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Given 1960's waveform and data analysis (but 2015 detector technology) could GW150914 have been found in the data?

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Why the topic?

Popular among students

Multi disciplinary

Excellent Introductory Analysis- Authentic Hands on Experience of Real time data

Interest in Astronomy

Timeline

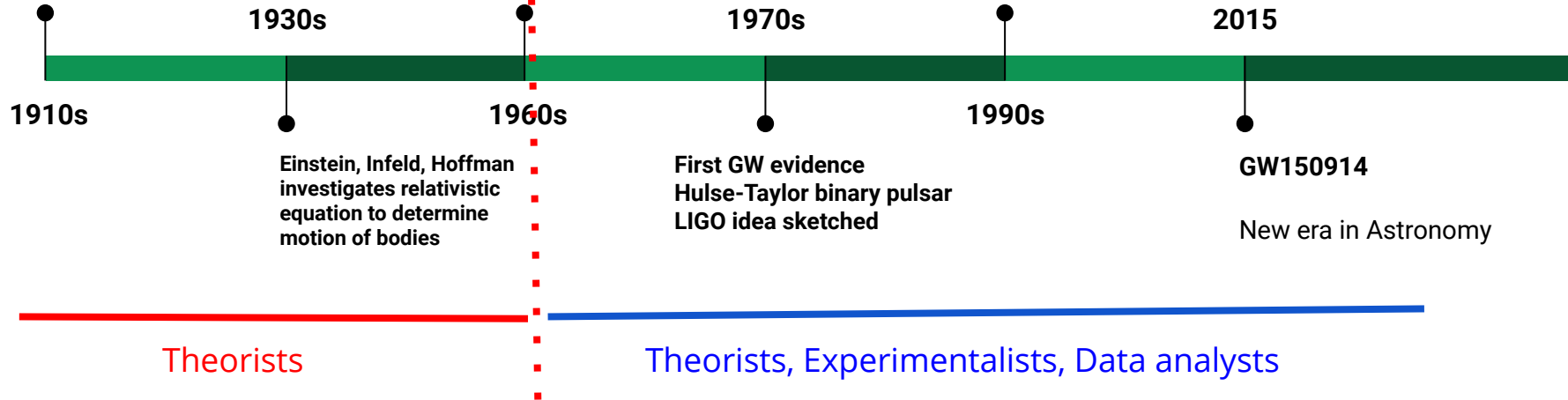


Rainer Weiss, Barry Barish, Kip Thorne

Einstein's Theory of General Relativity

Interferometry was suggested
Experiments: Weber Resonant antenna
Peter and Mathews use 0 PN waveforms

Nobel Prize
LIGO construction
Solved 2 body problem in GR
Numerical relativity simulations



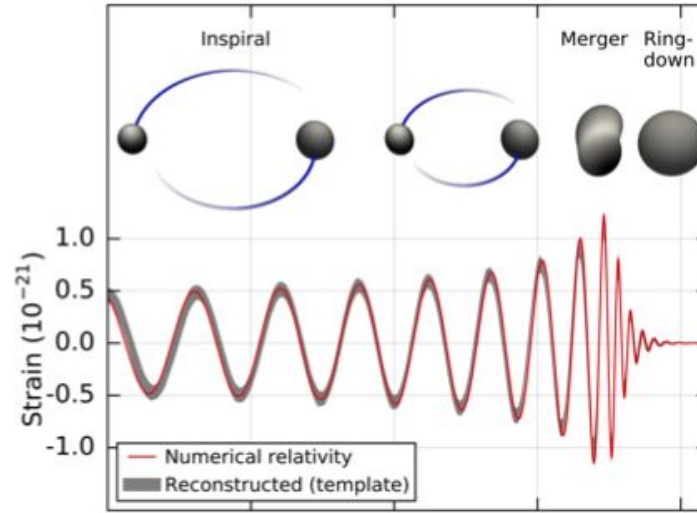
1960s	Present
0 PN waveform Newtonian order is the first approximation for the GW signal (Newtonian dynamics with Einstein's quadrupole formula)	Next to...Next to.... Next to.... Leading order waveform
Dependent largely on mass	Parameterised by masses, spins, distance, etc
Match filtering Noisy signal is convoluted with a theoretically constructed template (gives SNR)	Match filtering technique, Signal Vetoes, Numerous algorithms for full detection pipelines
No idea how to detect	LIGO Detectors

