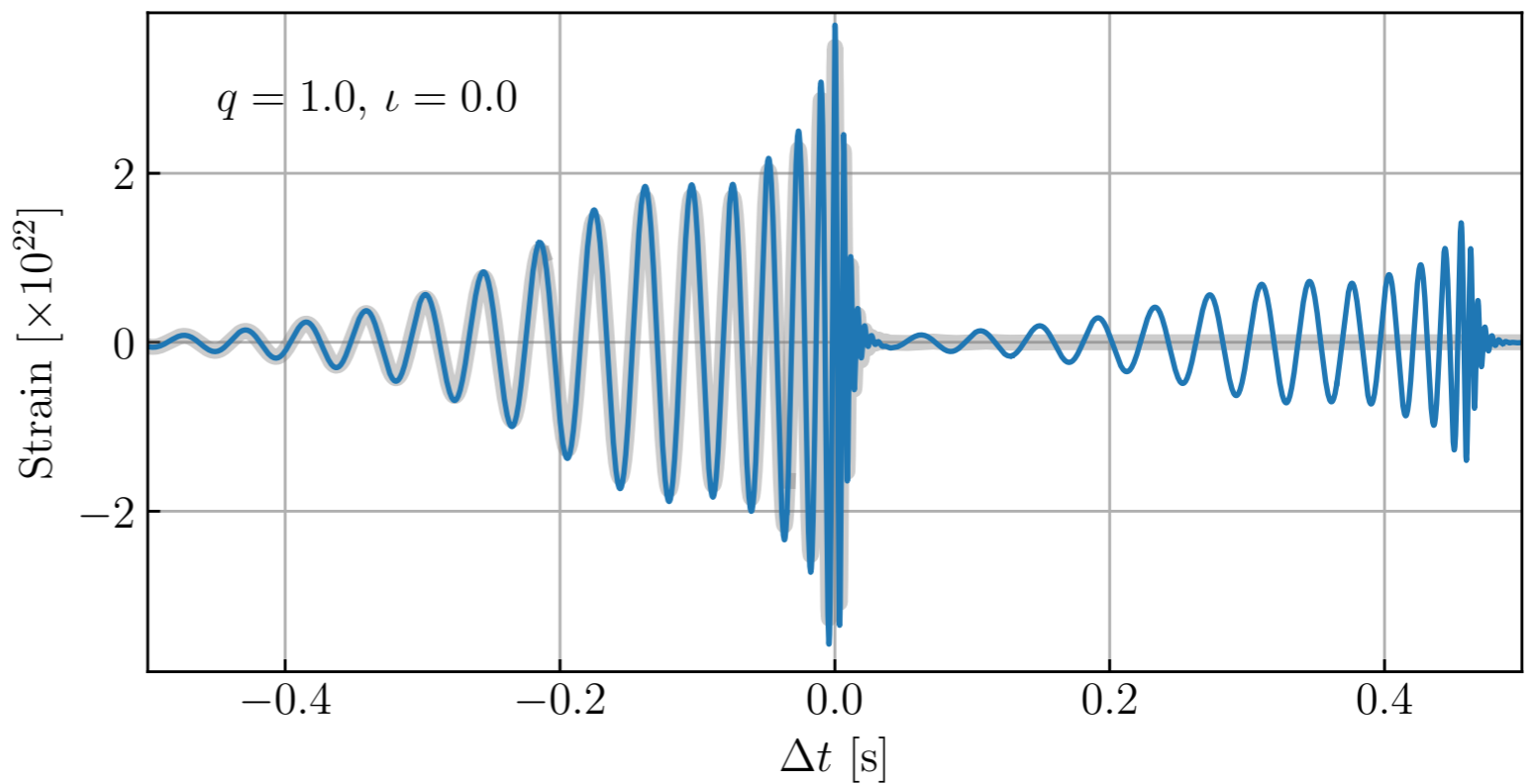
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  - DM distribution

# GW STRONG LENSING



(c) HE 0435-1223

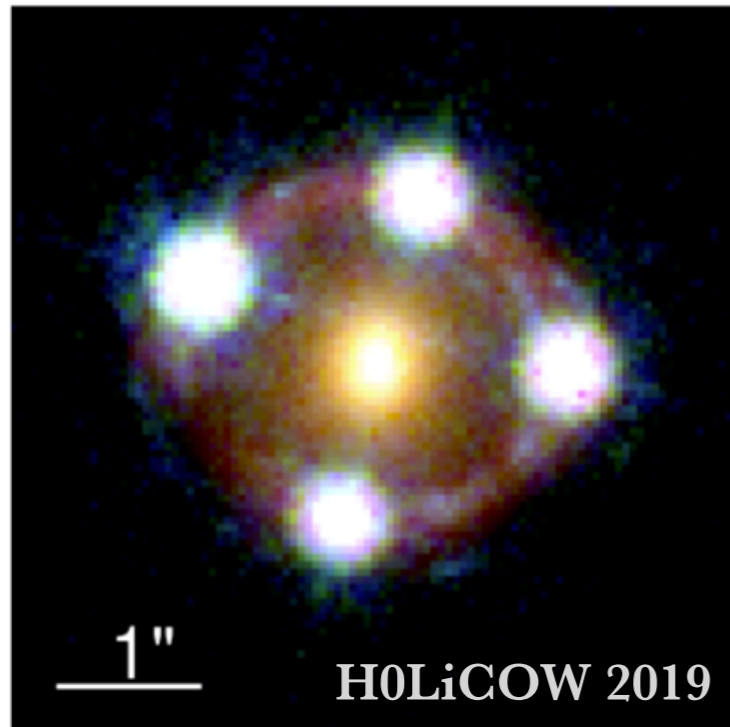


Ezquiaga, Holz, Hu, Lagos+ 2020

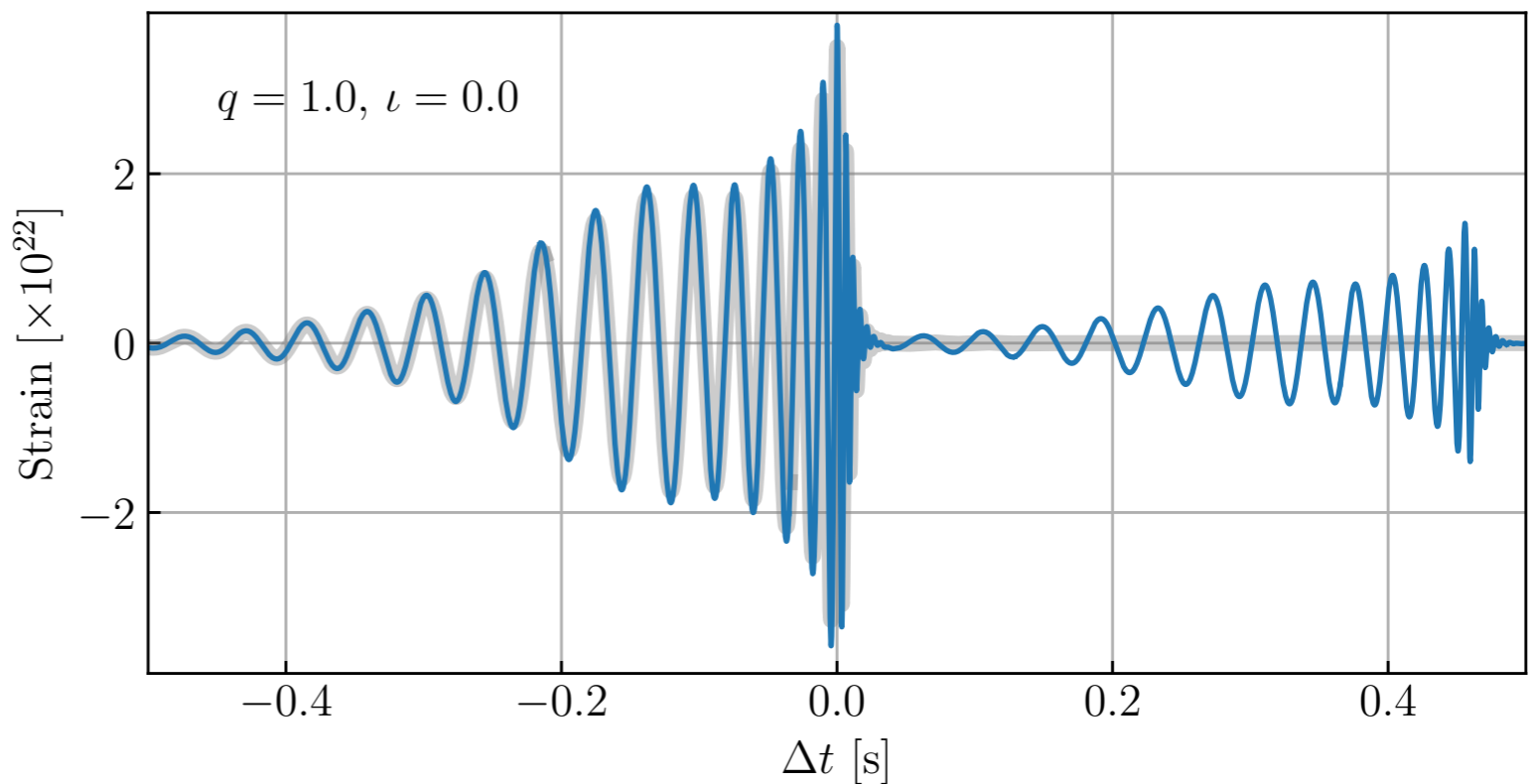
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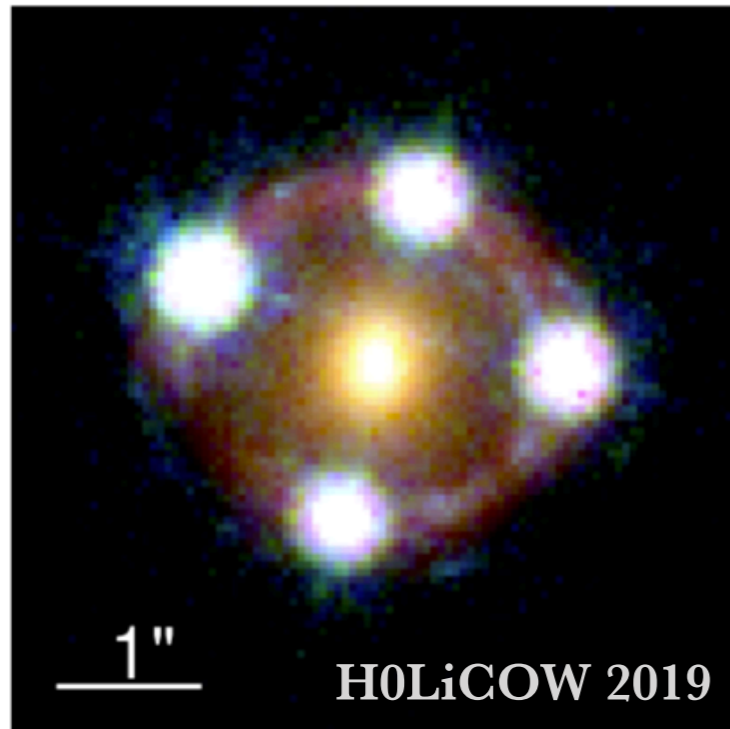
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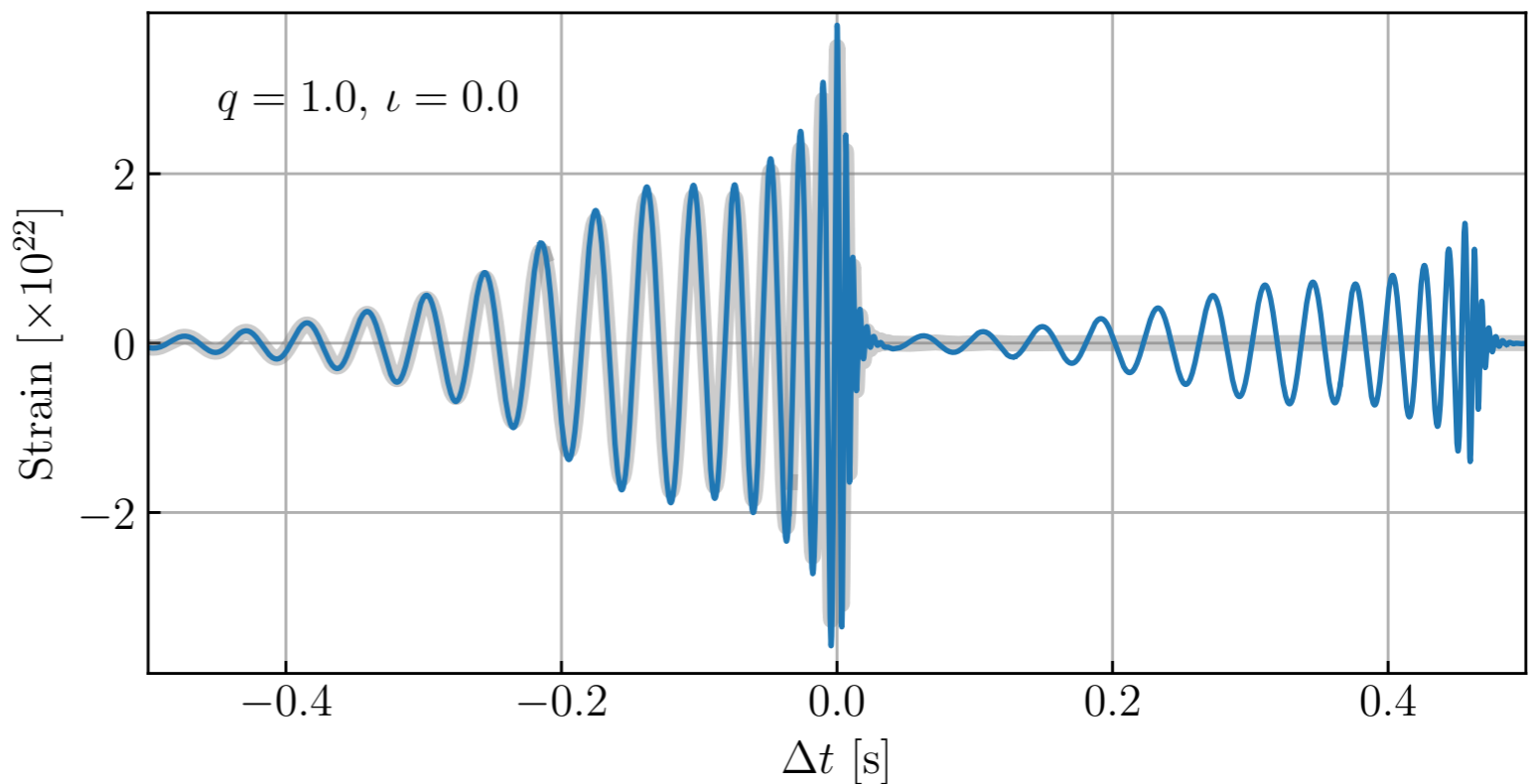
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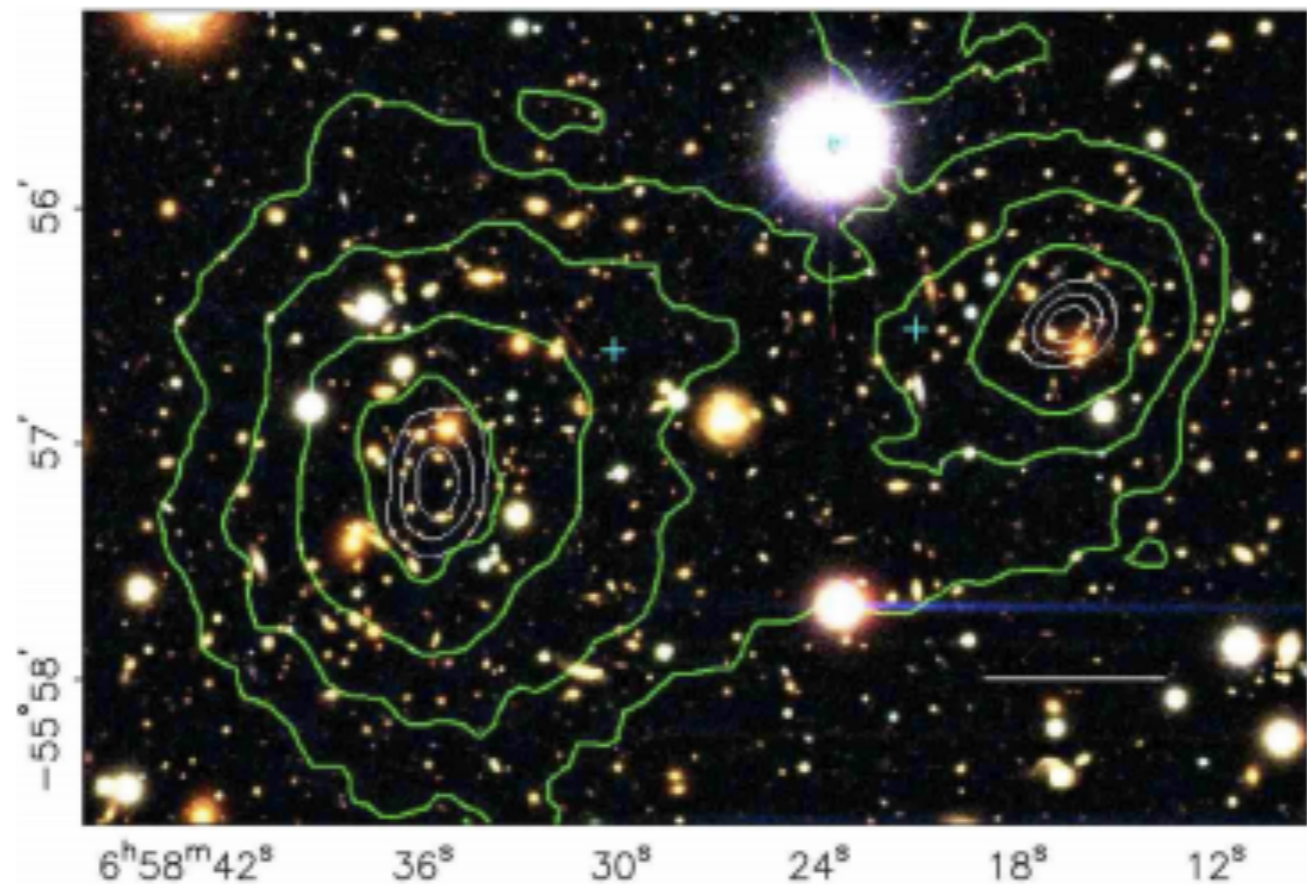
(c) HE 0435-1223