Compact binary coalescence waveform:

Inspiral, Merger, Ringdown explained using Post Newtonian expansions and Numerical Relativity

0 PN Waveform

- Inspiral Only, no merger and ringdown
- No relativistic corrections
- Very Simple



Inspiral of compact binaries in Newtonian approximation

The data output of the detectors is the measure of strain of GW.

GW strain in time domain:

$$h^+(t) = A(t) \cos(\Phi_{GW}(t))$$

$$h^\times(t) = A(t) \sin(\Phi_{GW}(t))$$

Amplitude:

$$A(t) = -(2G\mu/c^4)(\pi G\mu f_{GW}(t))^{2/3}$$

Phase:

$$\Phi_{gw}(t) = -\frac{16\pi}{5} f_{gw}(t_c - t)$$

Time of coalescence:

$$t_c = \frac{5}{256\eta} \frac{G\mu}{c^3} \left(\frac{\pi G\mu f_0}{c^3} \right)^{-8/3}$$

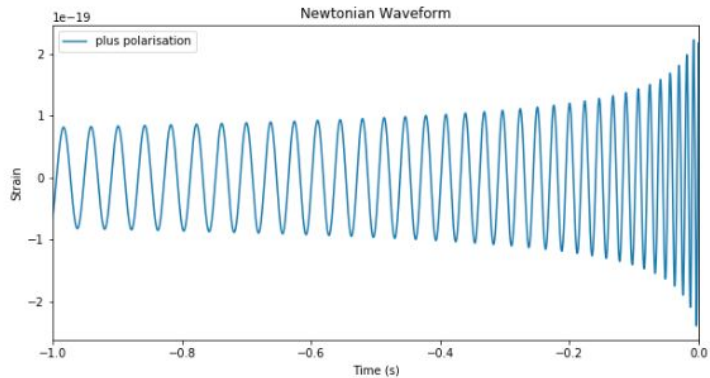
Uses

Kepler's law,

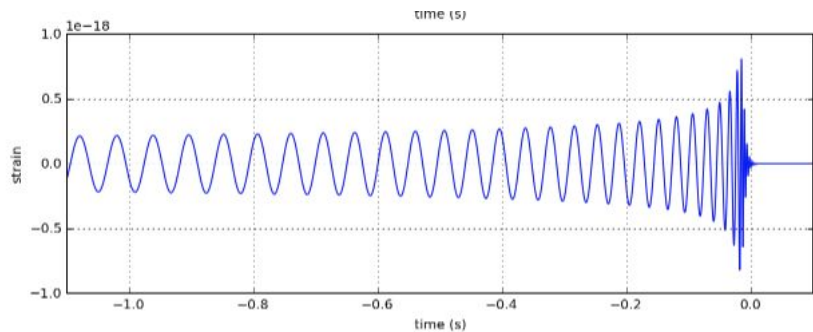
Newton's laws of motion,

Newton's universal law of gravitation, and

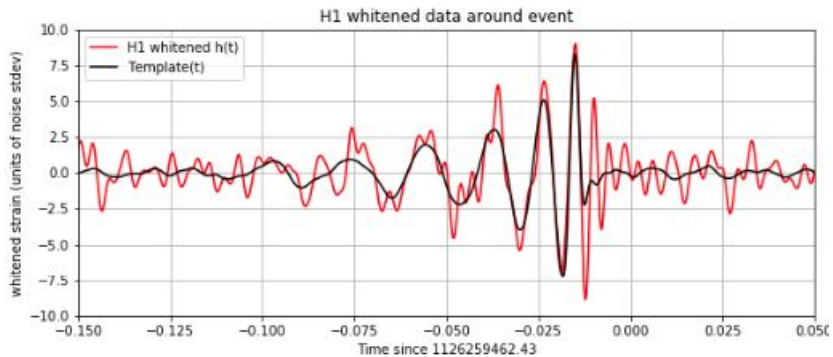
Einstein's quadrupole formula



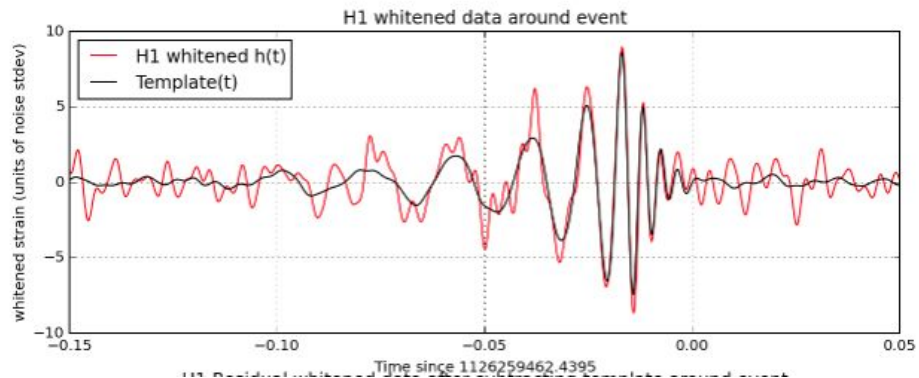
0 PN Waveform



LIGO Waveform



0 PN Waveform + Data



Data + LIGO Waveform

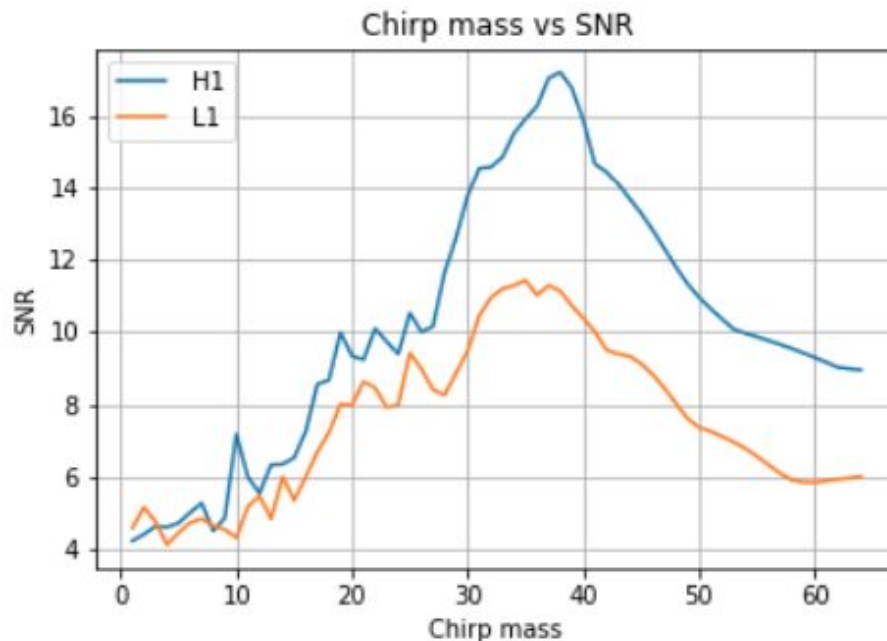
Chirp mass

The combination of the two component masses which sets how the binary inspirals together