Ezquiaga, Holz, Hu, Lagos+ 2020

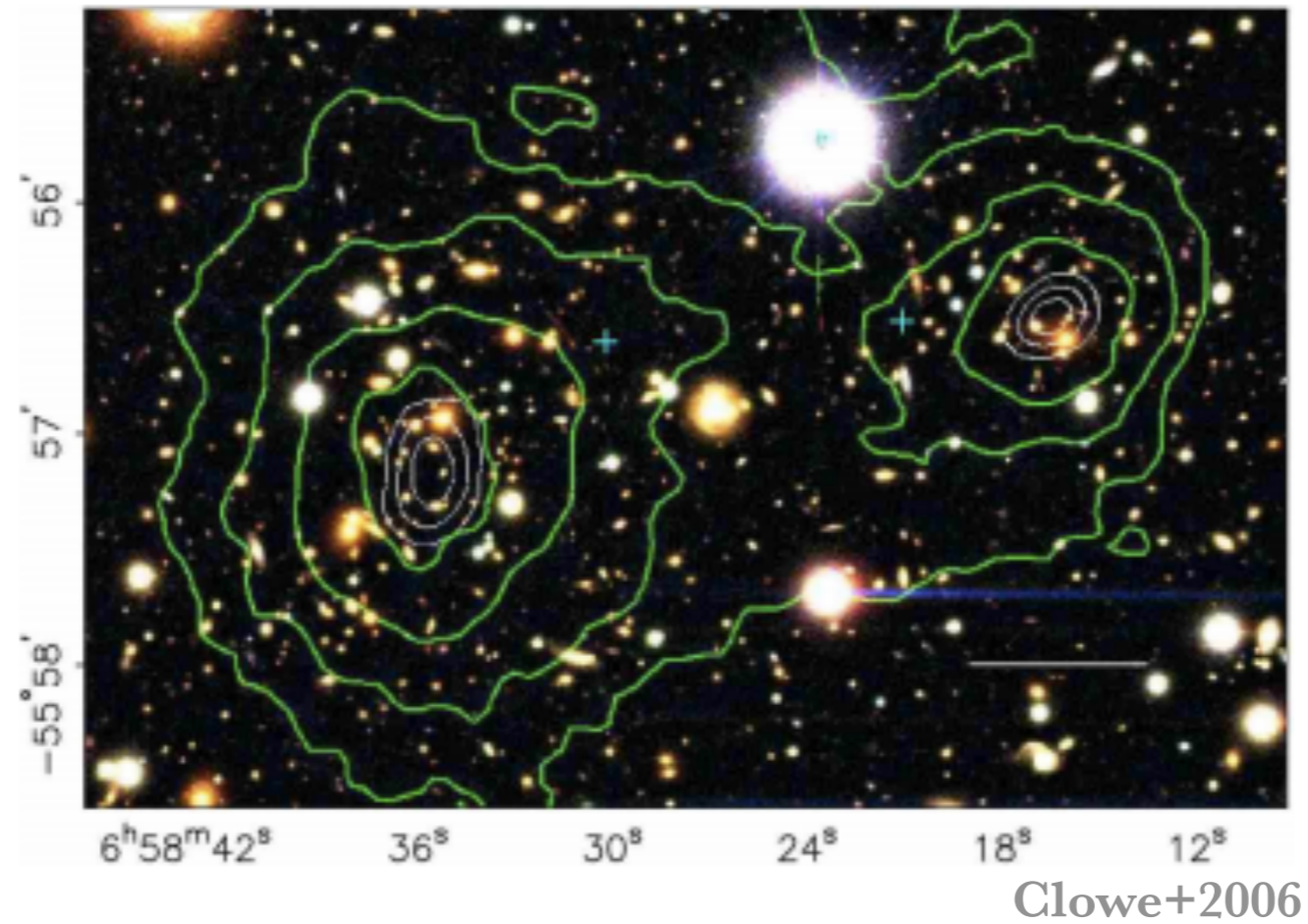
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  - Better localization and polarization (combine multiple time-delayed events) [Hannuksela+2020; Goyal+2020]
- Phase shift signature creates distortions for unequal mass ratios (IMRs, EMRIs) [Dai+2007; Ezquiaga, Holz, Hu, Lagos+2020; Wang+2021; Vijaykumar+2022]

# GW WEAK LENSING



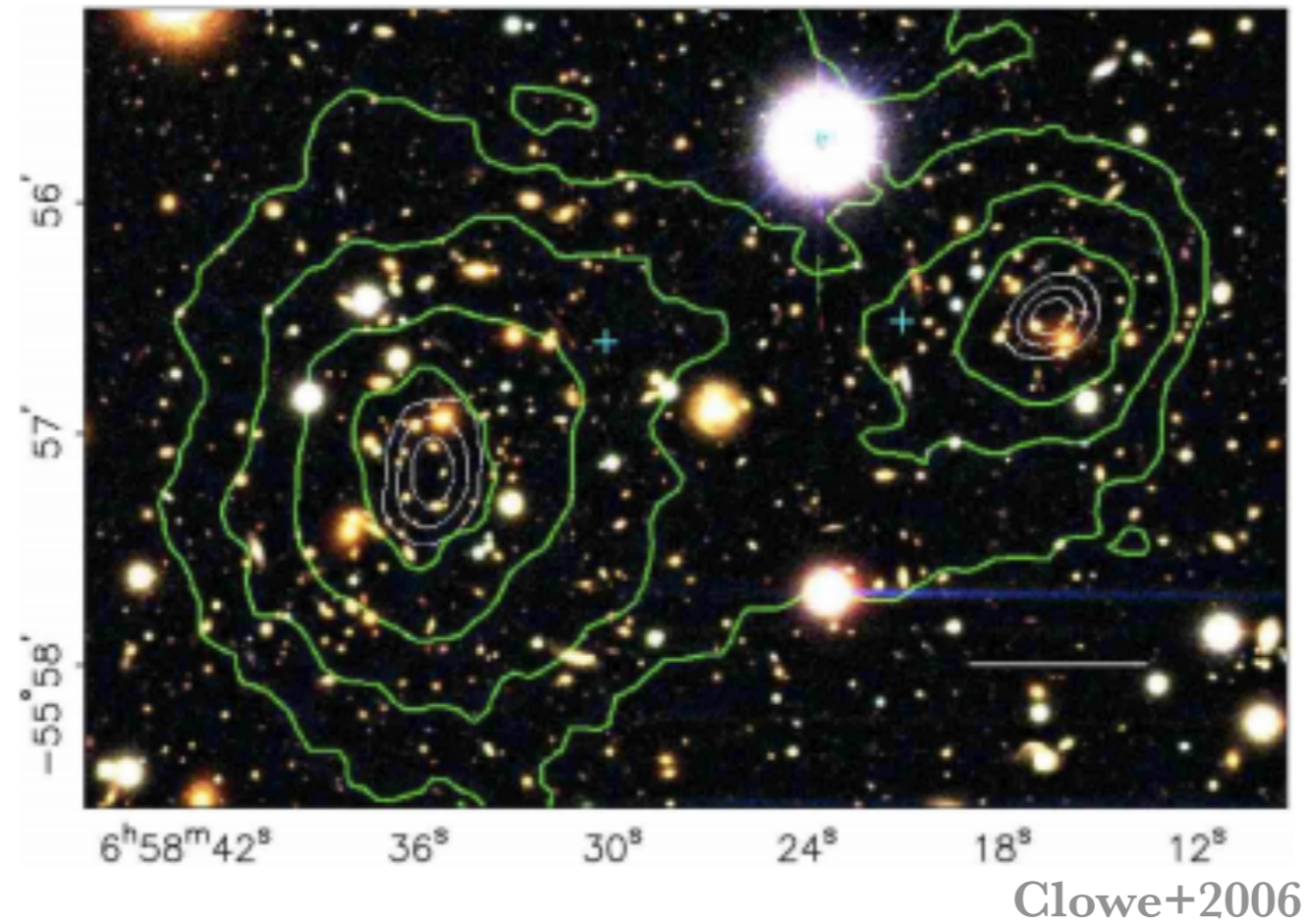
Clowe+2006

# GW WEAK LENSING



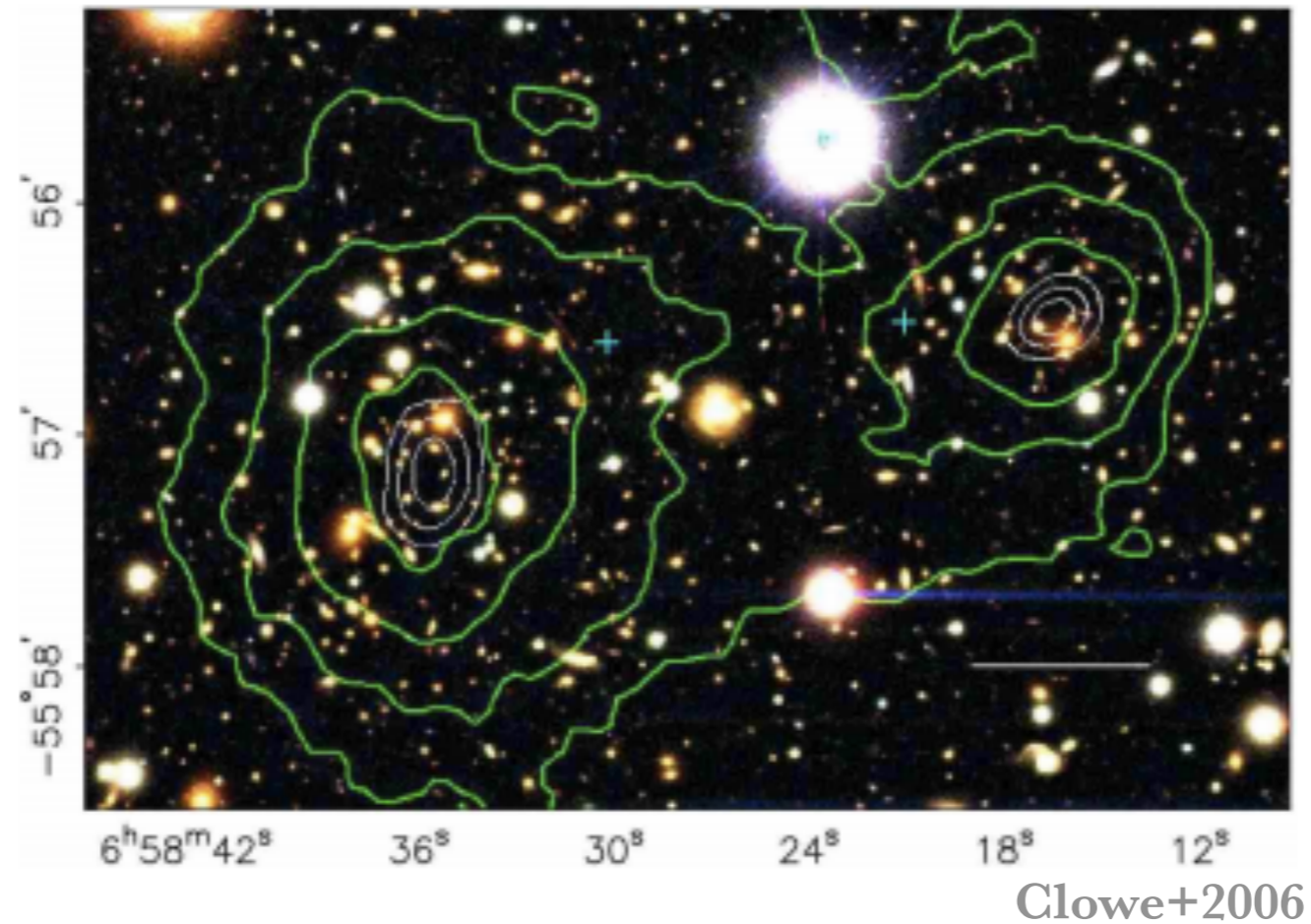
- Single image with small magnification:  $d_L^{obs} = d_L(z; H_0, \Omega_m) \times (1 - \kappa)$

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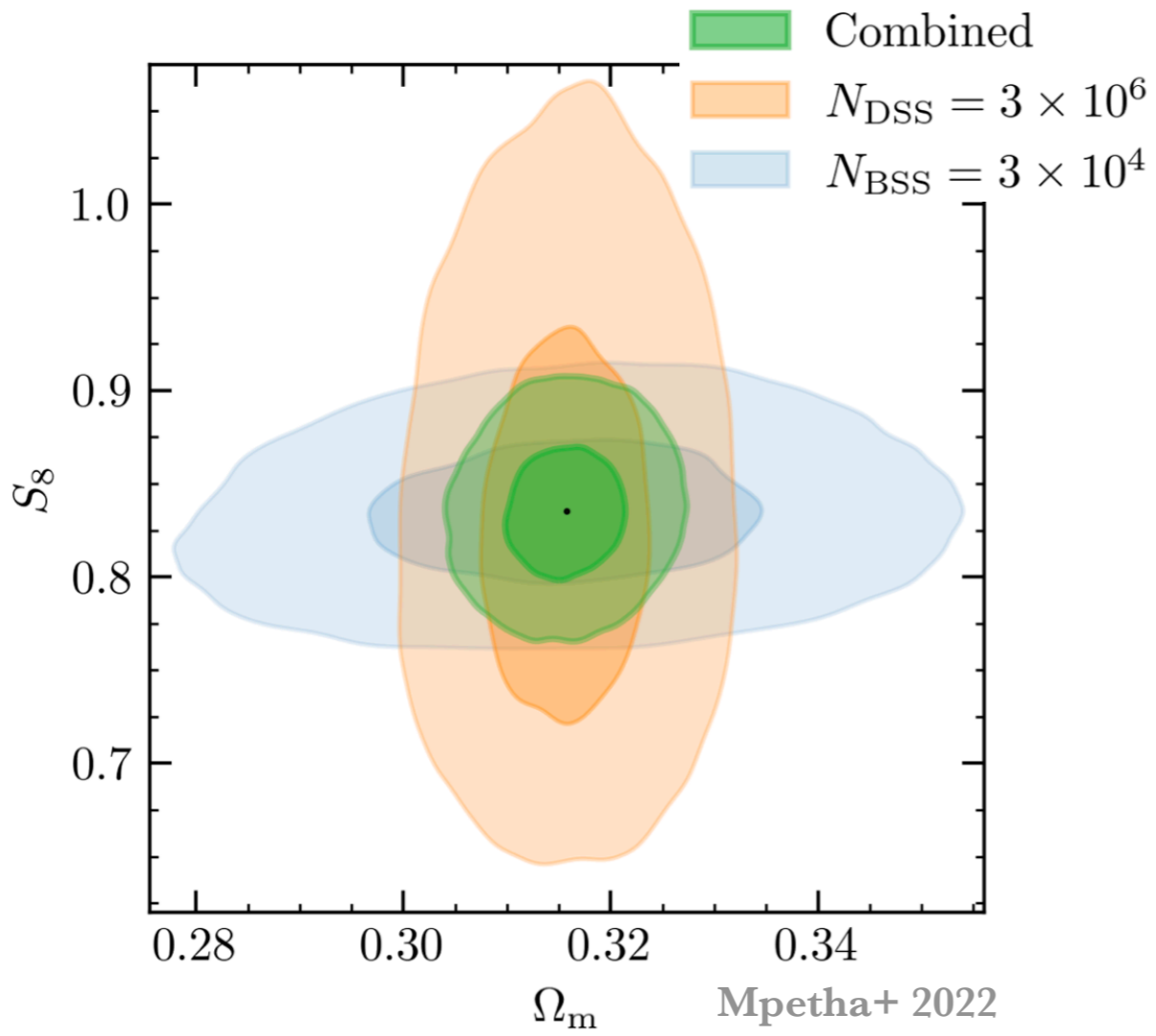
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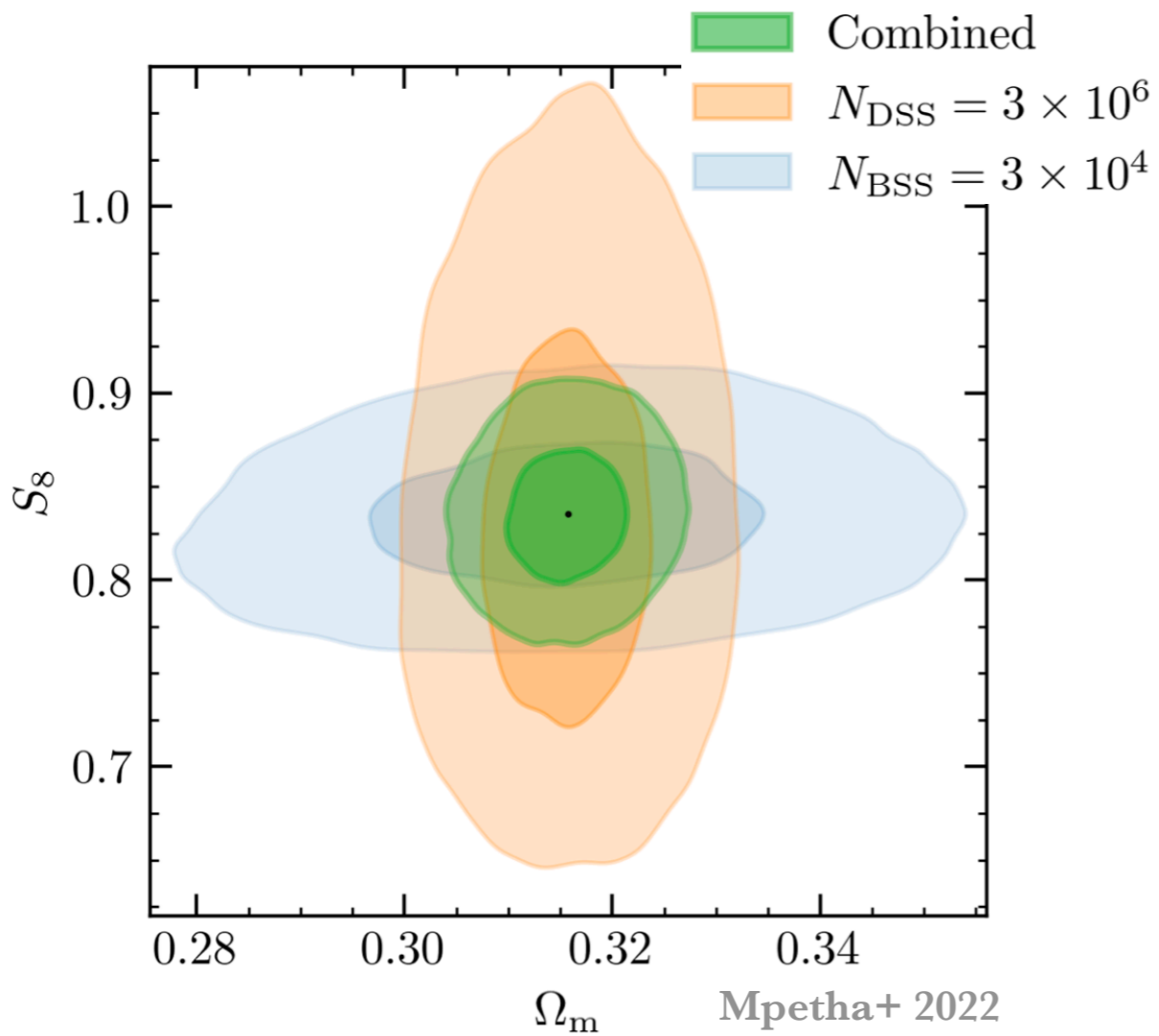