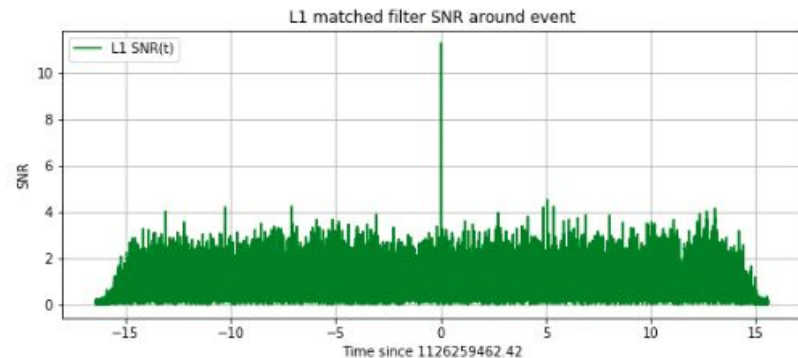
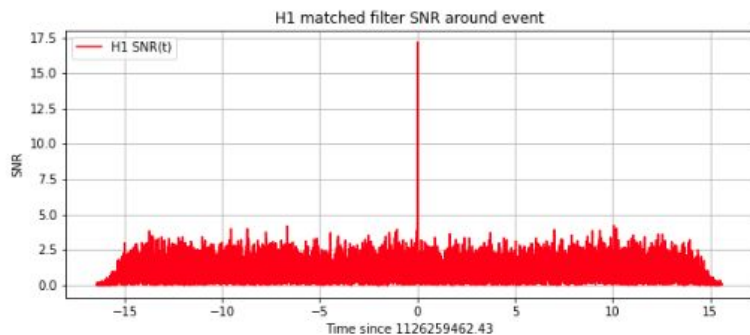
$$\mu = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$

SNR (Signal to noise ratio)

A value which measures strength of the **signal** compared with the sources of **noise** that could potentially contaminate it