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- Ideal case: GW distances with angular correlations +  $z$  [Cutler+2009; Shang+2010, Congedo+2019; Mpetha+ 2022]

# GW WEAK LENSING



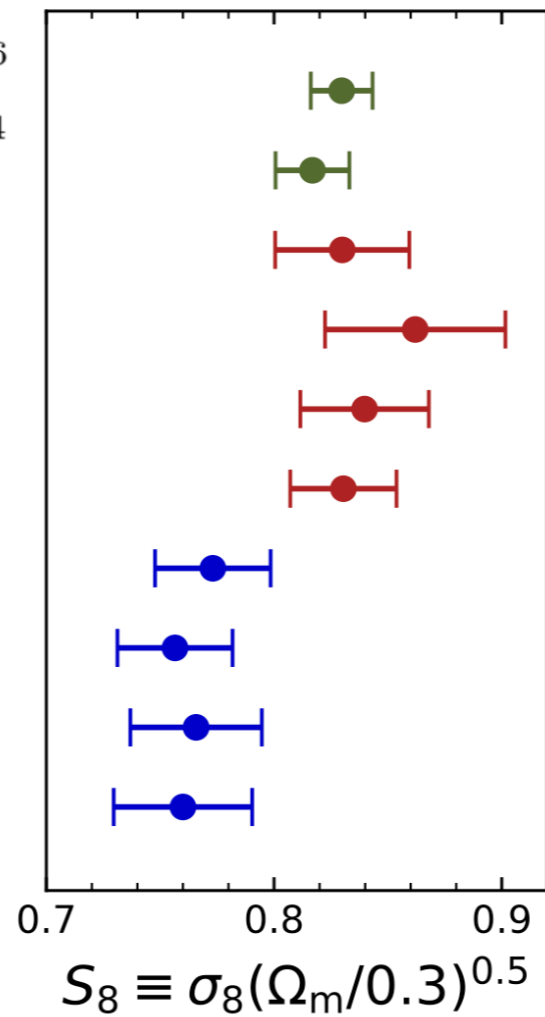
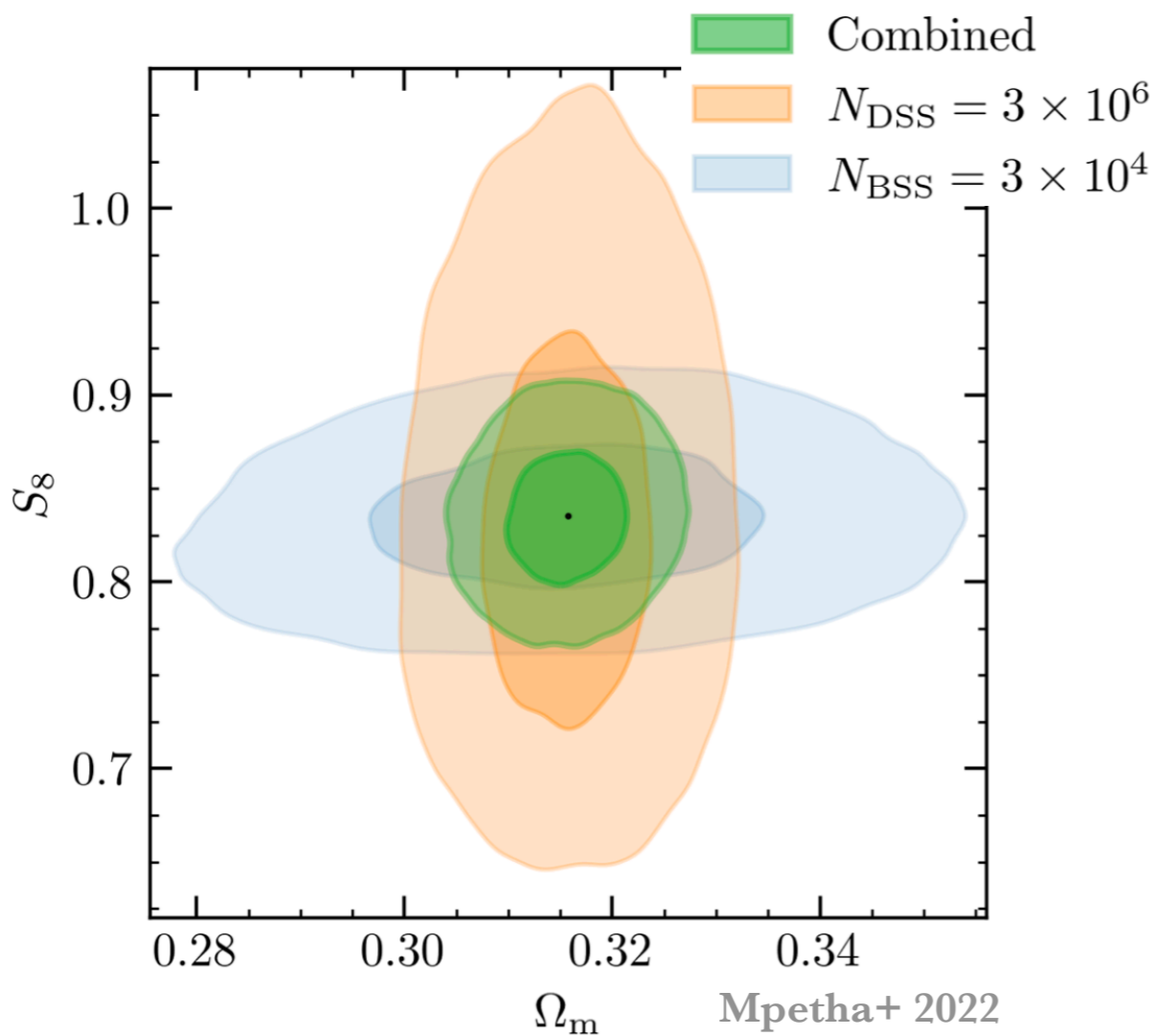
# GW WEAK LENSING



- Independent measurement with less systematics



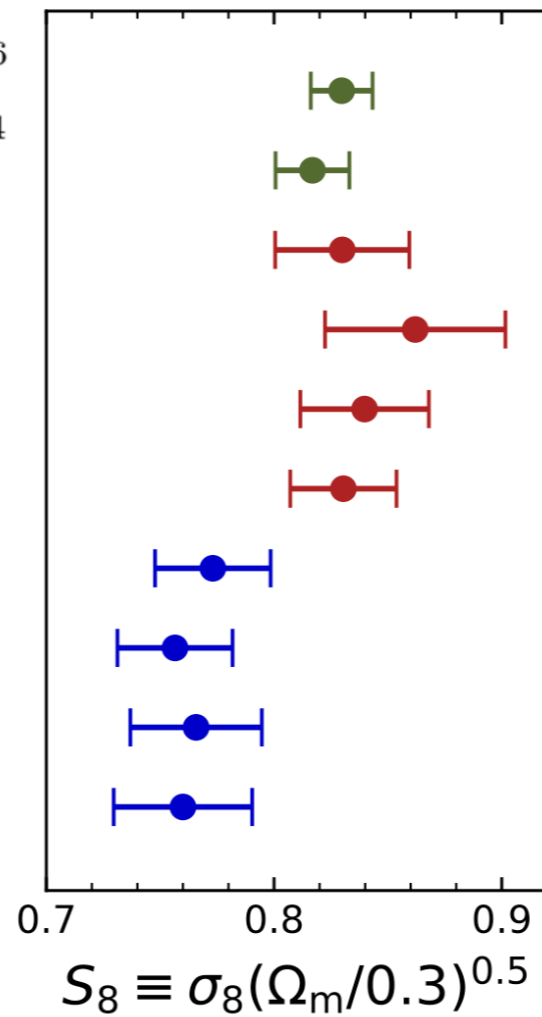
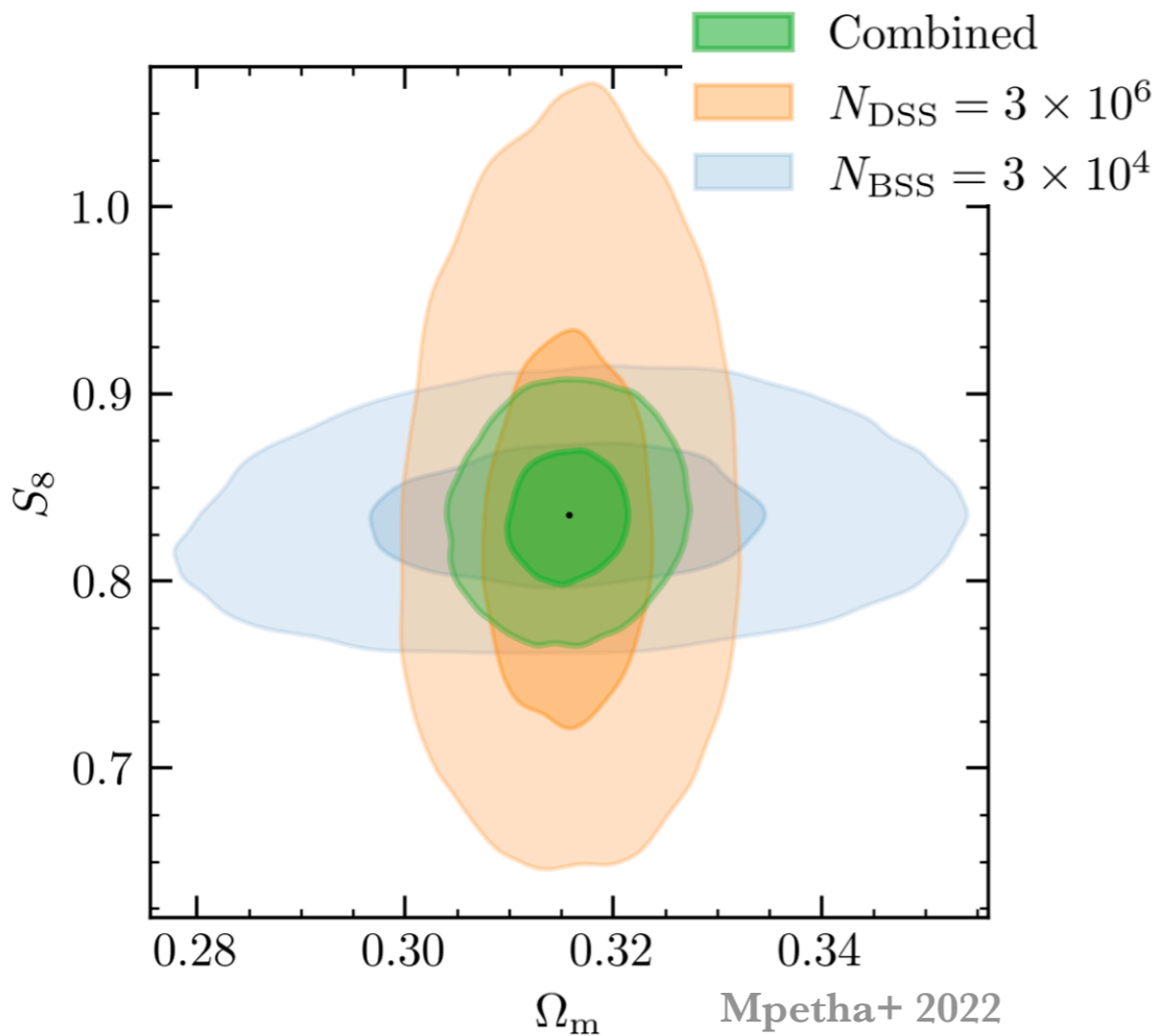
# GW WEAK LENSING



- Planck CMB aniso.
- Planck CMB aniso. (+ $A_{\text{lens}}$  marg.)
- Planck CMB lensing + BAO
- SPT CMB lensing + BAO
- ACT CMB lensing + BAO**
- ACT+Planck CMB lensing + BAO**
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- KiDS-1000 galaxy lensing + BAO
- HSC-Y3 galaxy lensing (Fourier) + BAO
- HSC-Y3 galaxy lensing (Real) + BAO