How detection works



	LIGO	Me
SNR (H1)	18.6	17.2
SNR (L1)	13.2	11.3
Combined SNR	22.8	20.6

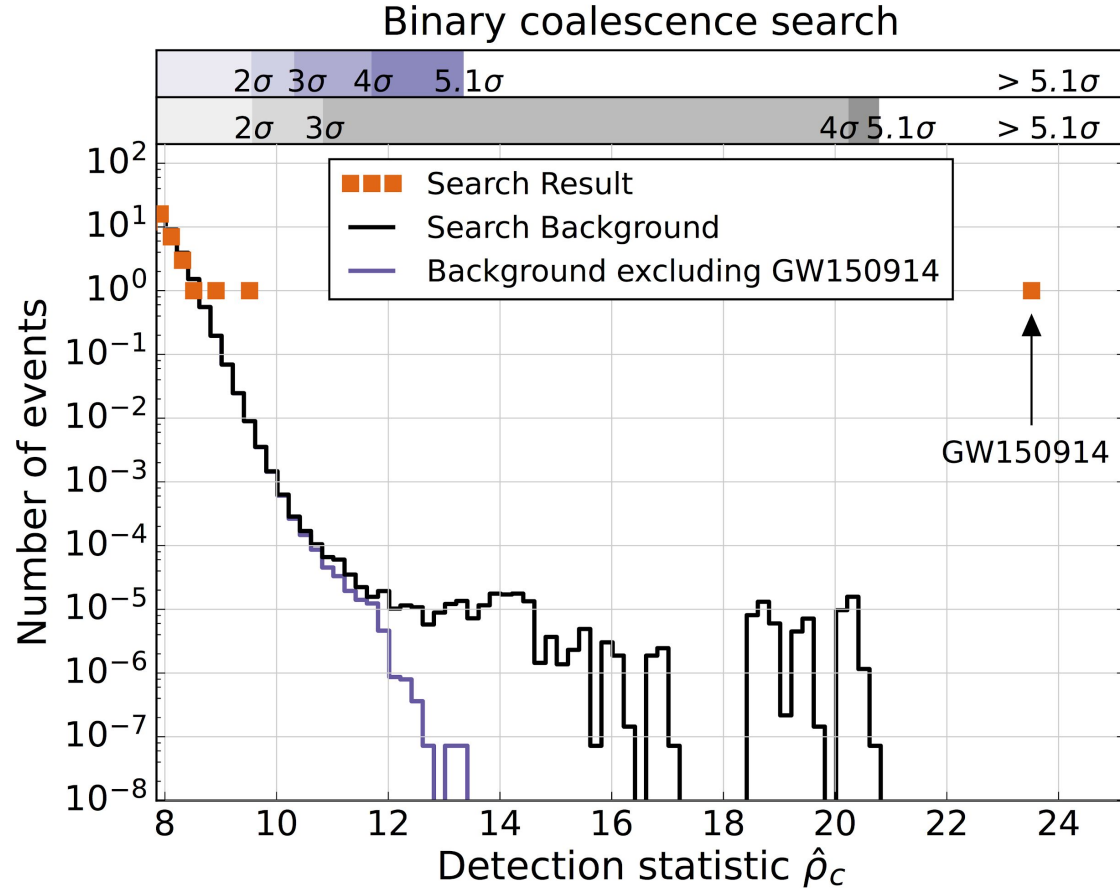
LIGO > Me

LIGO Result

Significance

P-value: 10^{-14}

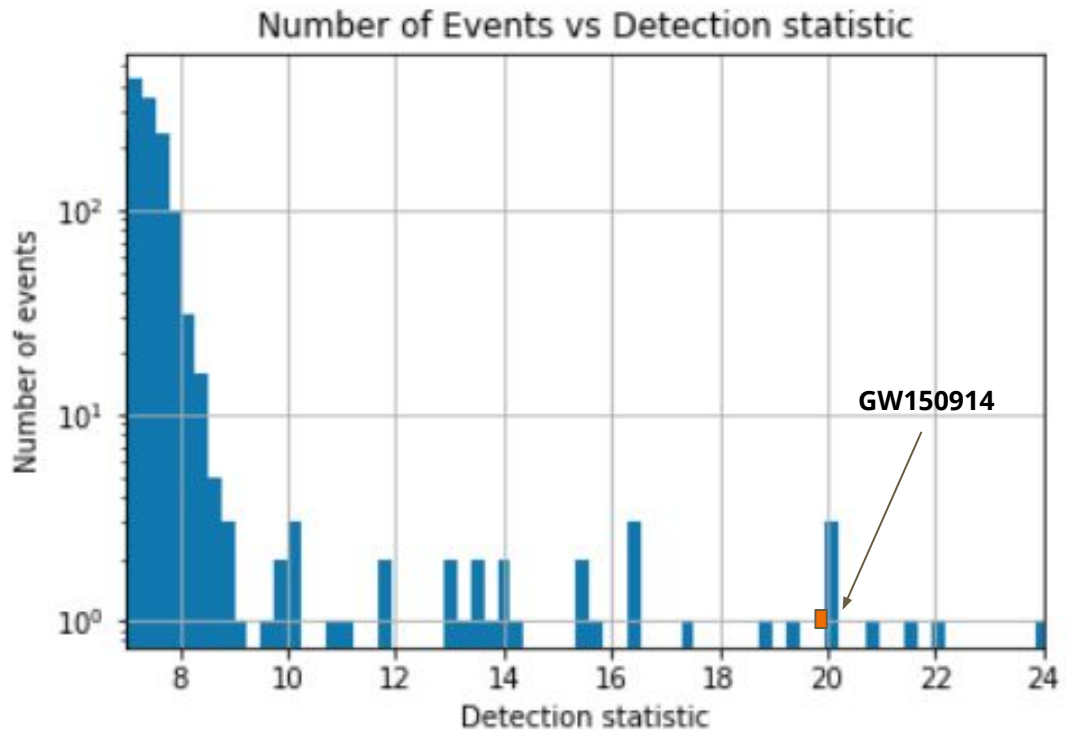
Probability that match would happen by chance due to a random noise fluctuation if the data was purely noise.



My 0 PN Result

Significance

P-value: 0.0104



Signal consistency test

We perform **Chi Squared** statistic to test how well the data actually fits the model

Chi Squared test



Compare chirp mass

LIGO	Me
$30.4^{+2.1}_{-1.9} M_{\odot}$	$37.5^{+3.6}_{-3.6} M_{\odot}$

Conclusion

GW150914 is detectable with a Newtonian Waveform

Not suitable for parameter estimation

Time for Questions :)

Thank You !