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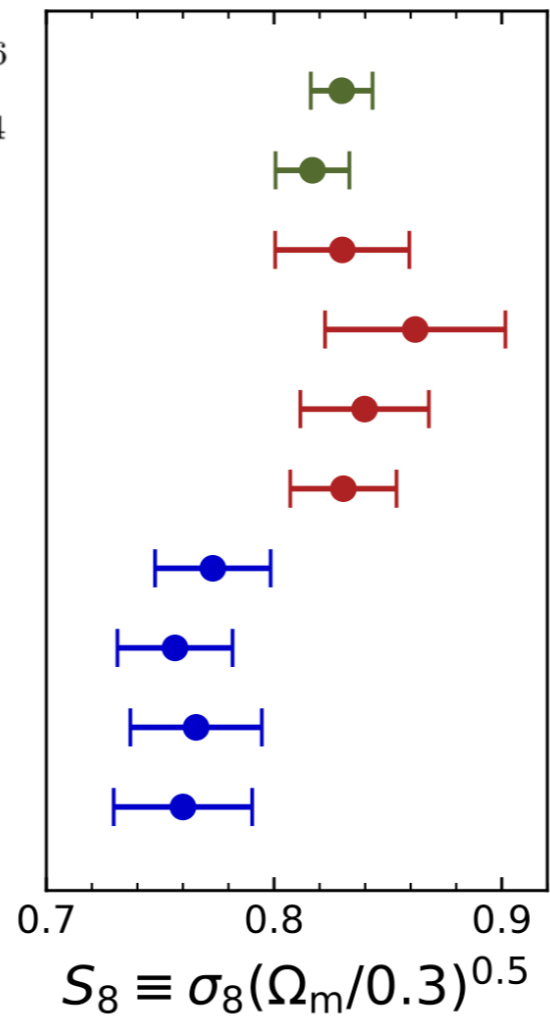
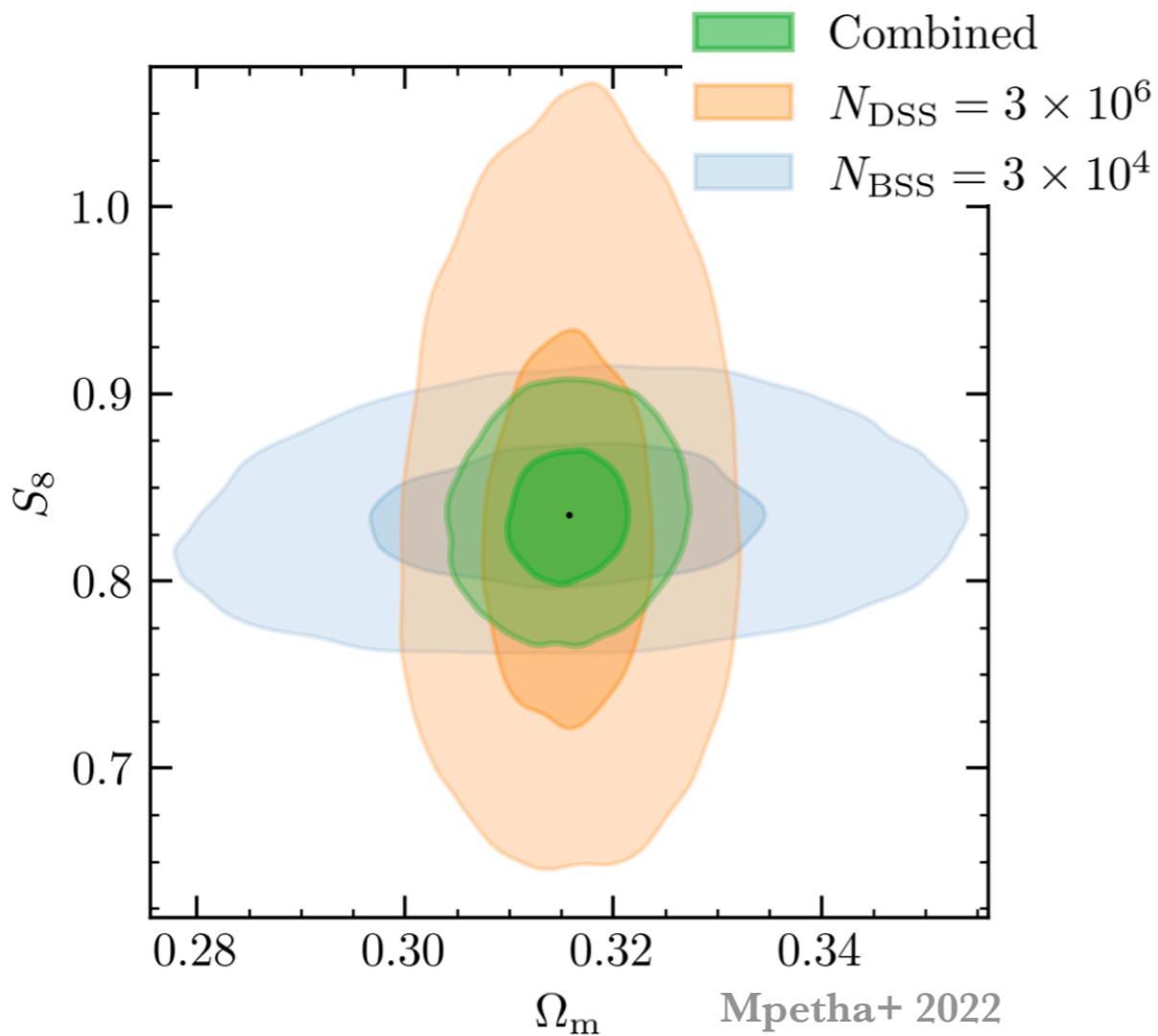
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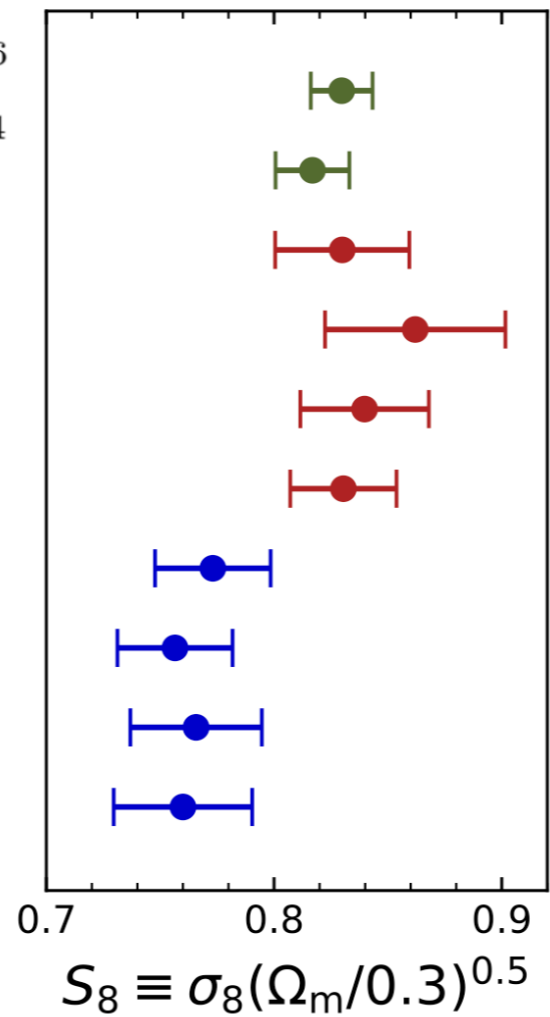
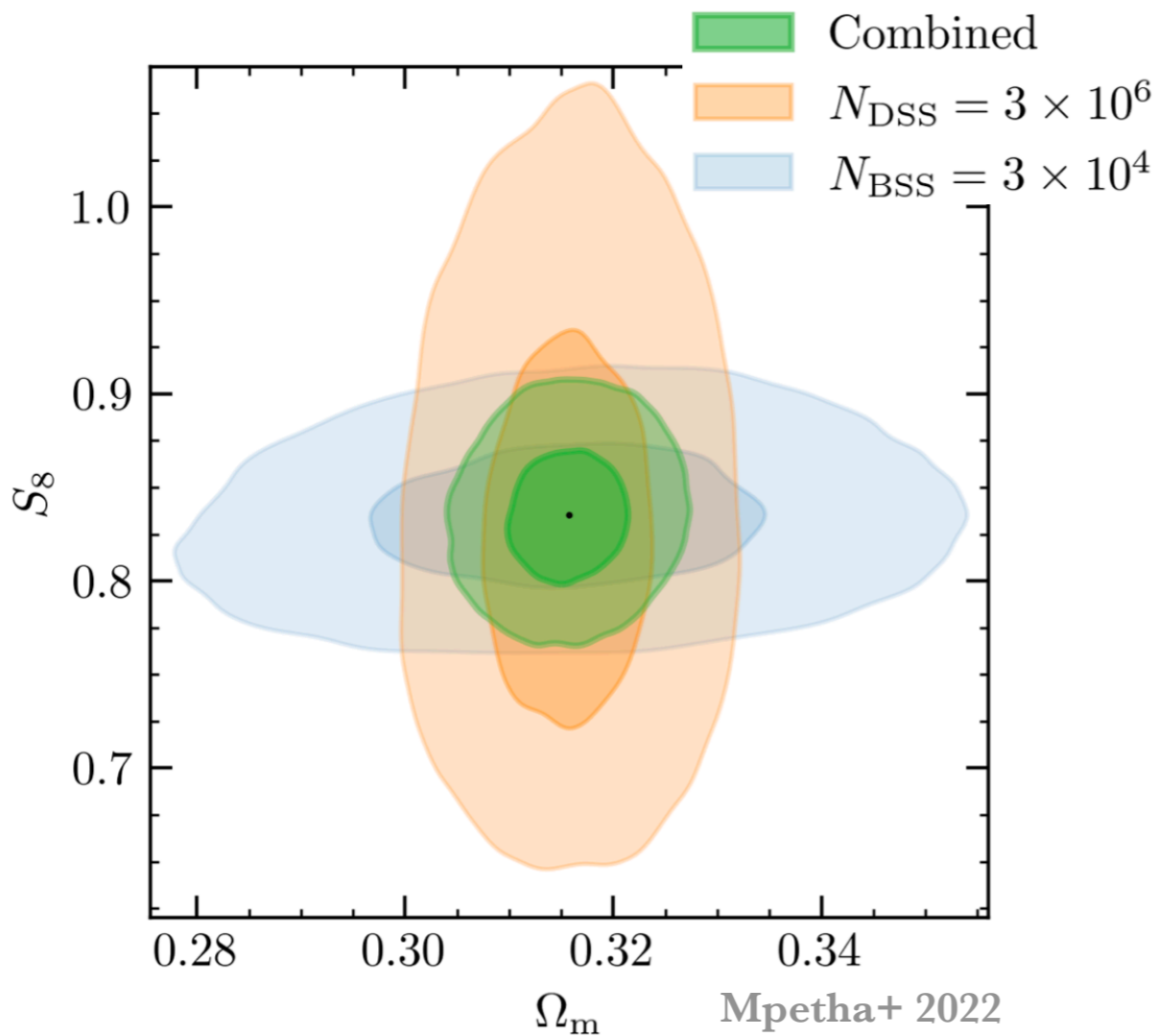
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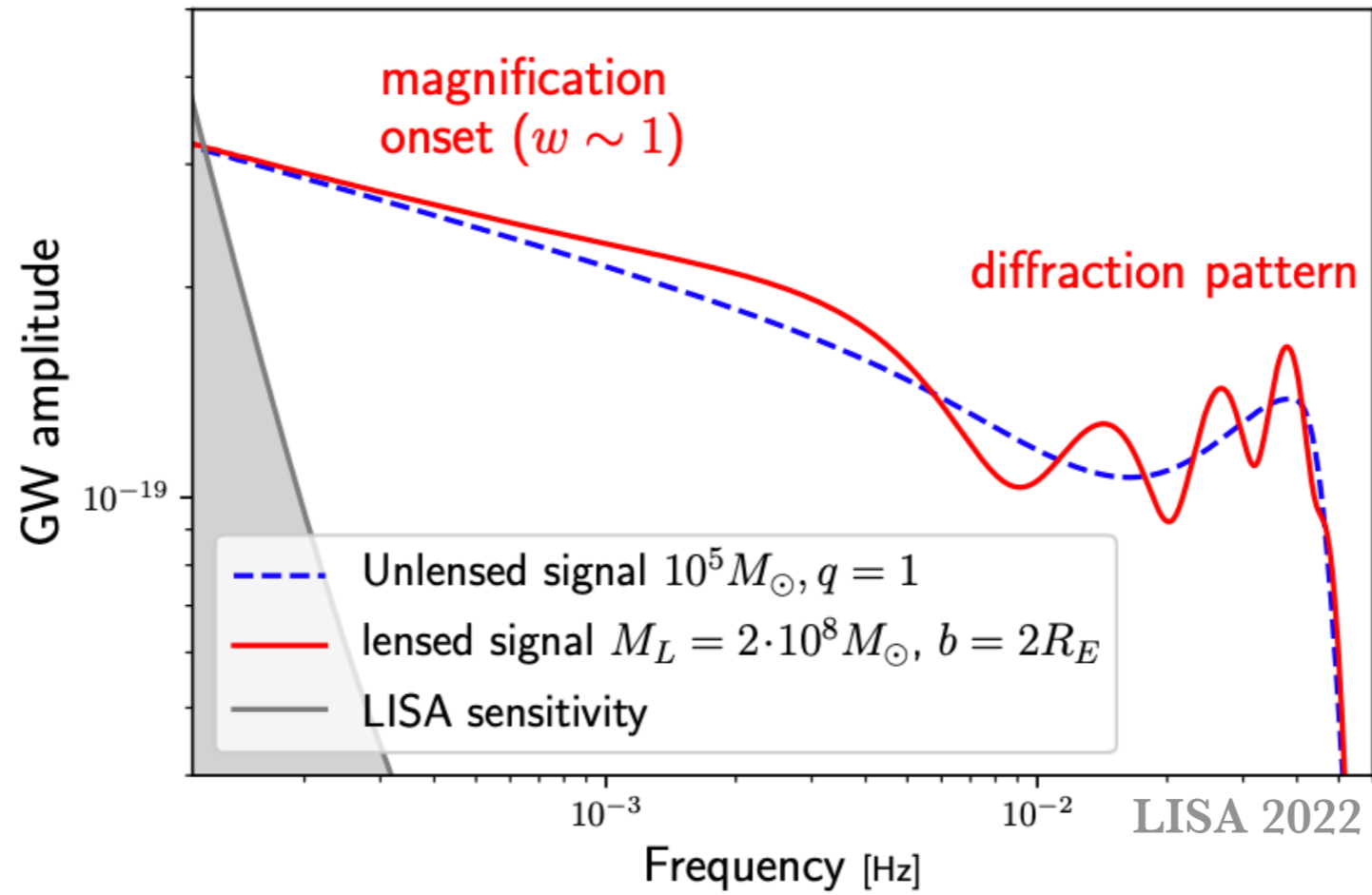
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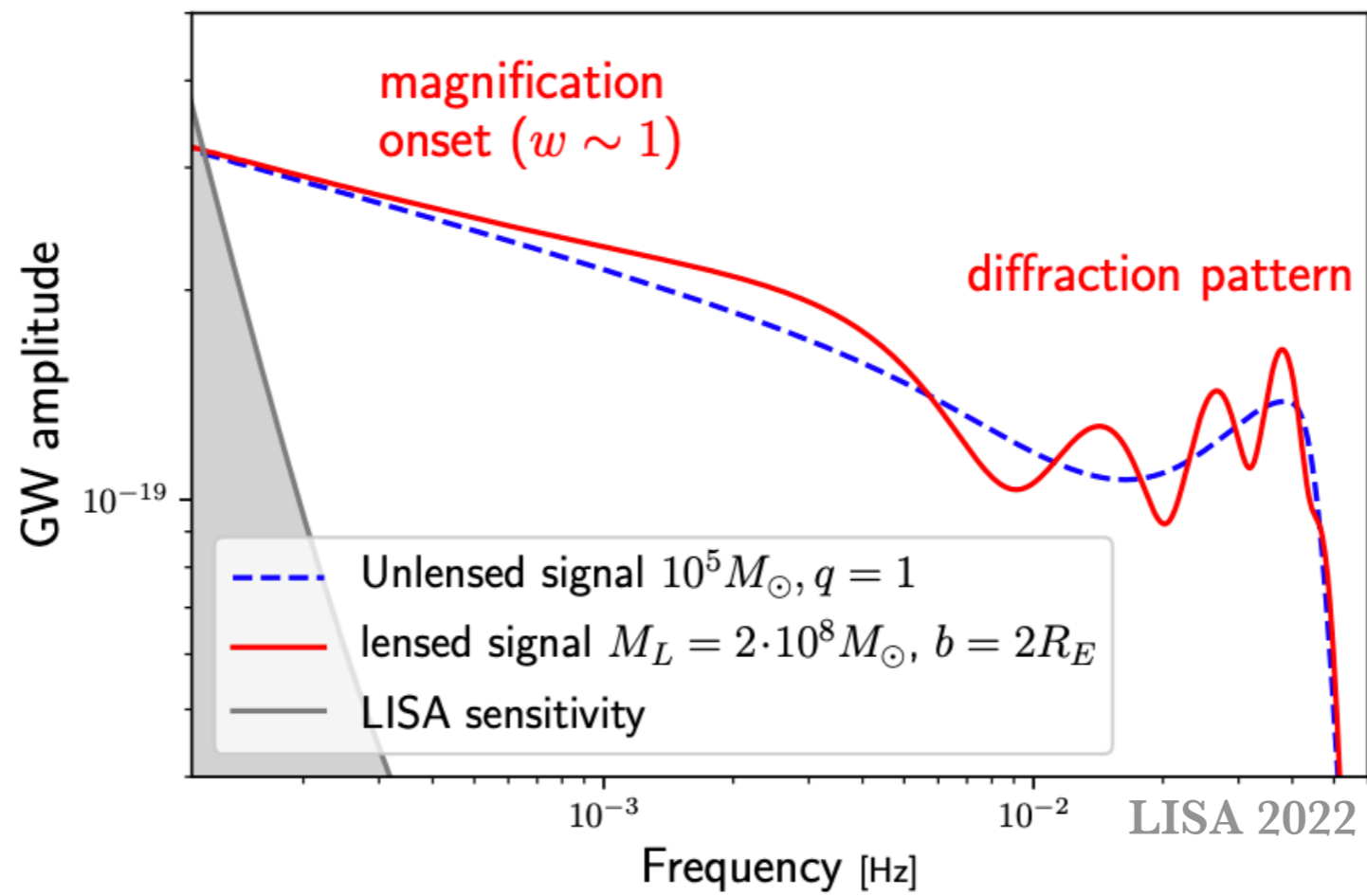
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  - LISA:  $M_L \sim 10^6 - 10^8 M_\odot$

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- Up to 2% mergers with detectable distortions by low-mass DM halos in CDM [Gao+ 2022]

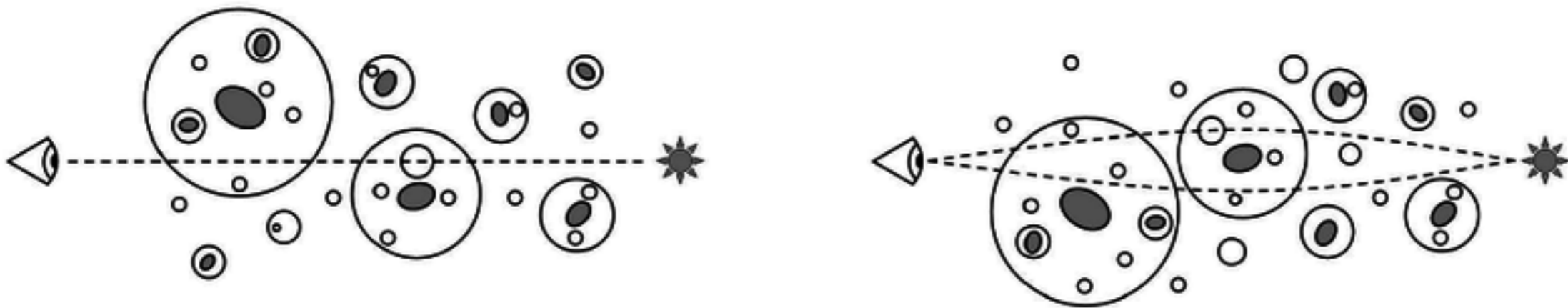


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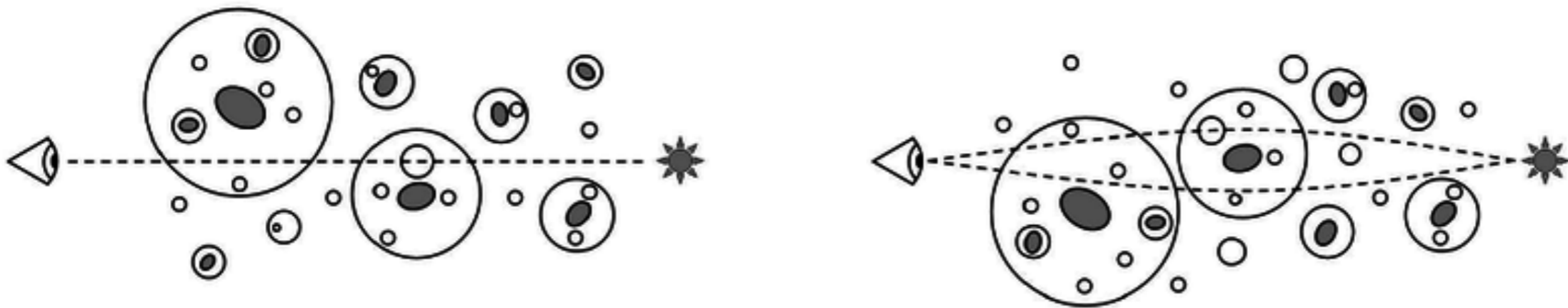
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  - Different for individual strongly-lensed images [Tambalo+2023]





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